

**13<sup>th</sup> Lomonosov Conference on Elementary Particle Physics  
Moscow State University, Russia  
August 23 – 29, 2007**

# **Big-Bang Cosmology, Nucleosynthesis and Neutrino Oscillation**

**Taka Kajino**

**National Astronomical Observatory  
Dept of Astronomy, Grad School of Science, University of Tokyo**

# OUTLINE

Burbidge, Burbidge, Fowler & Hoyle (B<sup>2</sup>FH, 1957) — 50 yr

Pontecorvo ( $\nu$  Oscillation, 1957~60) — ~ 50 yr

Koshiba (SN  $\nu$ , 1987) — 20 yr

Smoot & Mathar (COBE, 1992) — 15 yr

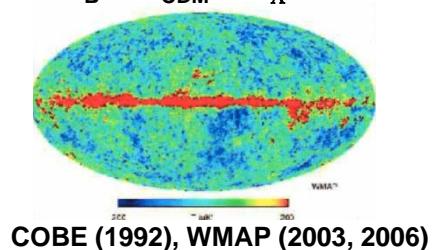
X-process is known today to be the Big-Bang Nucleosynthesis (BBN) !

Power of the BBN to constrain Cosmological Theories !

- DARK ENERGY ( $\Omega_{\Lambda} = 0.74$ ), CDM ( $\Omega_{CDM} = 0.22$ ) ?
- BARYON ( $\Omega_B = 0.04$ ) consistent with particle-nuclear theory ?  
→  $^6\text{Li}$ ,  $^7\text{Li}$  problems

Universe is flat & accelerating !

$$\Omega_B + \Omega_{CDM} + \Omega_{\Lambda} = 1$$



COBE (1992), WMAP (2003, 2006)

Supernova  $\nu$ -oscillation – MSW Effect !

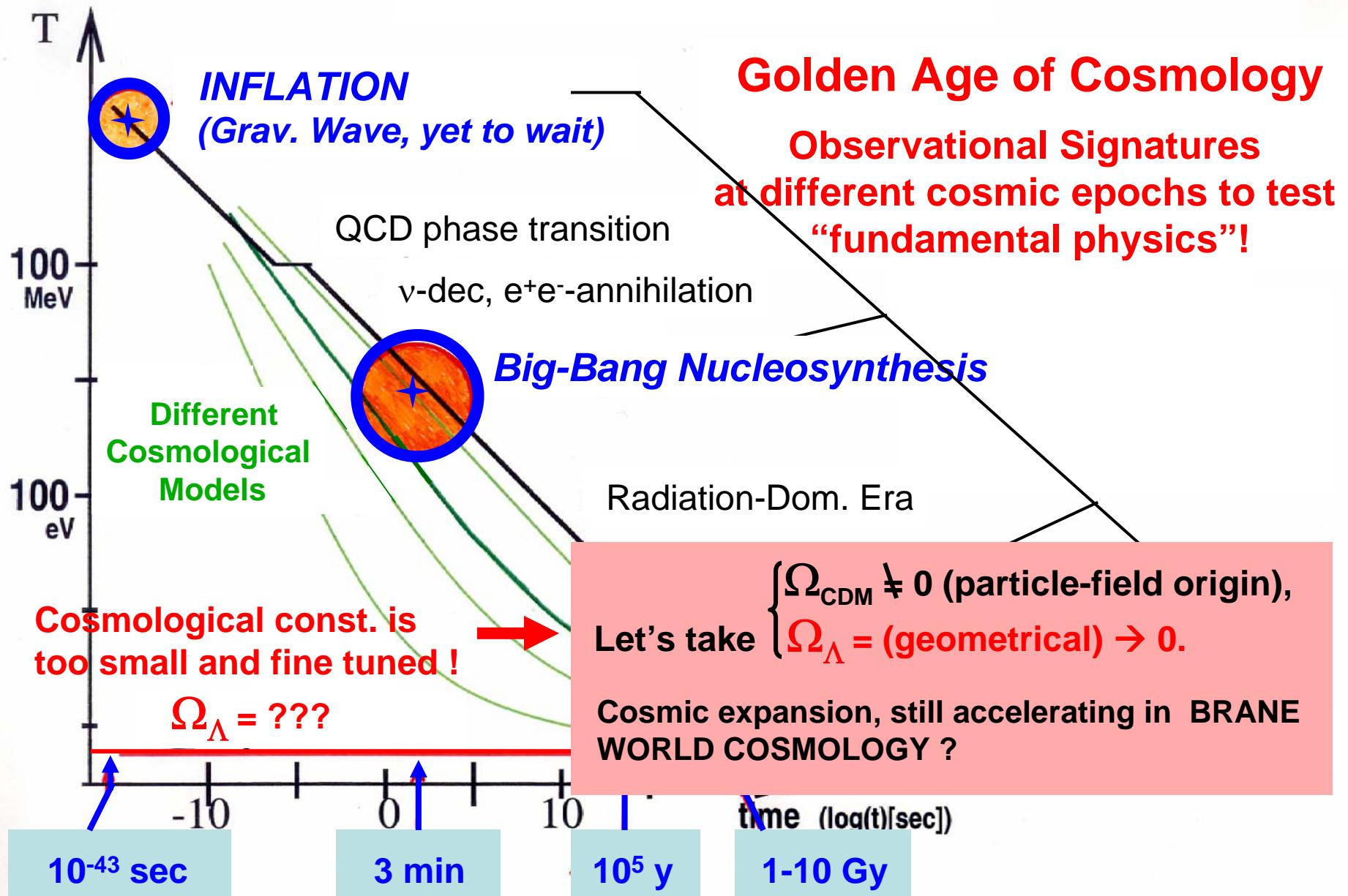
X-process operates in SN  $\nu$ -process, too !

- New Method using “MSW Effect” to determine  $\theta_{13}$  and Mass Hierarchy !

SN1987A



# Thermal History of our Expanding Universe



# *Brane World Cosmology with $\Omega_\Lambda = 0$*

— A Model for Accelerating Universe ? —

Motivated by the D-brane solution  
in 10 dim STRING THEORY

Randall-Sundrum II; PRL 83 (1999)

The Universe is embedded  
in a 5 dim spacetime

Brane

||

4D-Einstein Universe

CDM particles flow in and out  
between brane and bulk !  
→ Mass-Energy Exchange

CDM particles (SUSYs, etc.)

5-th bulk dim. Z

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}(\bar{\rho} + \rho + \rho_\chi) + \frac{k}{a^2}$$

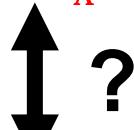
Dark Radiation term

$$\dot{\rho}_\chi + 4H\rho_\chi = -\alpha/a^q \times \rho_{cr}H,$$

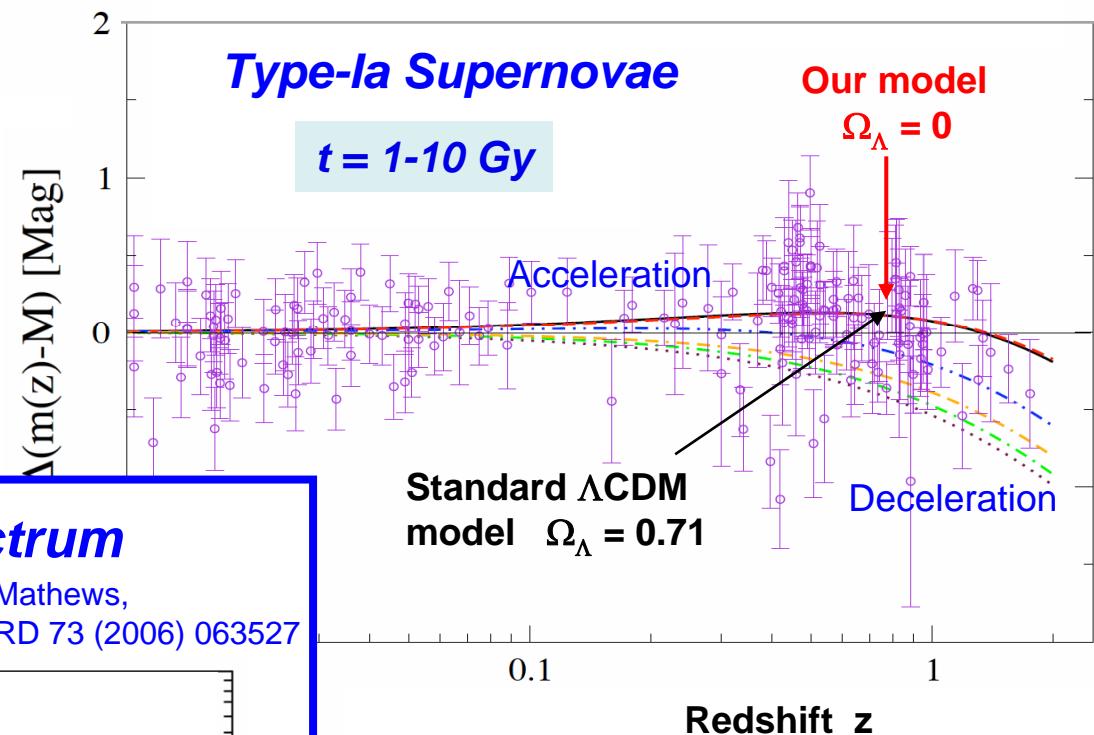
$q$  = adjustable parameter

## BRANE WORLD COSMOLOGY

with  $\Omega_\Lambda = 0$

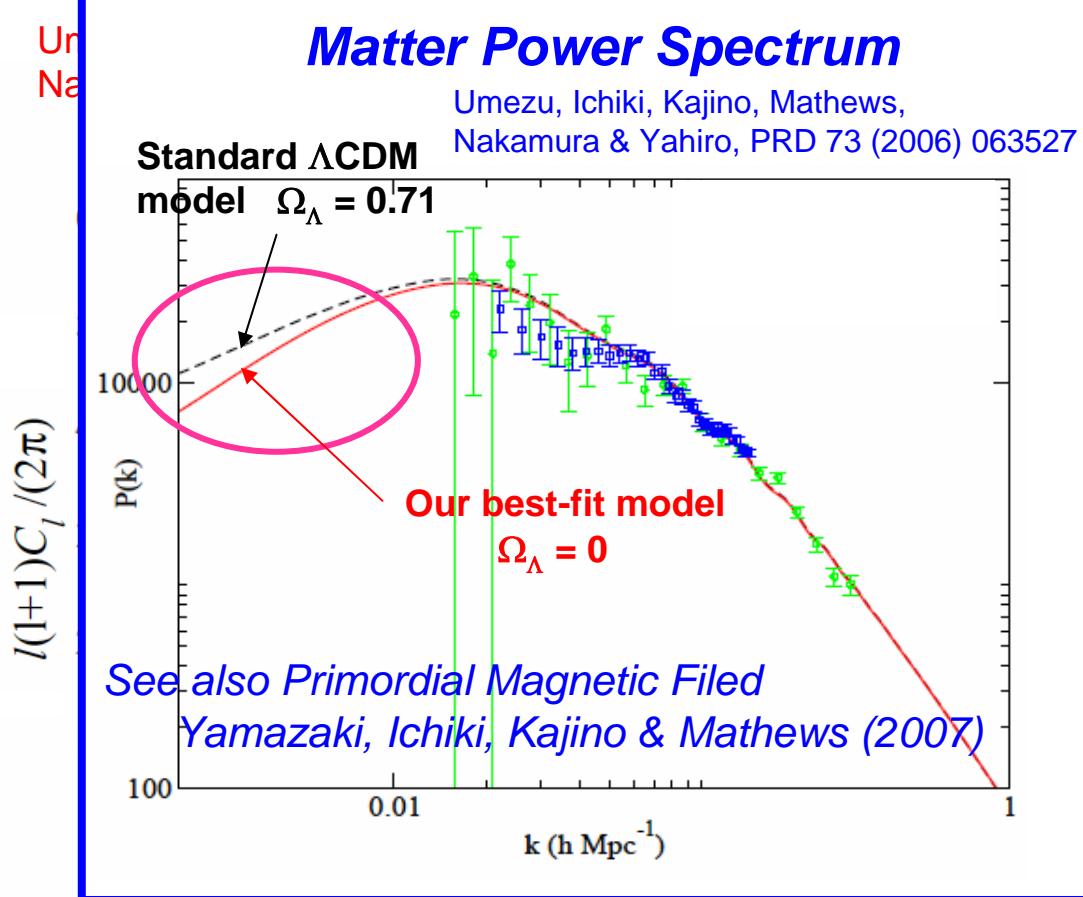


Standard  $\Lambda$ CDM  
with  $\Omega_\Lambda \neq 0$



## Matter Power Spectrum

Umezu, Ichiki, Kajino, Mathews,  
Nakamura & Yahiro, PRD 73 (2006) 063527



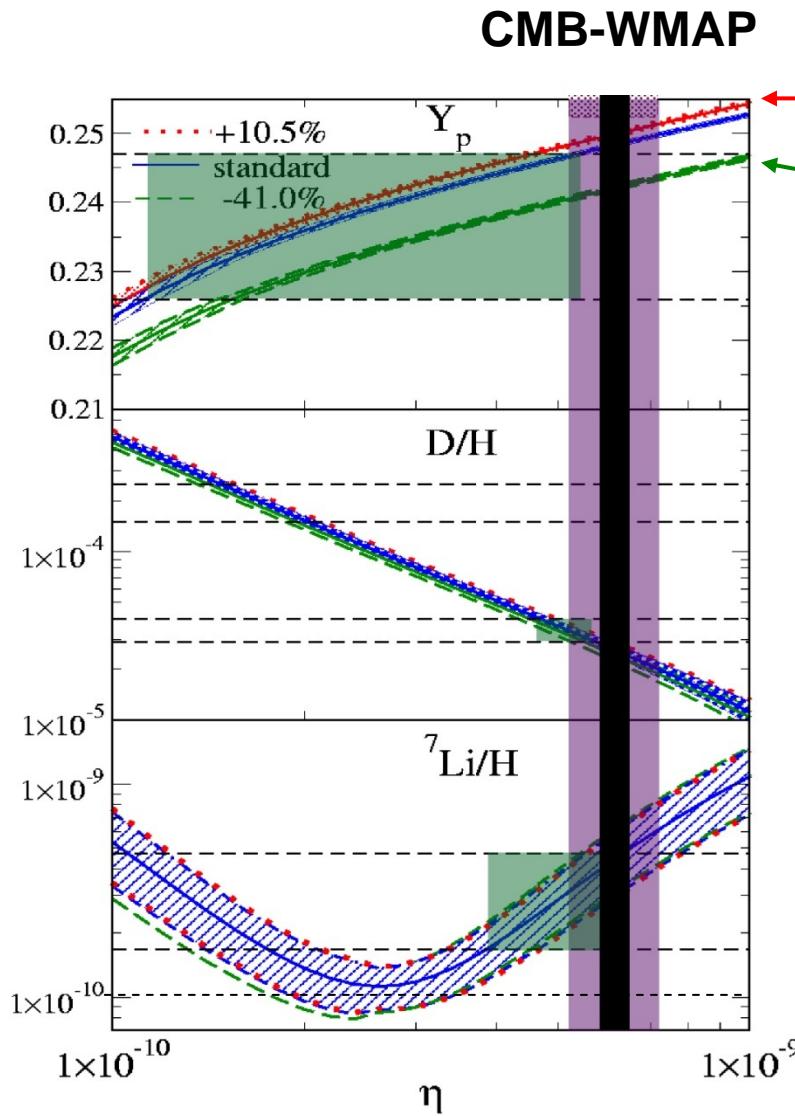
ACCELERATING  
Universal expansion  
without  $\Omega_\Lambda$  !

Multiple I

# BBN constrains Brane World Cosmology

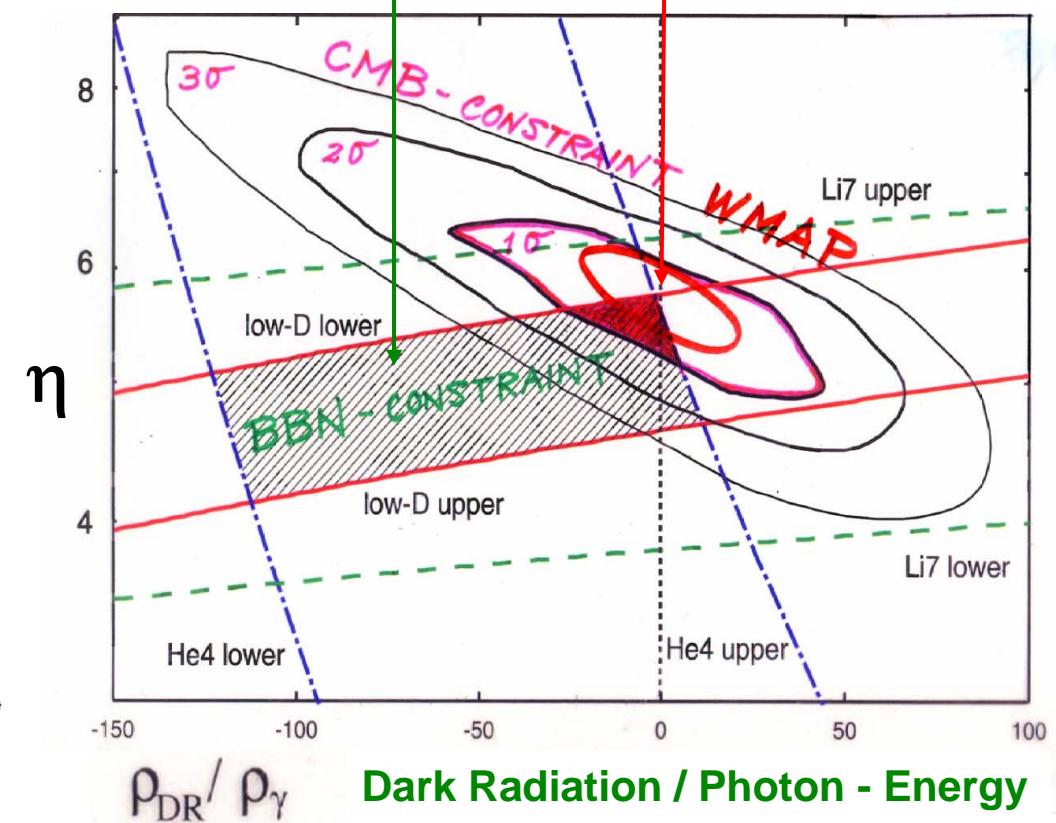
Ichiki, Garnavich, Kajino, Mathews & Yahiro, PRD 68 (2003) 083518

$t = 3 \text{ min}$



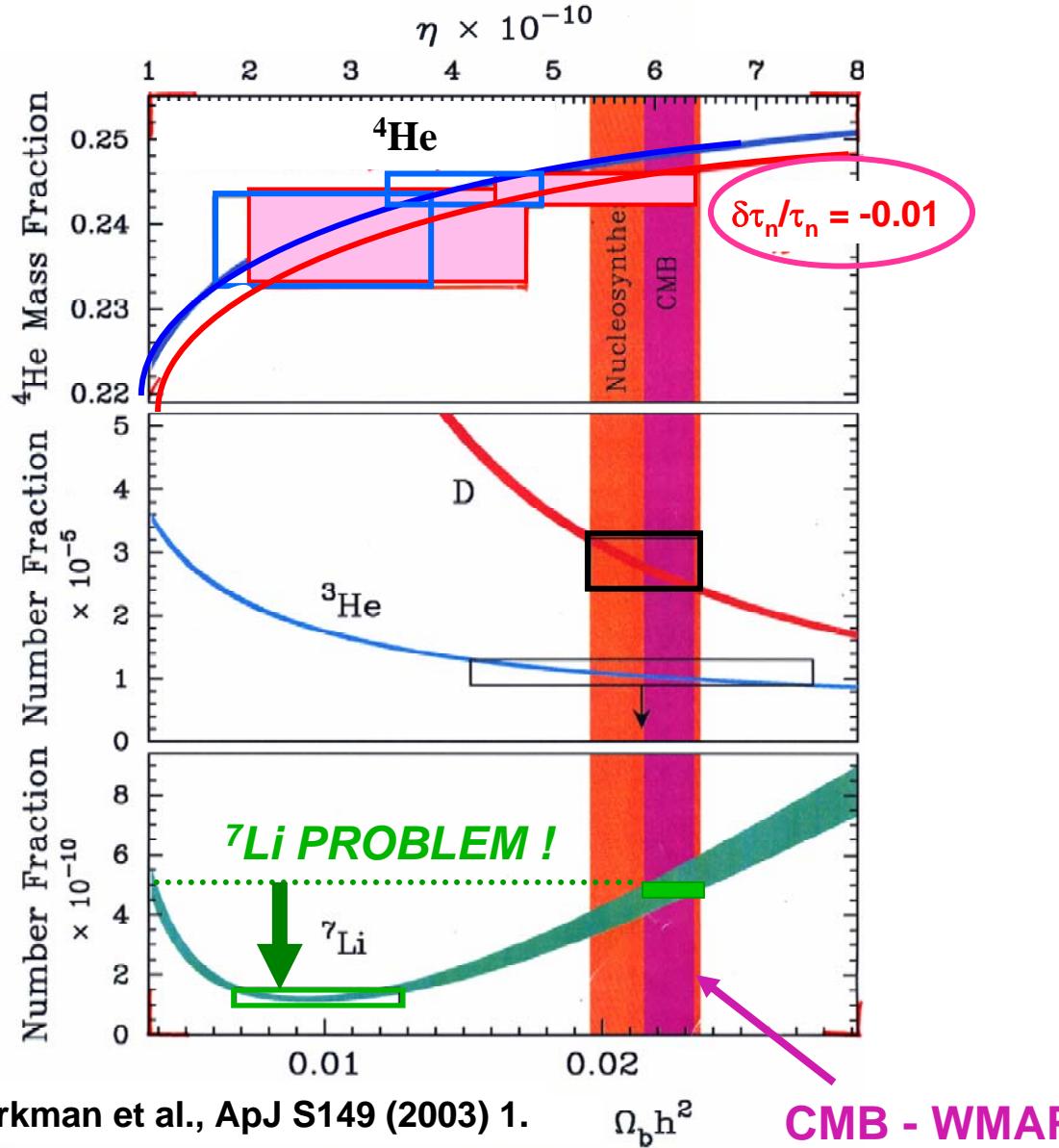
Standard BBN Model

Dark Radiation relaxes the tension between the CMB+D/H and  $^4\text{He}$ .



# BBN and Particle Physics

Smith, Kawano & Malaney, ApJ S85(2003) 219; Mathews, Kajino & Shima, PRD71 (2005) 21302 (R).



# Plateau like HIGH ${}^6\text{Li}$ ABUNDANCE --- primordial ?

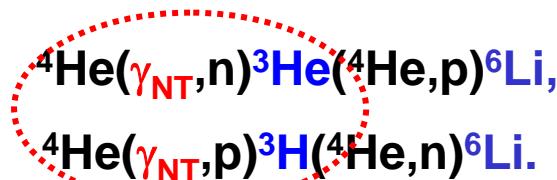
Factor 2~4 stellar depletion ?

Abundance scatter is too small to accept DEPLETION !

Relic DM particles (SUSY, etc.) X's decay to non-thermal photons:

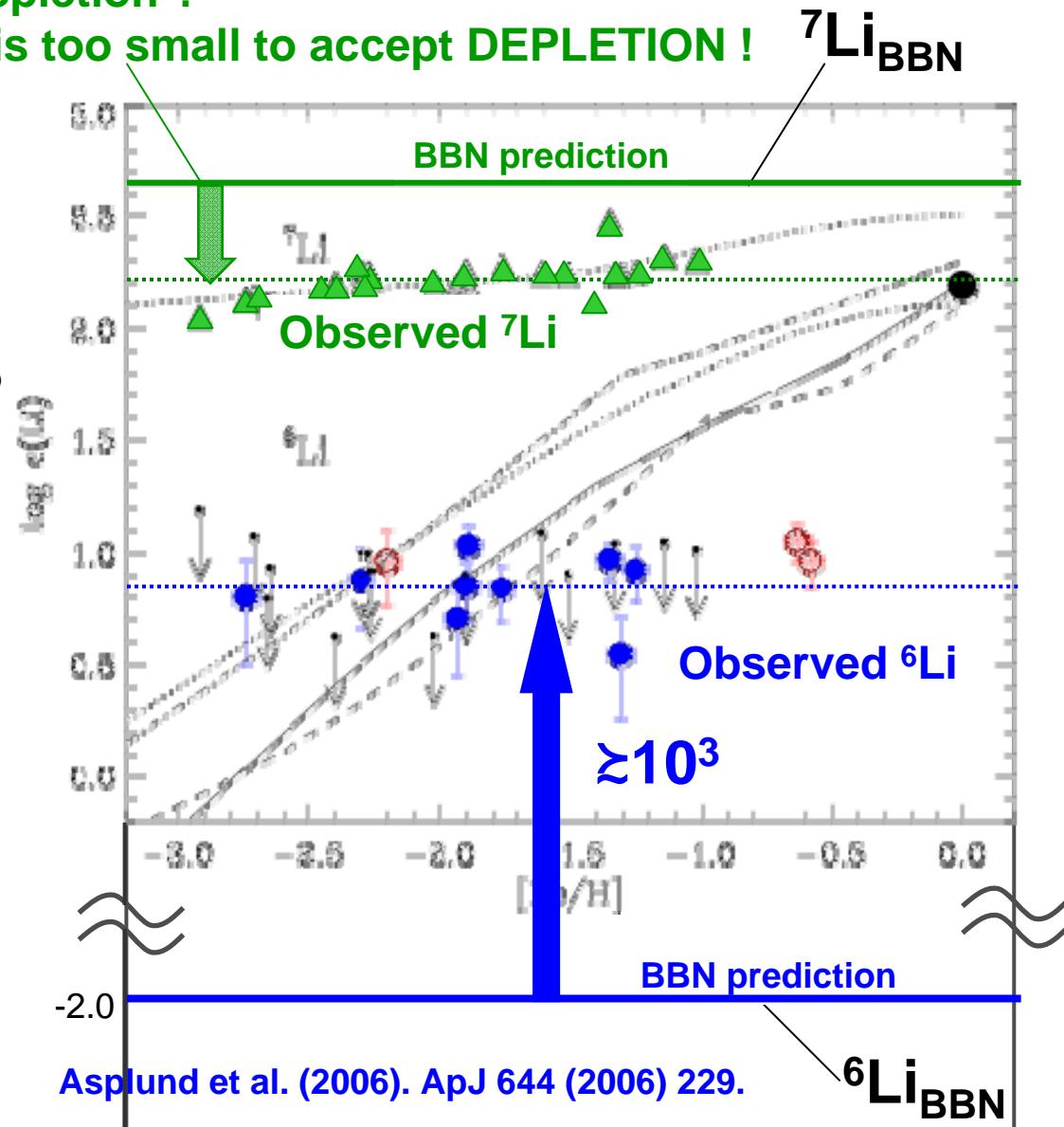
$\gamma_{\text{NT}}$ .

Non-thermal photons spalt  ${}^4\text{He}$  into  
 ${}^3\text{He}$ ,  ${}^3\text{H}$ . New class of BBN occurs:



critical reactions !

Ellis et al. (1986); Moroi and Kawasaki (1994); Jedamzik PRL 84 (2000) 3248;  
Cyburt et al., PRD 67 (2003) 103521; Ellis et al. PLB619 (2005) 30  
Kusakabe, Kajino & Mathews, D74 (2006), 023526.



# Theoretical of X decay: $X \rightarrow \gamma_{NT}$

Kusakabe, Kajino & Mathews, D74 (2006), 023526.

## Spectrum of non-thermal $\gamma_{NT}$ $p_\gamma(E_\gamma)$

Primary  $\gamma_{NT}$  interacts with CBRs

Pair creation ( $\gamma\gamma_{bg} \rightarrow e^+e^-$ )

Inverse Compton ( $e^\pm + \gamma_{bg} \rightarrow e^\pm + \gamma$ )

Then it degrades its energy by:

Compton scattering ( $\gamma + e^\pm_{bg} \rightarrow \gamma + e^\pm$ )

Bethe-Heitler process ( $\gamma + \text{nucl}_\text{bg} \rightarrow e^+ + e^- + \text{nucleus}$ )

Photon-photon scattering ( $\gamma\gamma_{bg} \rightarrow \gamma\gamma$ )

## Two Parameters

Life time of X

$$\tau_x$$

Number density \*  $E\gamma$  of X

$$\zeta_x = \frac{n_x^0}{n_\gamma^0} E_{\gamma 0}$$

## Reaction process

Rate equation  $\frac{dY_A}{dt} = \sum_P N_A(P) \left( -\frac{Y_A}{N_A(P)!} [A\gamma]_P + \frac{Y_P}{N_P(P)!} [P\gamma]_A \right) + \text{SBBN}$

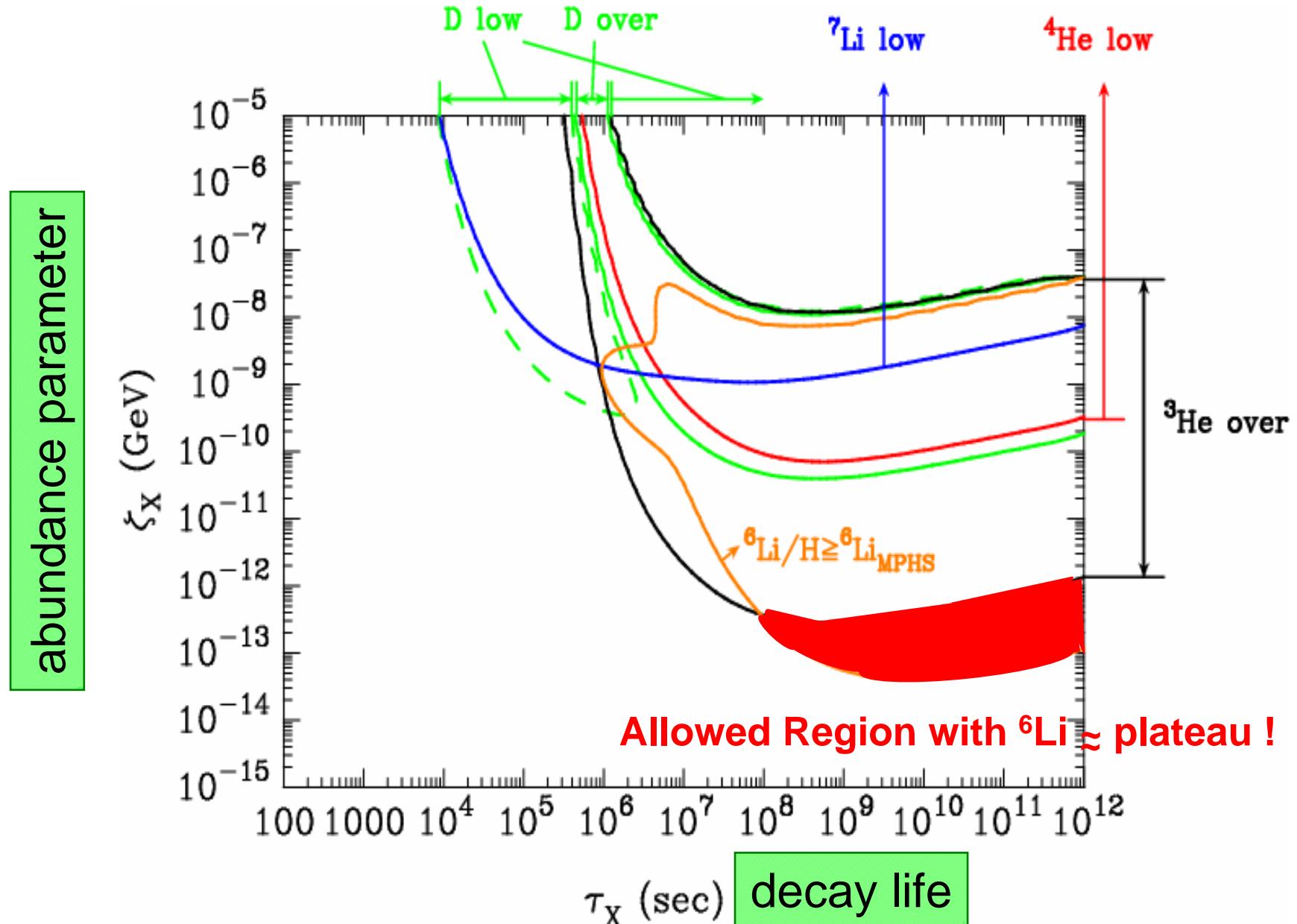
$$[A\gamma]_P \equiv \frac{n_\gamma^0 \zeta_x}{\tau_x} \left( \frac{1}{2H_r t} \right)^{3/2} \exp(-t/\tau_x) \int_0^\infty \left( \frac{\tau_x}{E_{\gamma 0} n_x} N_\gamma^{QSE}(E_\gamma) \right) \sigma_{\gamma+A \rightarrow P}(E_\gamma) dE_\gamma$$

Photon # density  $N_\gamma^{QSE}(E_\gamma) = \frac{n_x p_\gamma(E_\gamma)}{\Gamma_\gamma(E_\gamma) \tau_x}$

$$H_r = \sqrt{\frac{8\pi G \rho_{rad}^0}{3}}$$

# BBN Light Elemental Abundance Constraints on X particle properties

Kusakabe, Kajino & Mathews, Phys. Rev. D74 (2006), 023526.



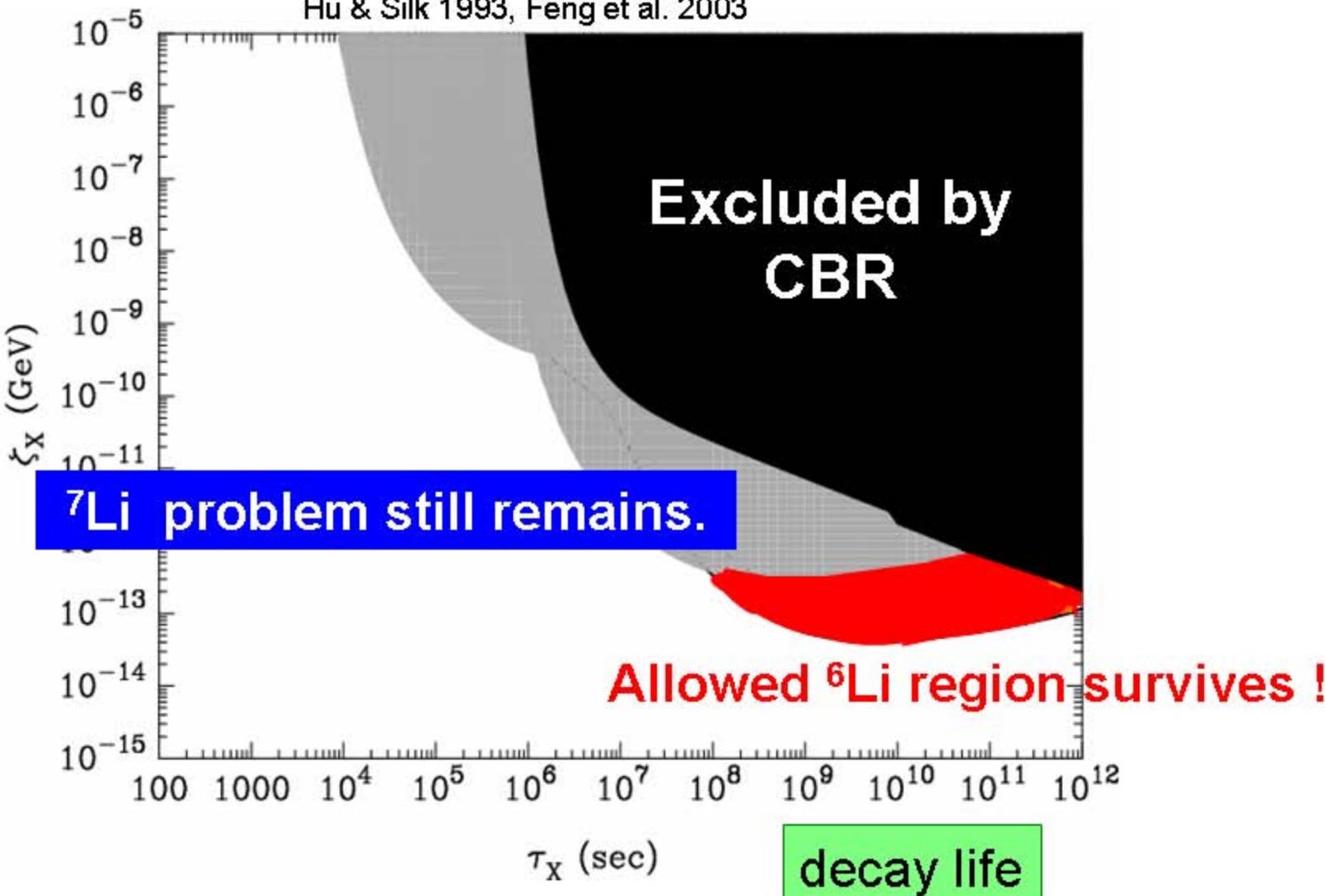
# Constraint from the CBR energy spectrum

Radiative decay causes CBR distortion from  
black-body distribution by  $e^\pm \gamma_{BG} \rightarrow e^\pm \gamma$

Another Constraint

Hu & Silk 1993, Feng et al. 2003

abundance parameter



# Case of Leptonic X-

Kusakabe, Kajino, Boyd, Yoshida, and Mathews (2007)

If relic X- particle is leptonic,  
X's form bound exotic nuclei  
like  ${}^4\text{He}_X$ ,  ${}^7\text{Be}_X$ ,  ${}^4\text{He}_{XX}$ ,  ${}^7\text{Be}_{XX}$ ,  
etc.

**Recombination of X particles**  
destroys normal nuclei, and  
new class of BBN proceeds:



Pospelov (2006), Hamaguchi et al. (2007)



${}^8\text{B}_X^*$  = nuclear excitation

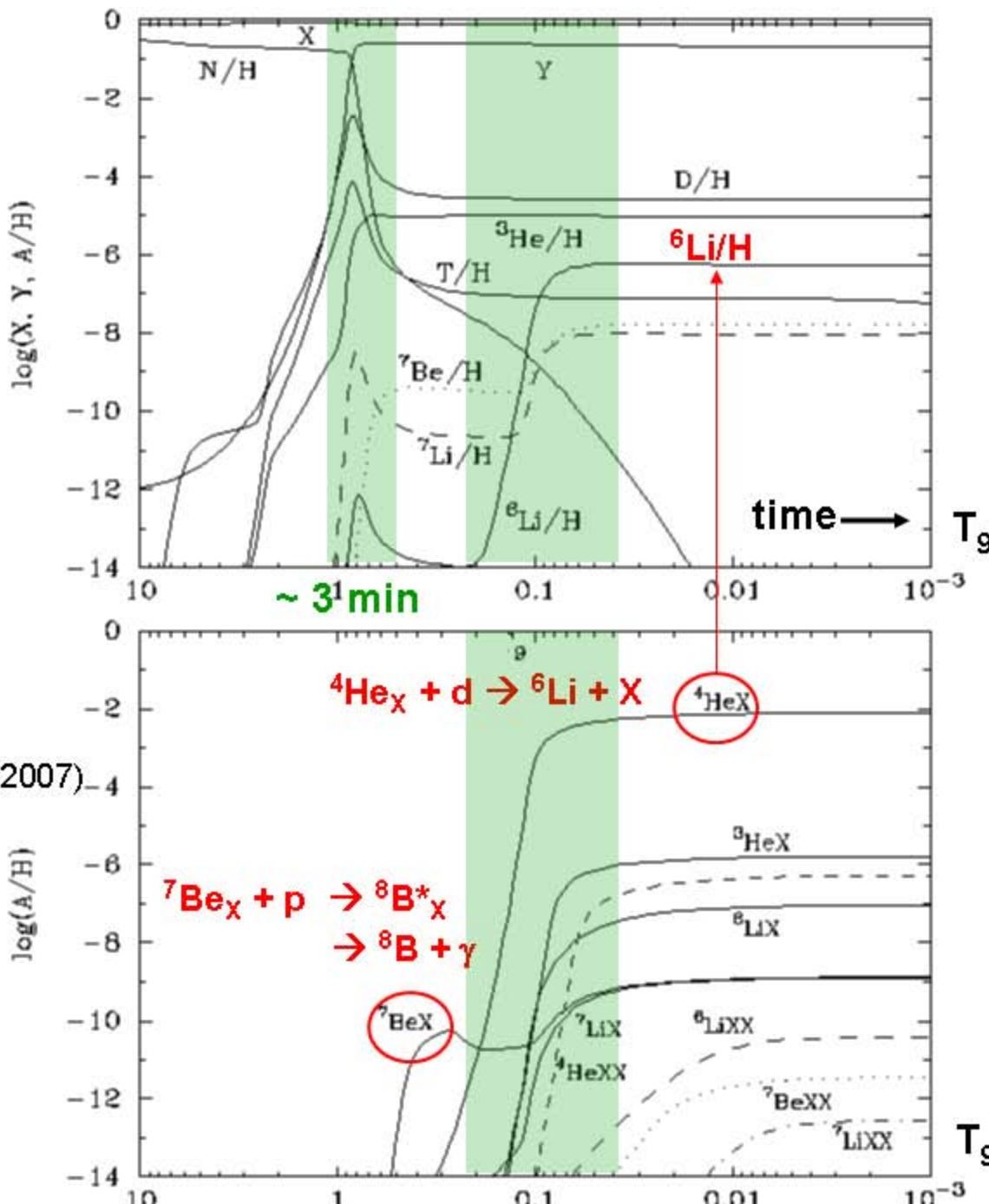
Kusakabe et al. (2007)

${}^8\text{B}_X^*$  = atomic excitation

Bird et al. (2007)

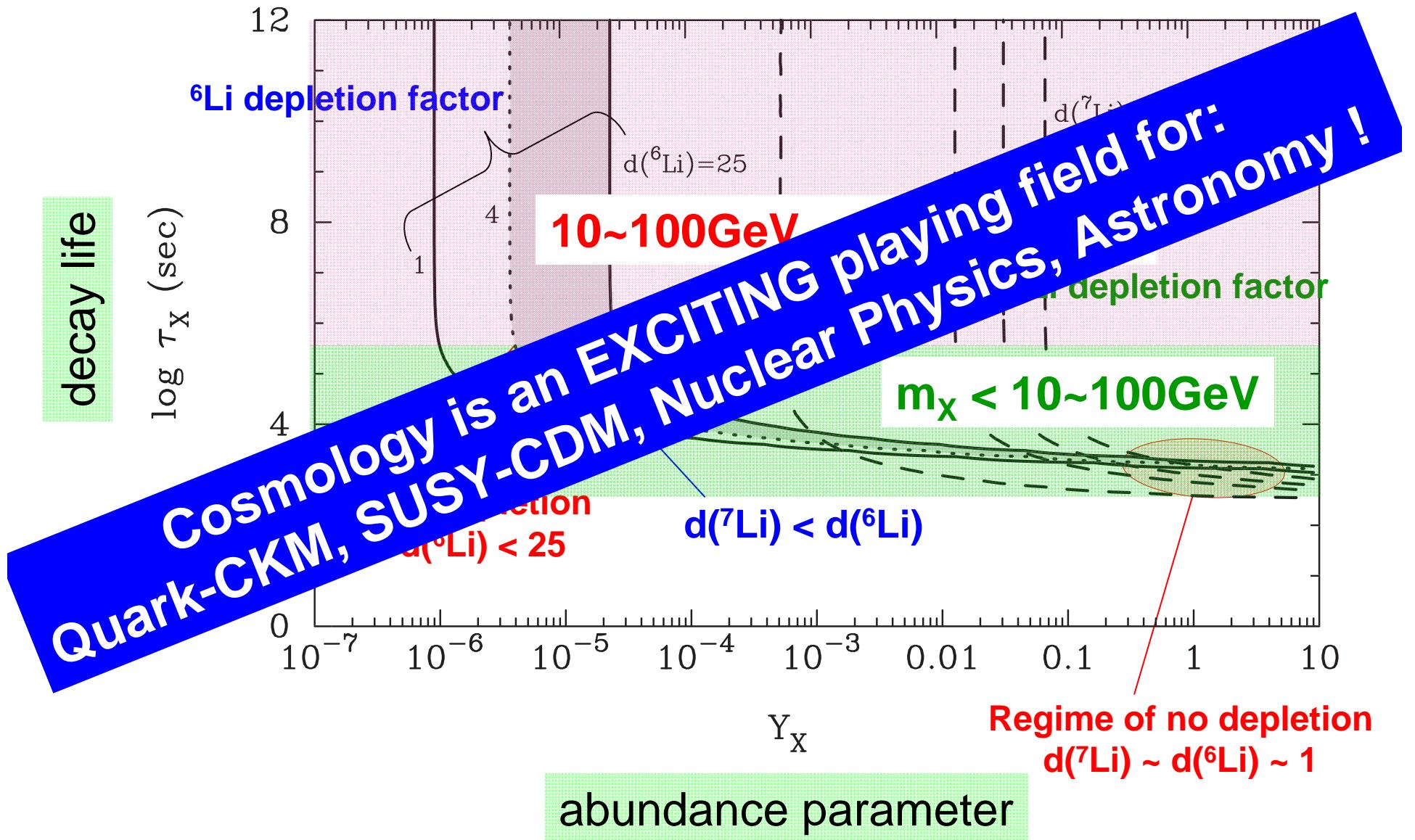


Bird et al. (2007)



# Depletion Factor of ${}^6,7\text{Li}/\text{H}$ ratio (Abundance normalized to MPHSs)

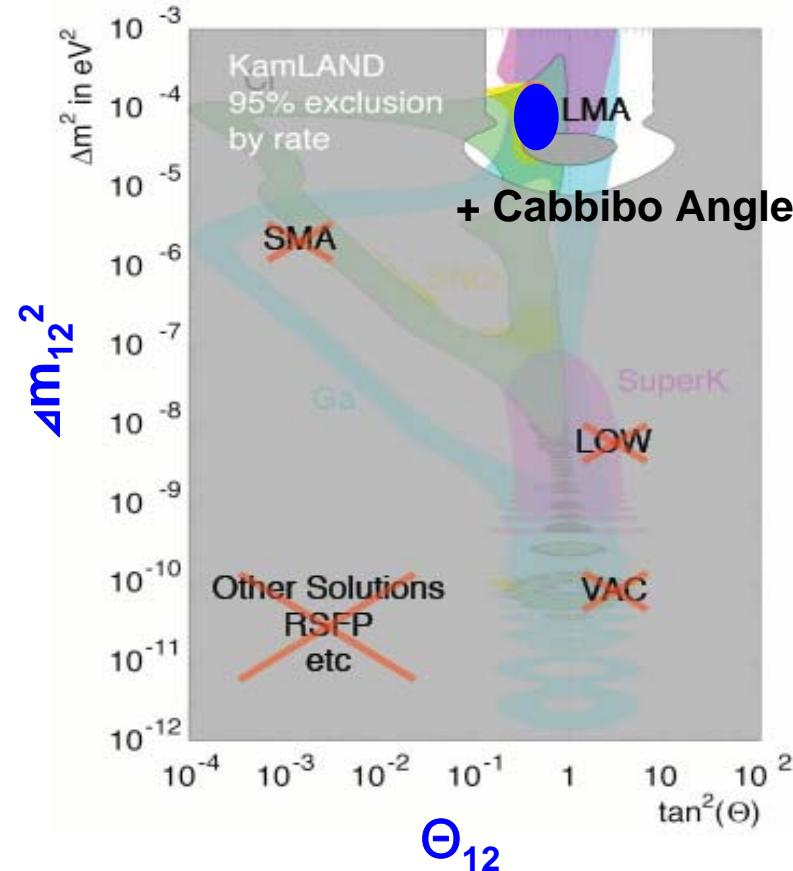
Kusakabe, Kajino, Boyd, Yoshida, and Mathews (2007)



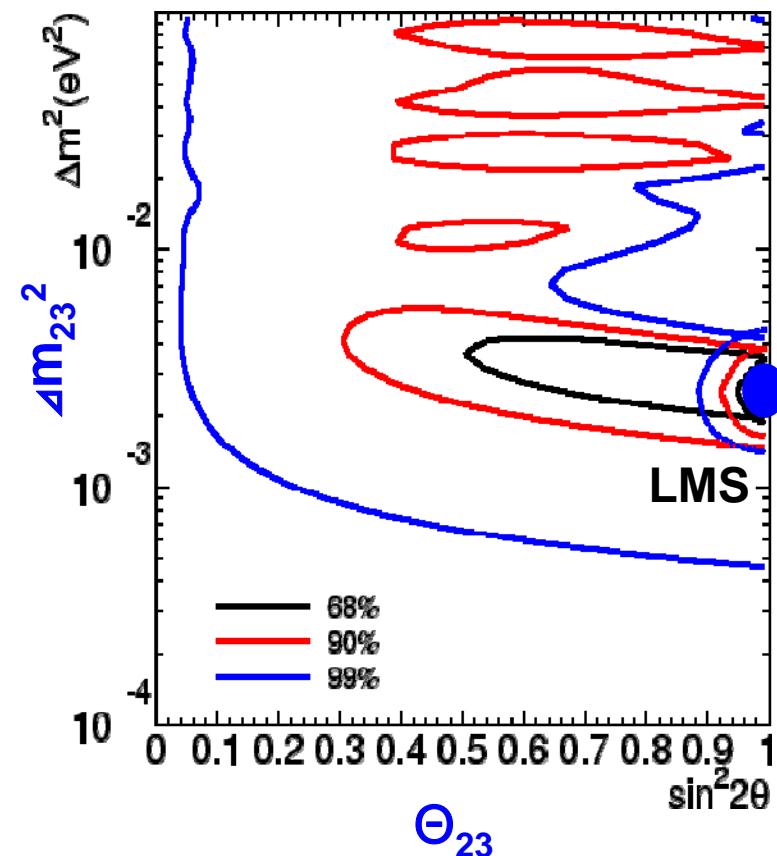
# Neutrino Physics in Supernovae

$\nu$ -oscillation, proposed by Pontecorvo 1957, Sov. Phys. JETP 6, 429 ~ ibid. 1960, 37, 1236,

Super-K, SNO, KamLand (reactor  $\nu$ )  
determined  $\Delta m_{12}^2$  and  $\theta_{12}$  uniquely.



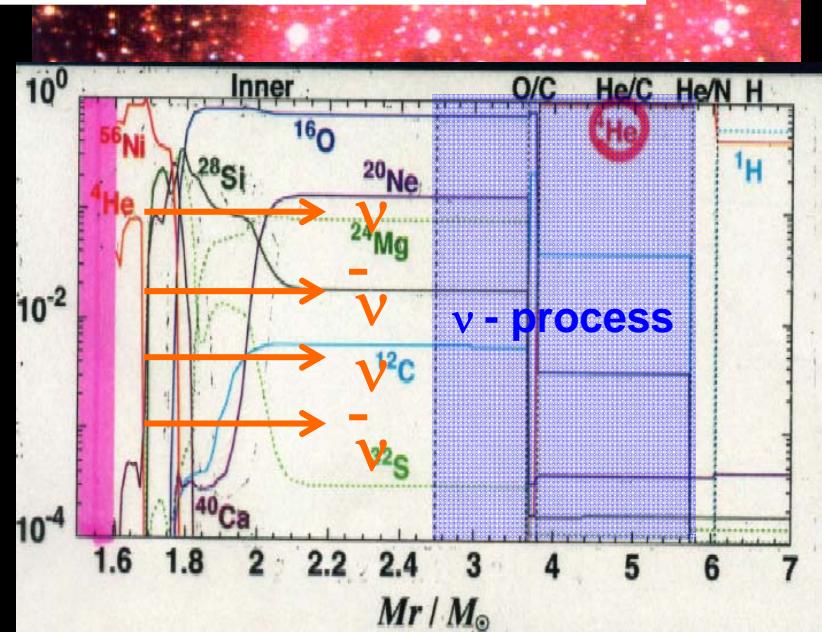
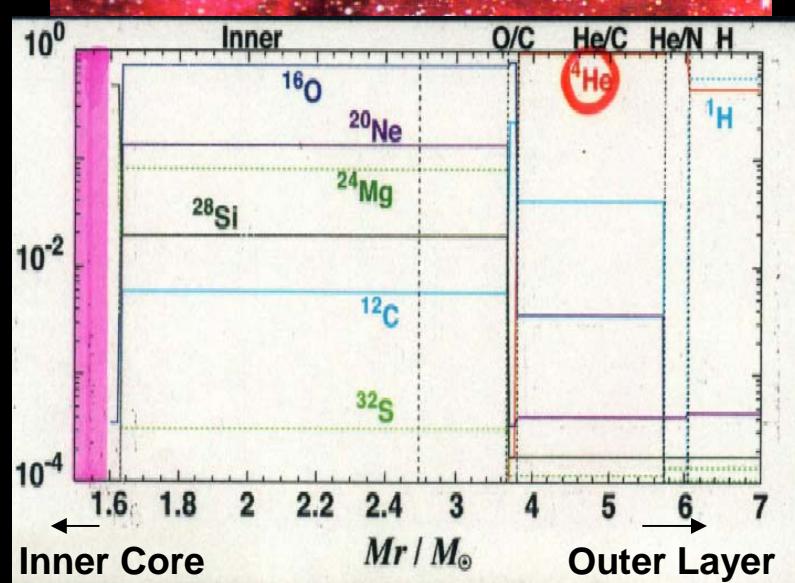
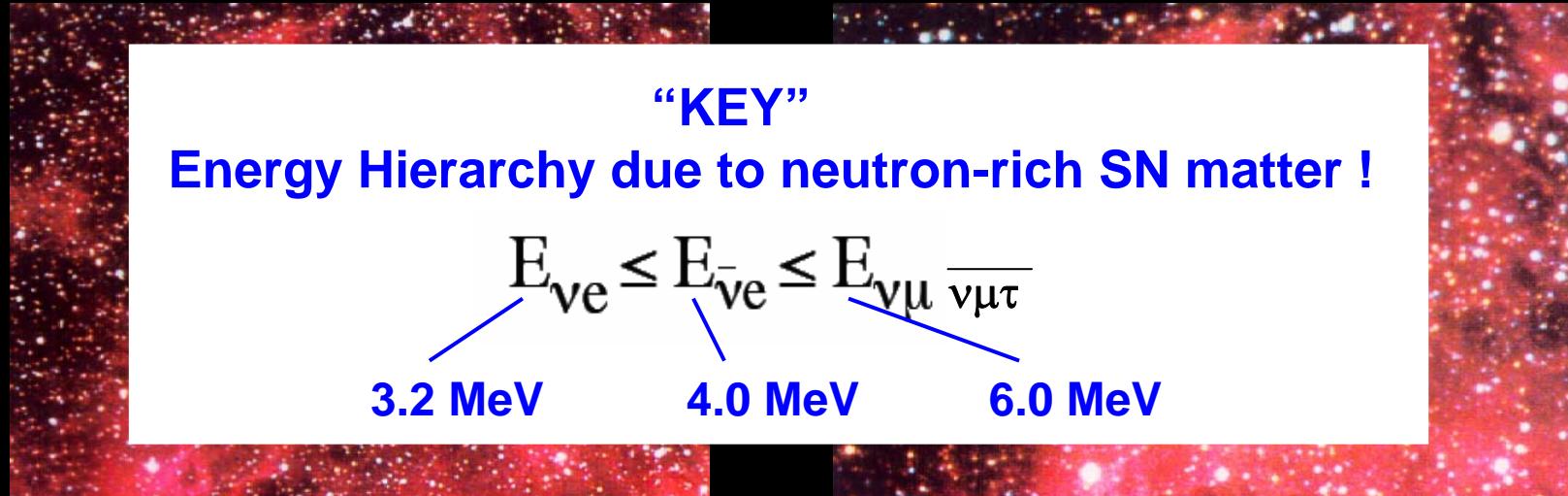
Super Kamiokande (atmospheric  $\nu$ )  
determined  $\Delta m_{23}^2$  and  $\theta_{23}$  uniquely.



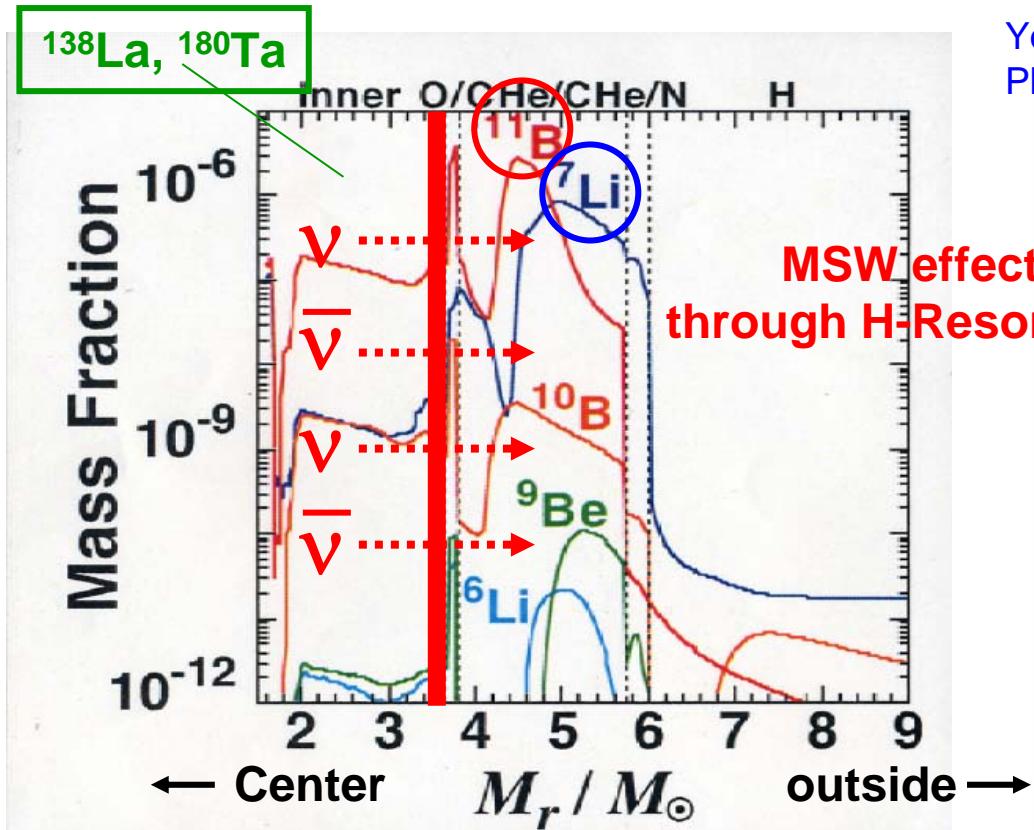
“UNKNOWN” Neutrino-Oscillation Parameters:  
 $\sin^2\theta_{13} < 0.1$ ,  $|\Delta m_{13}^2| = 2.4 \times 10^{-3} \text{ eV}^2$ ,  $\delta_{CP}$  = CP violation phase?

We propose a new method to determine  $\theta_{13}$  and  $\Delta m_{13}^2$  using the MSW-effect on SN  $\nu$ -process nucleosynthesis.

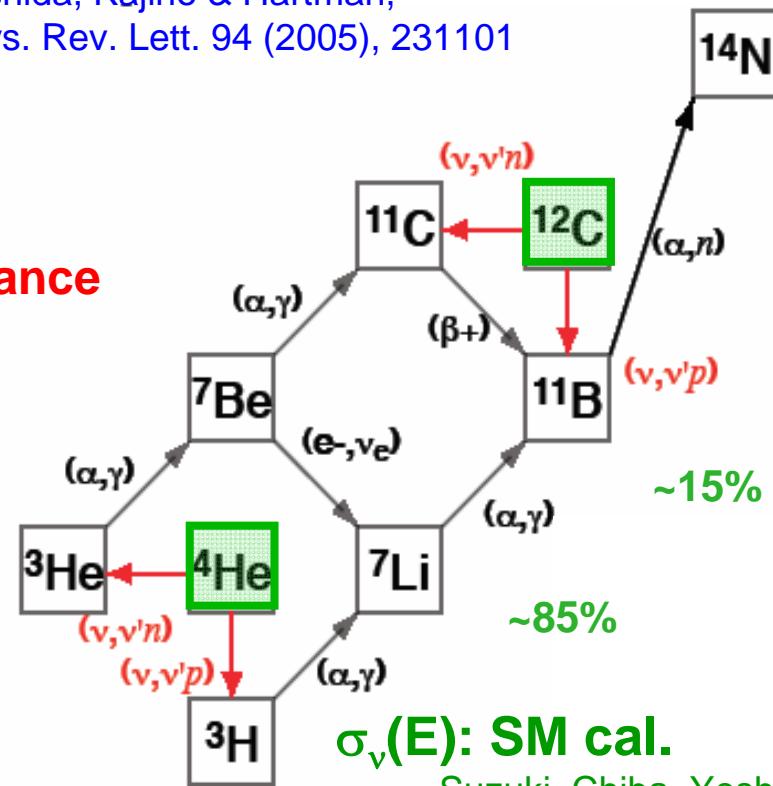
MSW: Wolfenstein 1978, PR D17, 2369; Mikheyev & Smirnov 1986, Sov. J. Nucl. Phys. 42, 913.



# X-process operates in Supernova $\nu$ -Process !



Yoshida, Kajino & Hartman,  
Phys. Rev. Lett. 94 (2005), 231101



Suzuki, Chiba, Yoshida,  
Kajino & Otsuka,  
PR C74 (2006), 034307



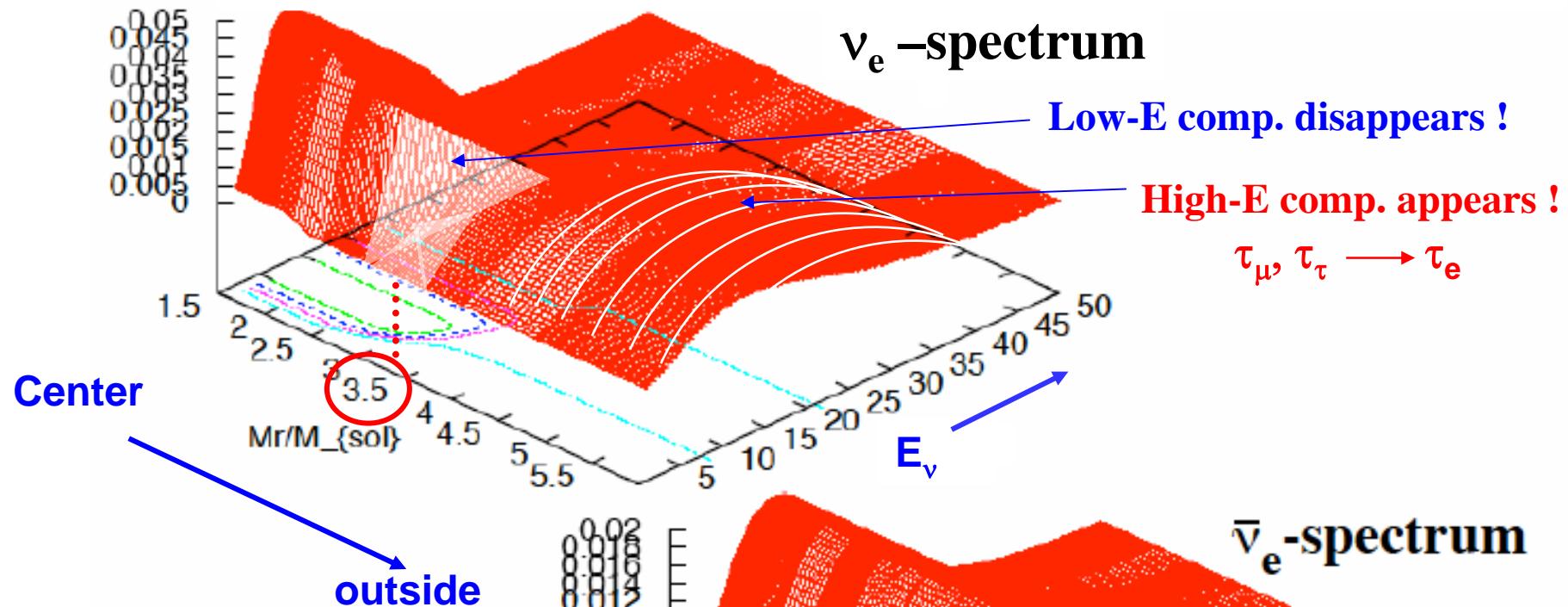
Additional Charged Current Int.

$$\nu_{\mu\tau}(\bar{\nu}_{\mu\tau}) \longrightarrow \nu_e (\bar{\nu}_e)$$

energetic



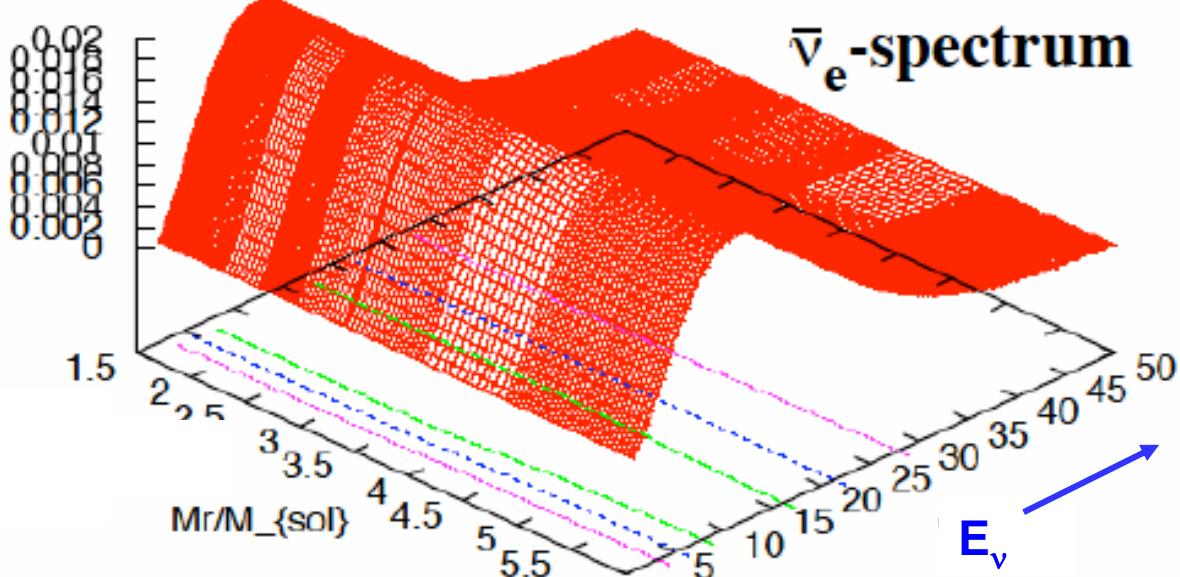
# Neutrino Oscillation (MSW Effect) through propagation

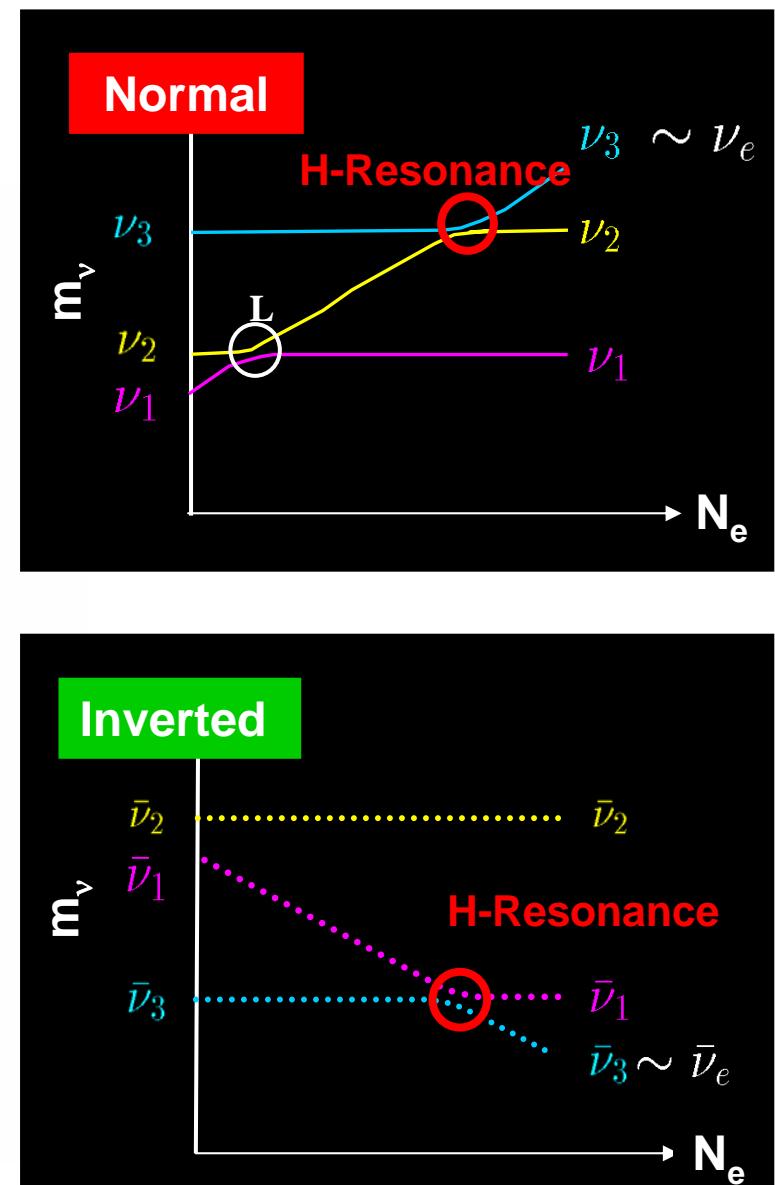
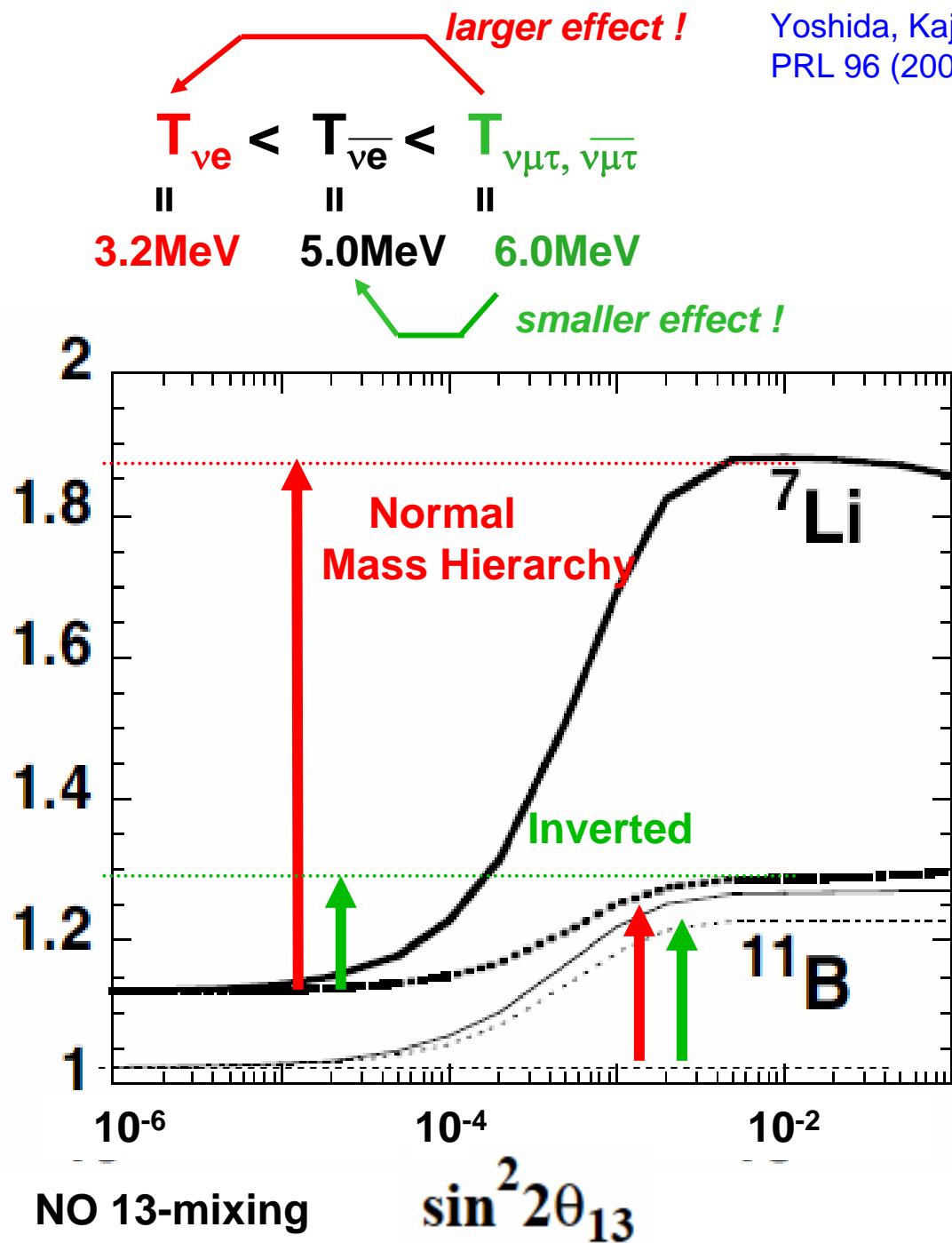


## Parameters:

25M<sub>solar</sub> progenitor SN model  
(Hashimoto & Nomoto 1999)

- $\sin^2 2\theta_{13} = 0.04$
- $\Delta m_{13}^2 = 2.4 \times 10^{-3} \text{ eV}^2$
- $L_\nu = 3 \times 10^{53} \text{ erg}, \tau_\nu = 3 \text{ sec}$
- $T_{\nu e} = 3.2 \text{ MeV}, T_{\bar{\nu} e} = 5.0 \text{ MeV}, T_{\nu \mu \tau} = 6.0 \text{ MeV}$

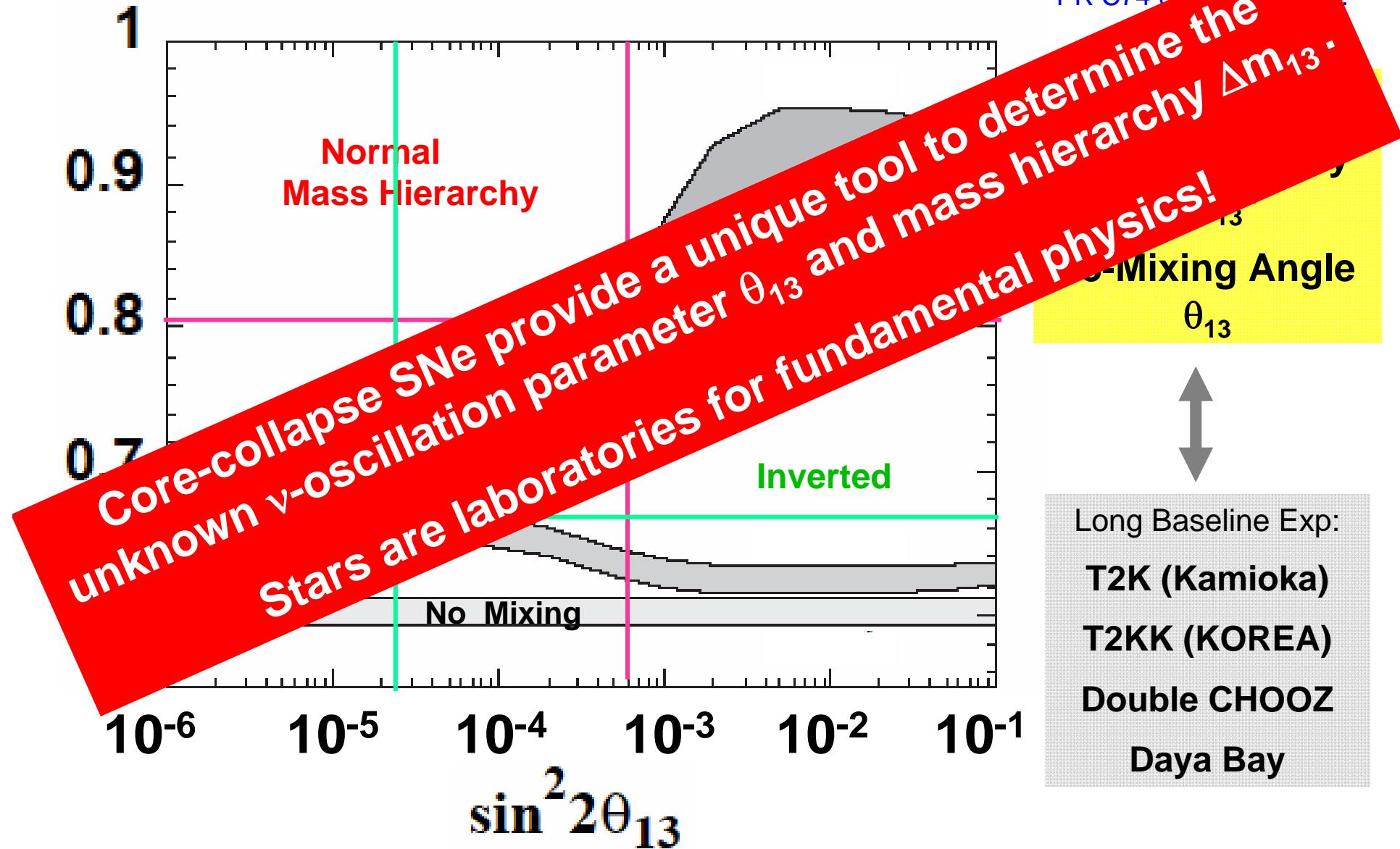




# $^{7}\text{Li}/^{11}\text{B}$ - Ratio

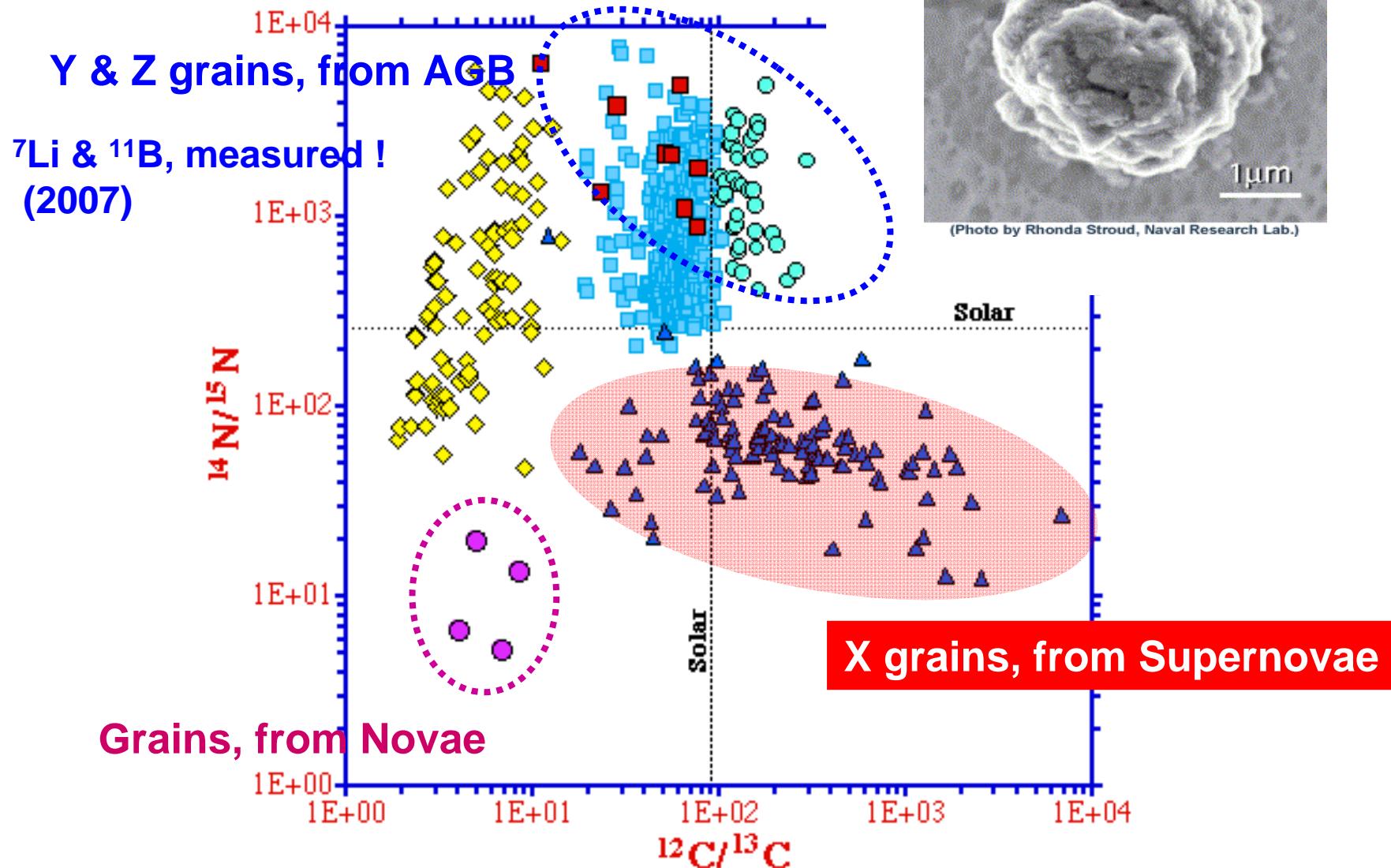
Yoshida, Kajino, Yokomakura, Kimura, Takamura & Hartmann,  
PRL 96 (2006) 09110; ApJ 649 (2006), 349.

Suzuki, Chiba, Yoshida, Kajino & Otsuka,  
PR C74 (2006) 025502



# How to observe the $^7\text{Li}/^{11}\text{B}$ ratio ?

## (1) Presolar SiC Grain



## (2) SPECTROSCOPIC OBSERVATION

$^{11}\text{B}$  absorption line  $\sim 2497 \text{ \AA}$  (Space Telescope like HST)

$^{11}\text{B}/^{10}\text{B}$ , observed in MPH Stars!

Rebull et al. ApJ 507 (1998) 387; Proc. (2000)

$^7\text{Li}$  absorption line  $\sim 6708 \text{ \AA}$  (Ground Base Telescope like SUBARU)

$^7\text{Li}$  &  $^7\text{Li}/^6\text{Li}$ , observed in MPH Stars, but BBN-comp. dominates!

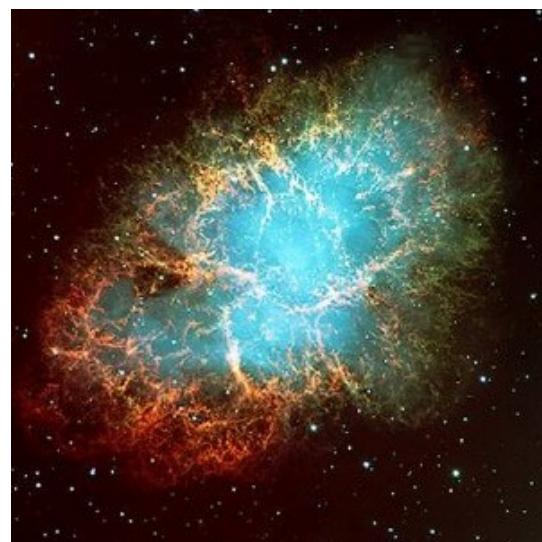
LMXB for both  $^7\text{Li}$  &  $^{11}\text{B}$  !

Many observations (1982 – present)

SN1987A Remnant



Crab Nebula



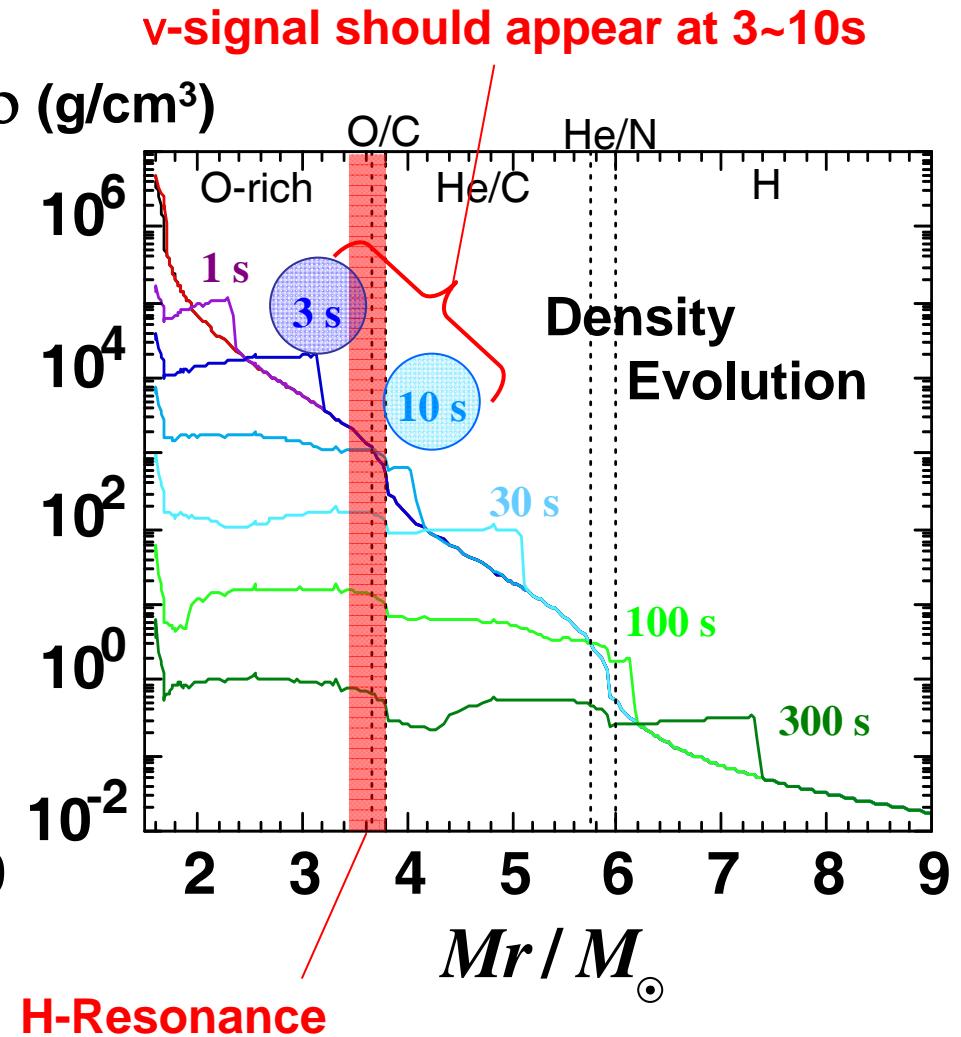
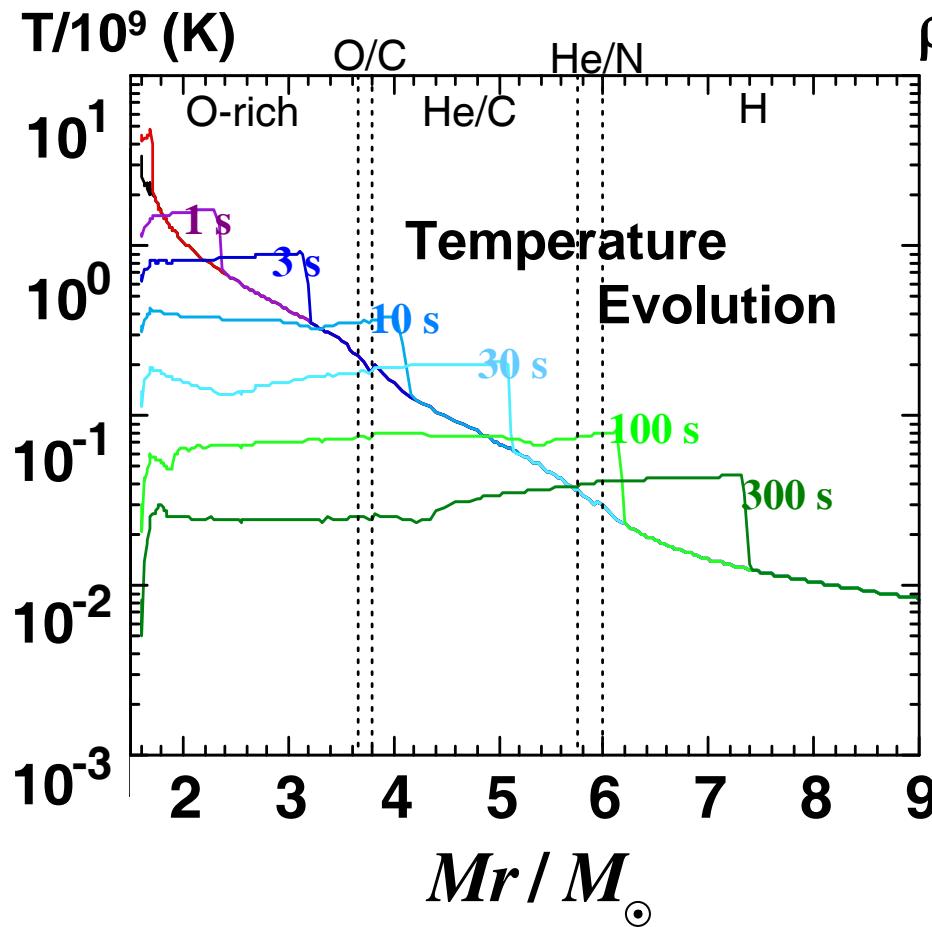
R-element enhanced  
Metal-Poor Halo Stars



# Neutrino Signal in $16.2 M_{\odot}$ - SN Model

## Shock Propagation Effect

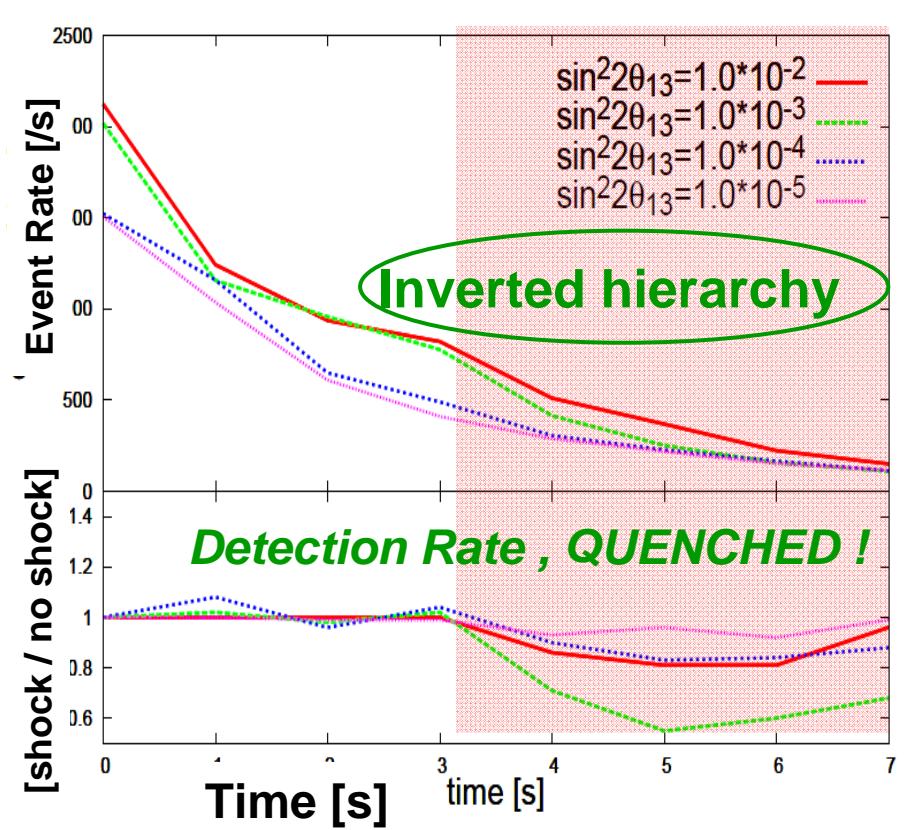
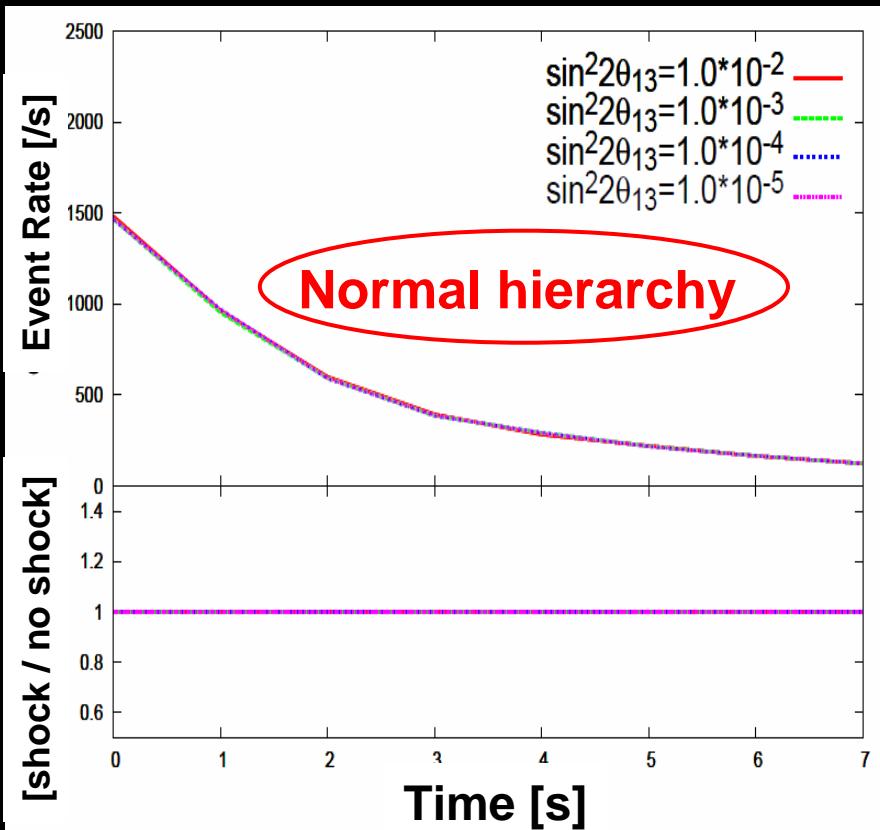
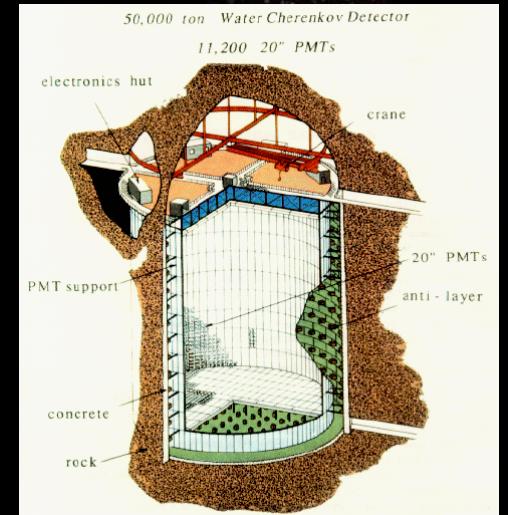
Kawagoe, Kajino, Sumiyoshi, Suzuki, & Yamada (2007)



# Event Rate in Super-Kamiokande

Kawagoe, Kajino, Sumyoshi, Suzuki & Yamada (2007)

★ target : pure water (32,000 t)  
★  $\bar{V}_e + p \rightarrow n + e^+$



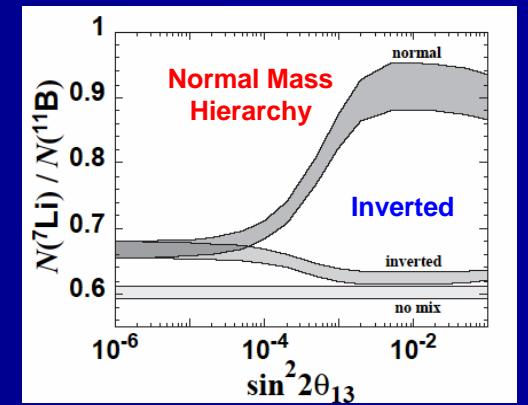
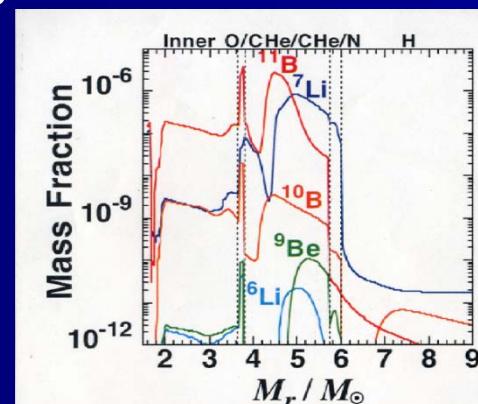
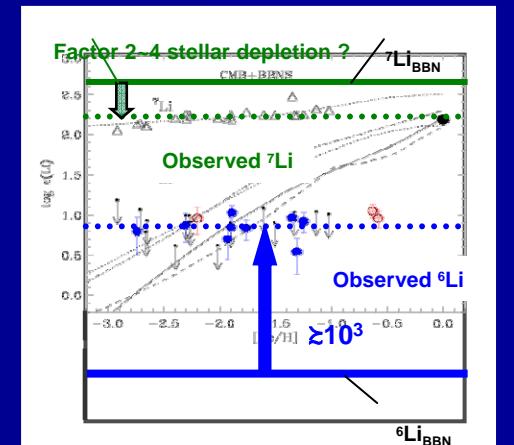
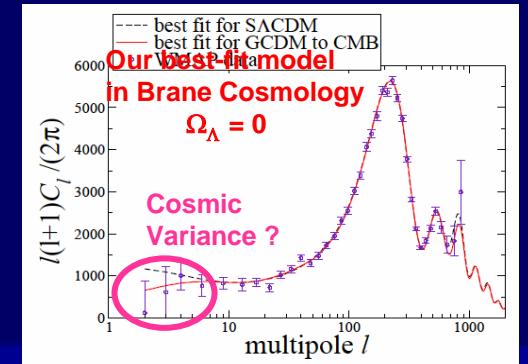
# Summary

1 .Big-Bang Nucleosynthesis provides “critical test” for particle & nuclear theories and observational cosmology.

1a: Brane World Cosmology with mass-energy exchange between brane and bulk can describe accelerating cosmic expansion with  $\Omega_\Lambda = 0$  !

1b: Relic X- particle model (progenitor of CDM), if they are bound in normal nuclei or radiative decay to non-thermal photons, can solve both  ${}^6\text{Li}$  and  ${}^7\text{Li}$  problems.

2 The core-collapse SN  $\nu$ -process provides a unique tool to determine the unknown  $\nu$ -oscillation parameter  $\theta_{13}$  and mass hierarchy  $\Delta m_{13}$  of active  $\nu$ 's in terms of  $\nu$ -matter effect (MSW) in nucleosynthesis.





# Theoretical Uncertainties ?

## (1) Neutrino Energy Spectrum, well known?

Fermi-Dirac distr. of  $T_\nu$

How to determine  $T_\nu$  ? ← from “SN1987A obs.” & “GCE”

Yoshida, T., Kajino, T., & Hartmann, D. H., PRL 94 (2005), 231101

## (2) Neutrino-Nucleus Cross Section $\sigma_\nu(E)$ , well known?

Previous SM cal. by W. Haxton (1990)

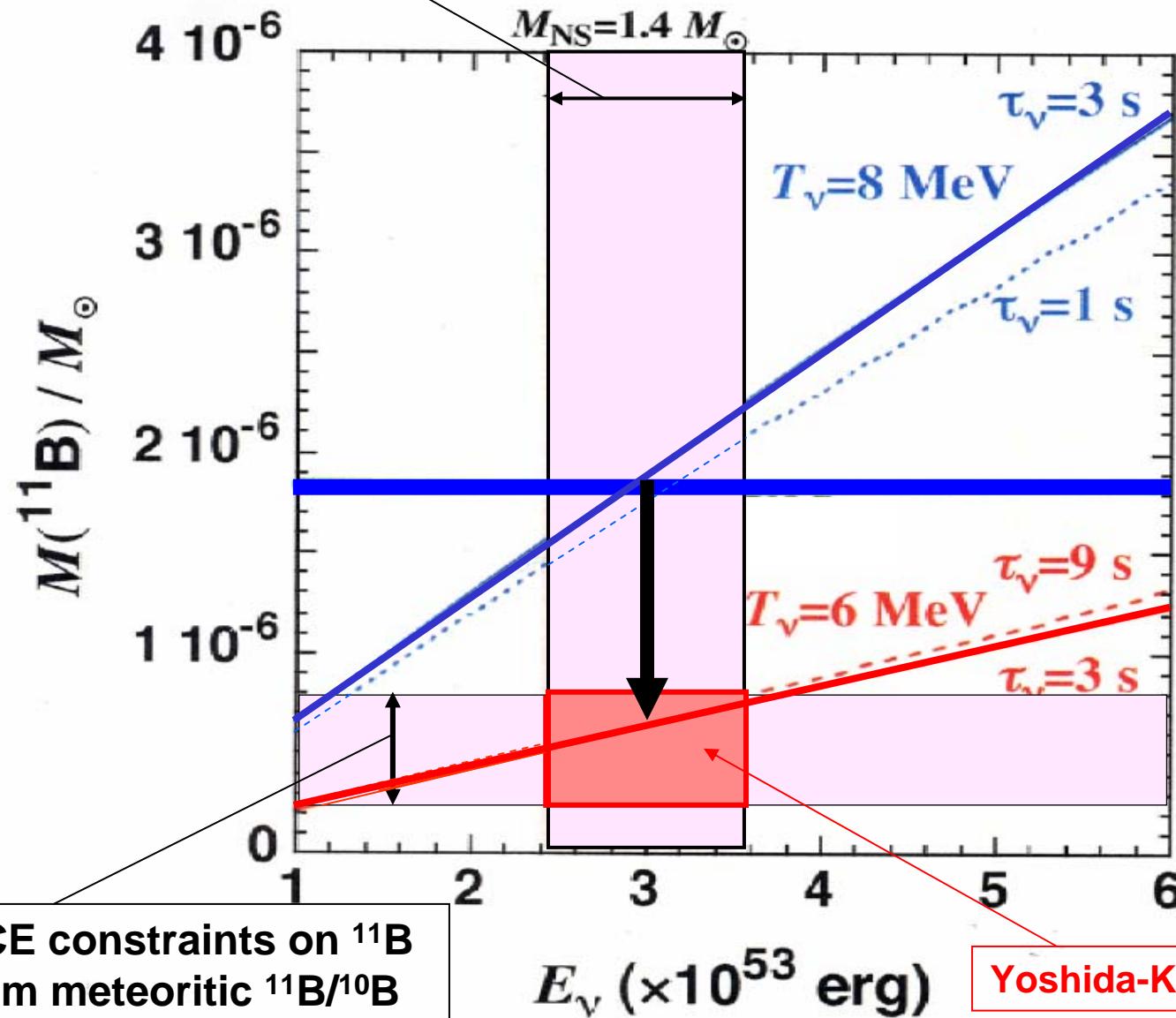
Precise SM cal. using better interactions, done (2006) !

Suzuki, Chiba, Yoshida, Kajino & Otsuka, PR C74 (2006), 034307.

# How to know SN $\nu_{\mu\tau}$ -Spectrum ?

Grav. Potential constraint

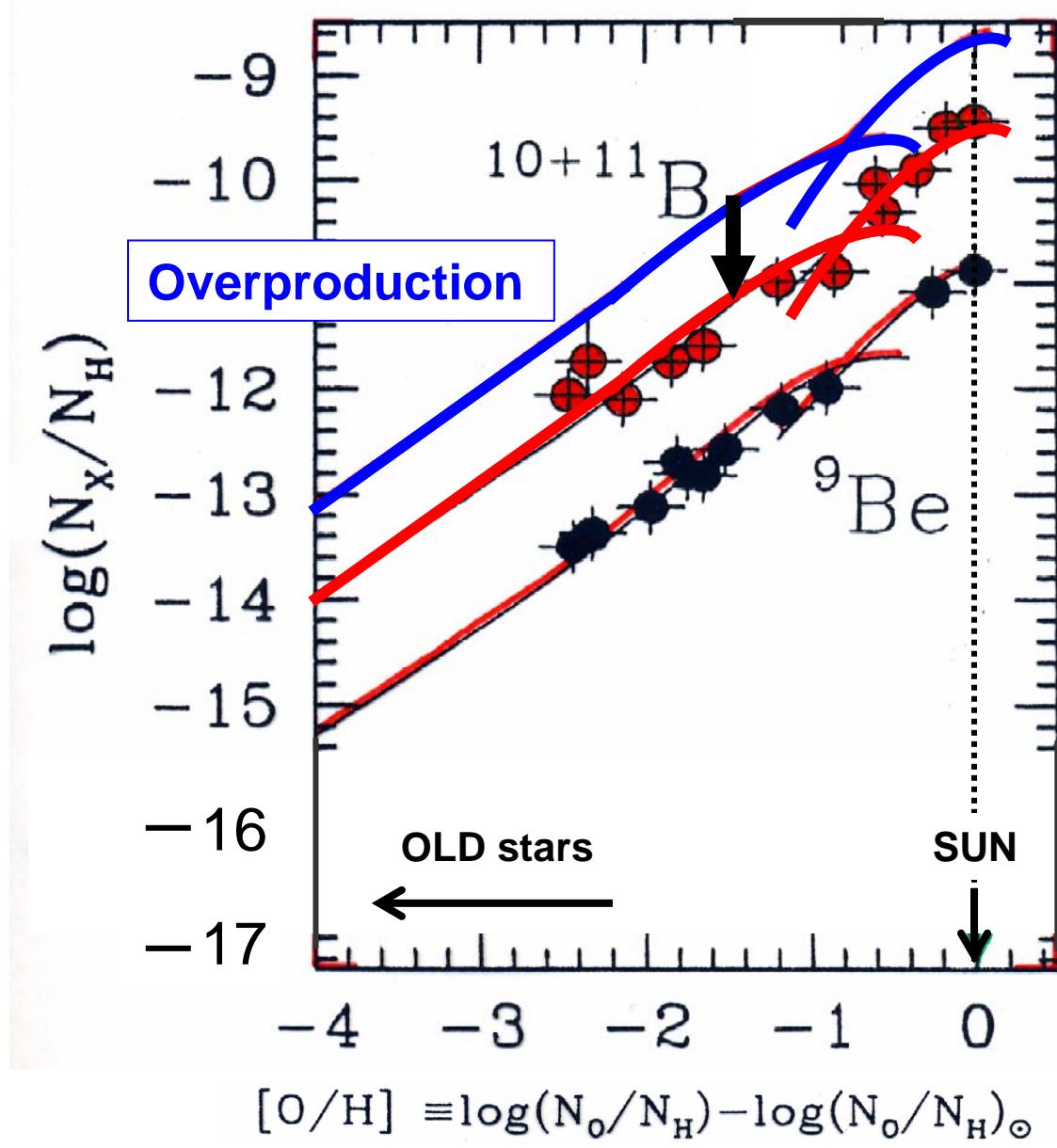
Yoshida, T., Kajino, T., and Hartmann, D., PRL 94 (2005), 231101.



Woosley & Weaver  
ApJS 101 (1995), 181.  
**OVERPRODUCTION**

Consistent with  
Thomas-Janka et al.  
2004 (MPA)

# Galactic Chemical Evolution of ${}^9\text{Be}$ & ${}^{10,11}\text{B}$



Livermore Model  
Woosley and Weaver  
ApJS 101 (1995) 181.  
 $T_{\nu_{\mu,\tau}} = 8 \text{ MeV}$

$T_{\nu_{\mu,\tau}} = 6 \text{ MeV}$

Yoshida, Kajino & Hartmann,  
PRL 94 (2005), 231101.

•  ${}^{11}\text{B}$  has two origins:

Supernova  $\nu$ -process  
Galactic Cosmic Rays

(GCR)

- ${}^9\text{Be}$  has pure GCR.
- ${}^{11}\text{B} \gg {}^{10}\text{B}$

# Theoretical Uncertainty?

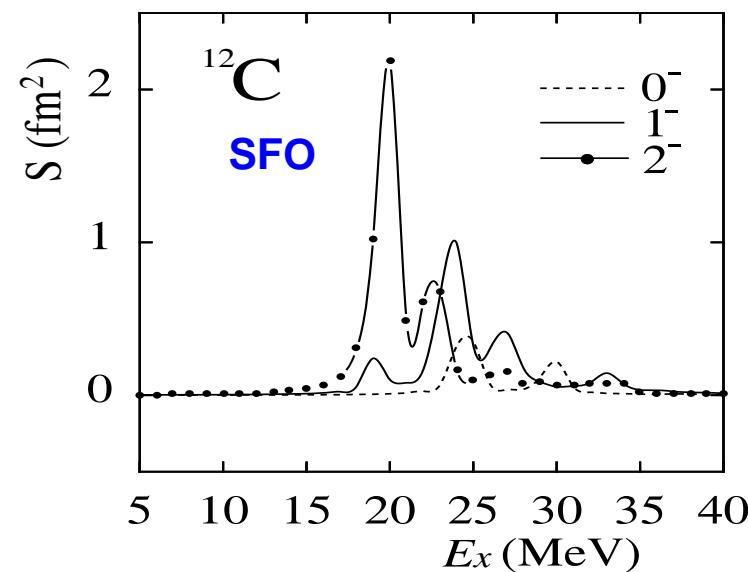
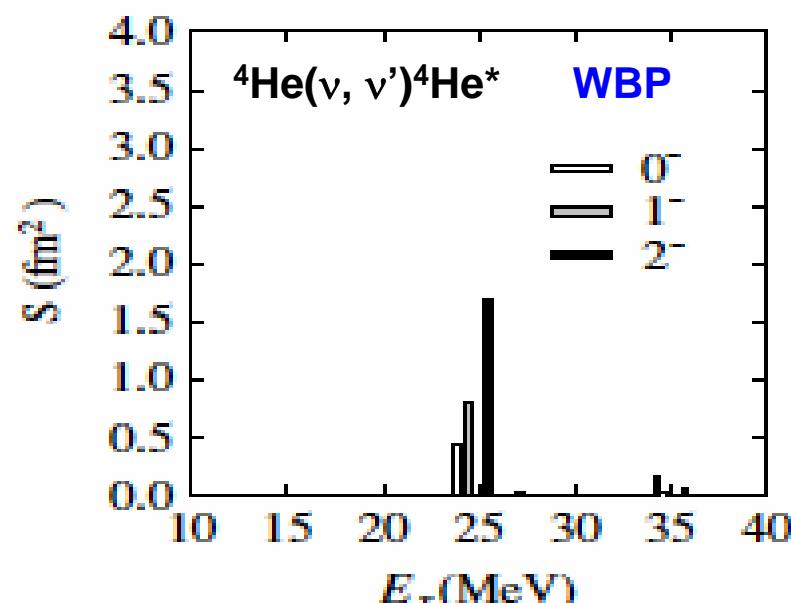
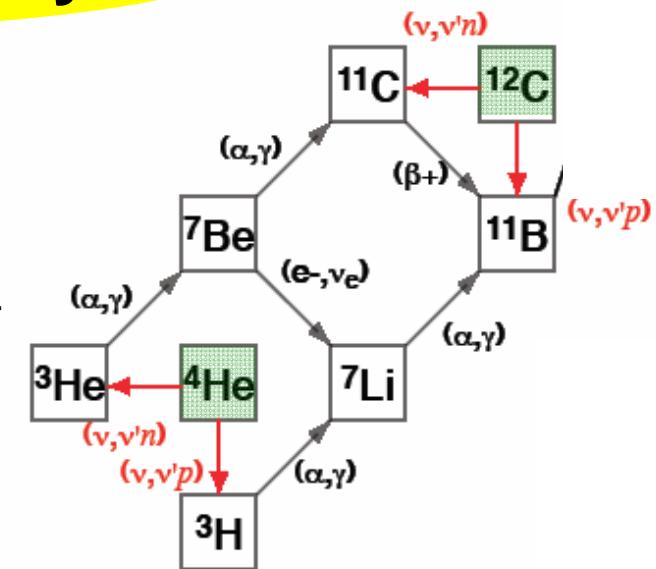
Haxton's SM cal. (Woosley et al. ApJ. 356 (1990), 272)

Suzuki's new SM cal. With new Hamiltonian

Suzuki, Chiba, Yoshida, Kajino & Otsuka, PR C74 (2006), 034307

$^4\text{He}$ : **WBP (Warburton-Brown) Hamiltonian** = Similar to microscopic ab initio cal. of Gazit et al. PRC70 (2004) 048801

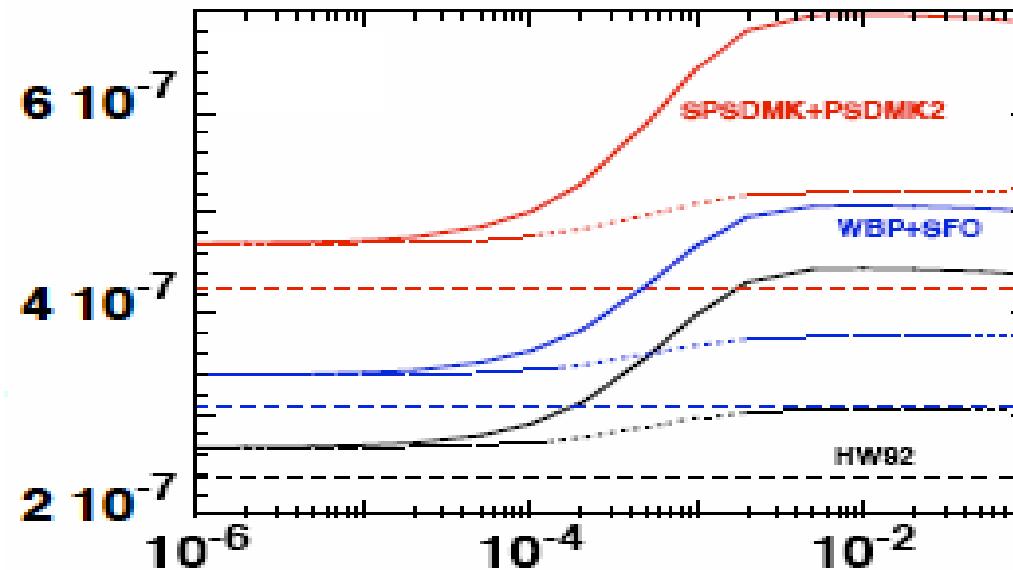
$^{12}\text{C}$ : **SFO Hamiltonian** = Spin-isospin flip int. with enhanced op<sub>1/2</sub>-op<sub>3/2</sub> separation from Cohen-Kurath  
 -  $\mu$ -moments of p-shell nuclei  
 - GT strength for  $^{12}\text{C} \rightarrow ^{12}\text{N}$ ,  $^{14}\text{C} \rightarrow ^{14}\text{N}$ , etc.  
 - proper tensor int.



# Neutrino Oscillation Matter (MSW) Effect

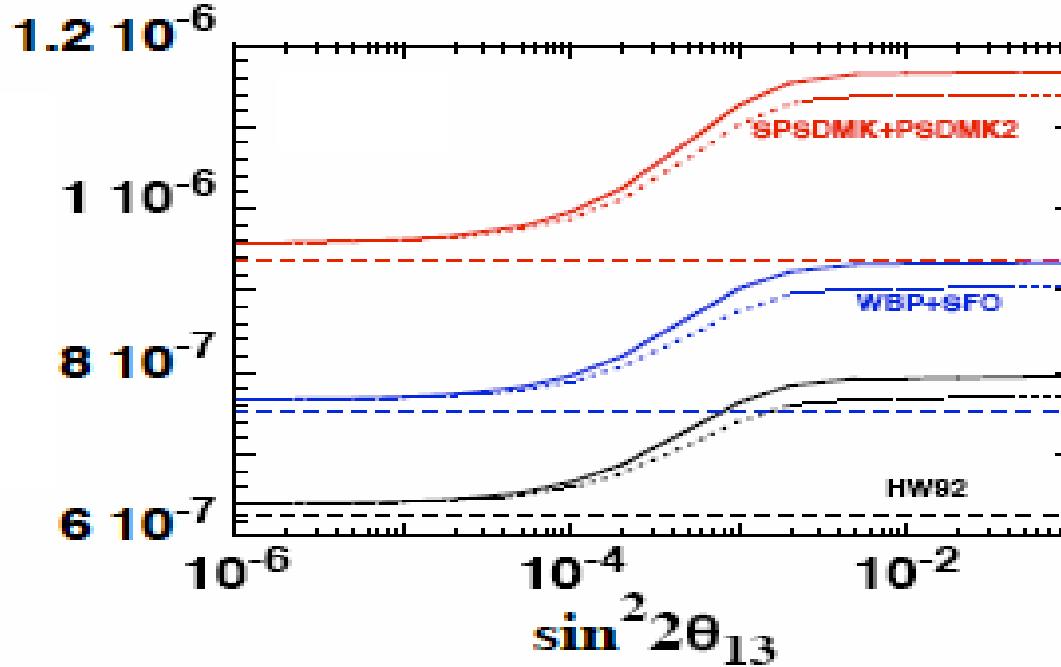
${}^7\text{Li}$

Ejected Mass



${}^{11}\text{B}$

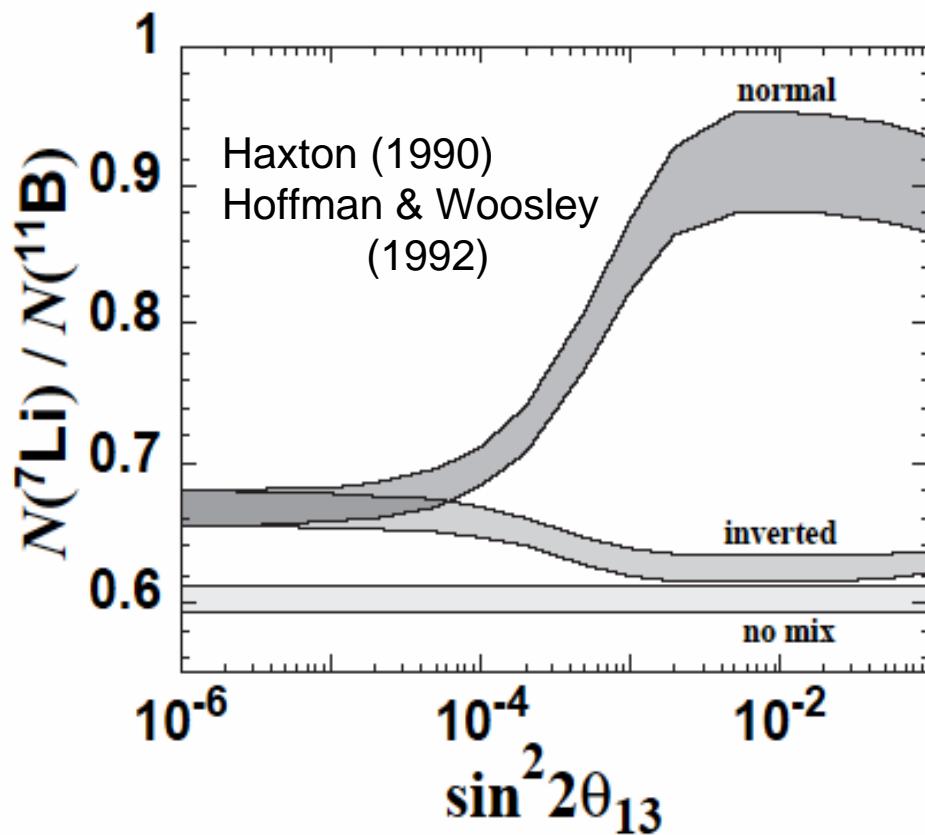
Ejected Mass



# Neutrino Oscillation Effect on ${}^7\text{Li}/{}^{11}\text{B}$ -ratio

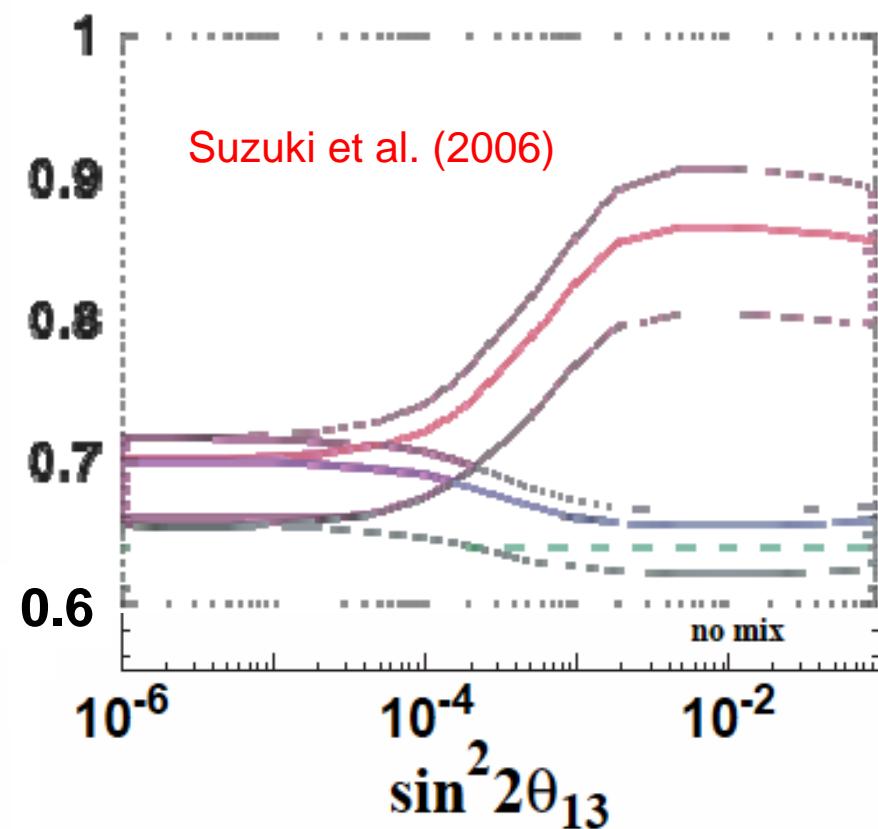
## Previous SM- $\sigma_\nu(E)$ of Haxton

Woosley, Haxton, Hoffmann, Wilson, ApJ. (1990).  
Hoffmann & Woosley, ApJ. (1992).



## New SM- $\sigma_\nu(E)$ using WBP( ${}^4\text{He}$ ) & SFO( ${}^{12}\text{C}$ ) interactions

Suzuki, Chiba, Yoshida, Kajino & Otsuka,  
Phys. Review C74 (2006), 034307.

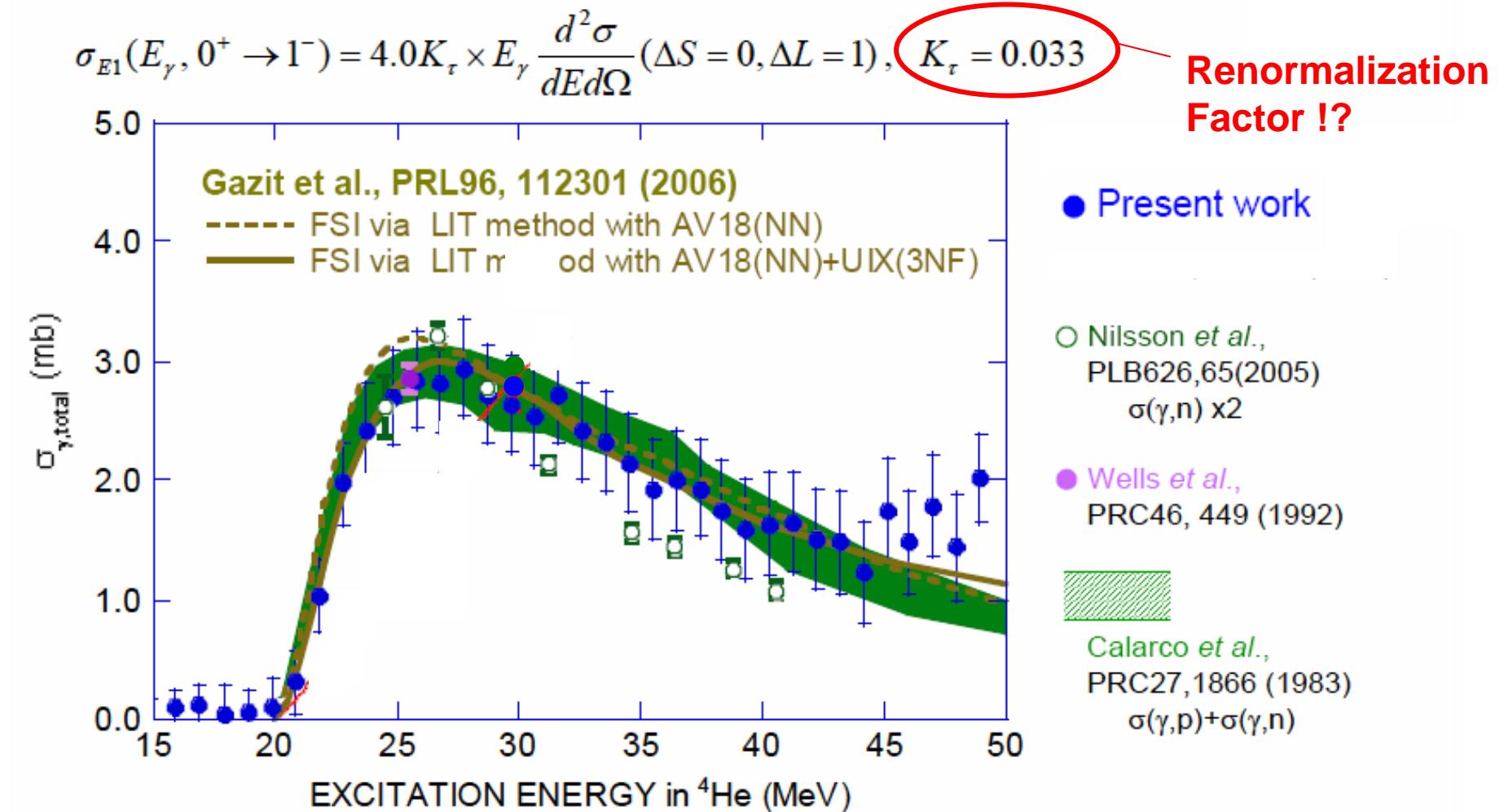
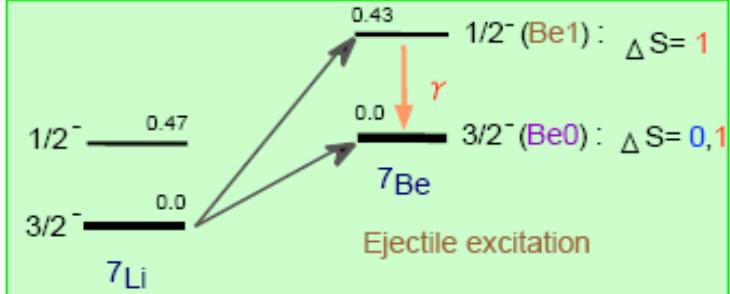


Almost the same result !  $\rightarrow {}^7\text{Li}/{}^{11}\text{B}$ -ratio is SM independent !

From S. Nakayama (Tokushima University)

## Charge Exchange ( ${}^7\text{Li}, {}^7\text{Be}$ ) Reactions $\Delta S=0$ spectrum & $\sigma_\gamma$ for ${}^4\text{He}(\gamma, n)$

${}^7\text{Li} \rightarrow {}^7\text{Be}$  transition and spin-selectivities



# **Similarity between Electro-Magnetic & Weak Interactions**

---

$$\text{EM-current} = \vec{V}, \quad \text{Weak-current} = \vec{V} - \vec{A}$$

$$\begin{aligned}\vec{V} &\approx g_V^{IV} \frac{i}{2m} \vec{\sigma} \times \vec{q} + \frac{g_V}{2m} (\vec{p} + \vec{p}') \\ \vec{A} &\approx g_A \vec{\sigma}\end{aligned}$$

**Weak operator in non-relativistic limit**

$$\text{Gamow-Tellar operator} = \vec{\sigma} \tau_{\pm}$$

$$\text{Spin-Dipole operator} = [\vec{\sigma} \times \vec{r}]^J \tau_{\pm}$$

**We still don't have the  $\nu$ -beam !**

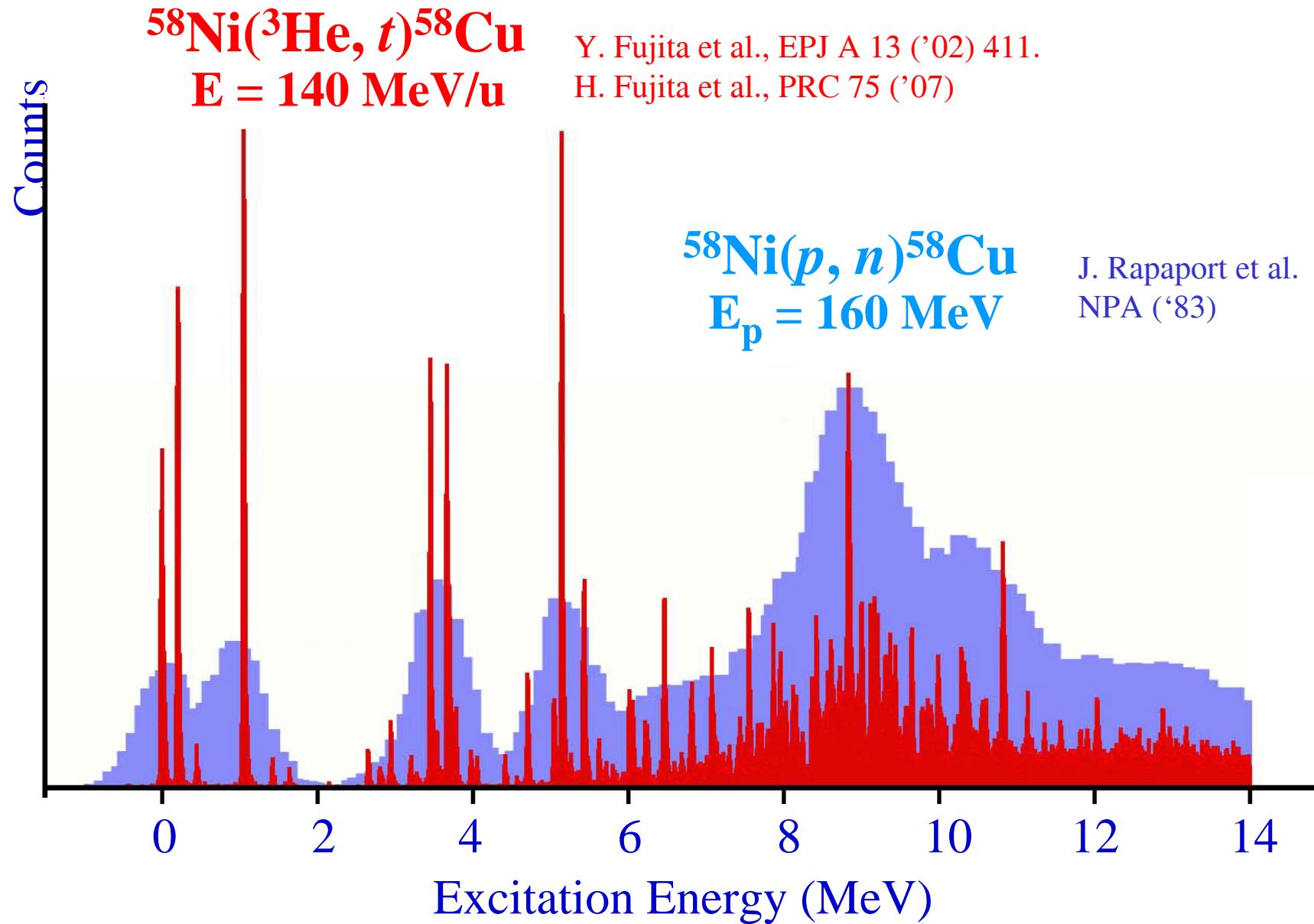
**However, we can use Electro-Magnetic PROBE:**

${}^4\text{He}(\gamma_{NT}, n) {}^3\text{He}$  and  ${}^4\text{He}(\gamma_{NT}, p) {}^3\text{H}$

→  ${}^4\text{He}(\nu, \nu'), {}^4\text{He}(\nu_e, e^-), {}^4\text{He}(\bar{\nu}_e, e^+)$

# Charge Exchange Reactions → B(GT)

Y. Fujita  
足立竜也

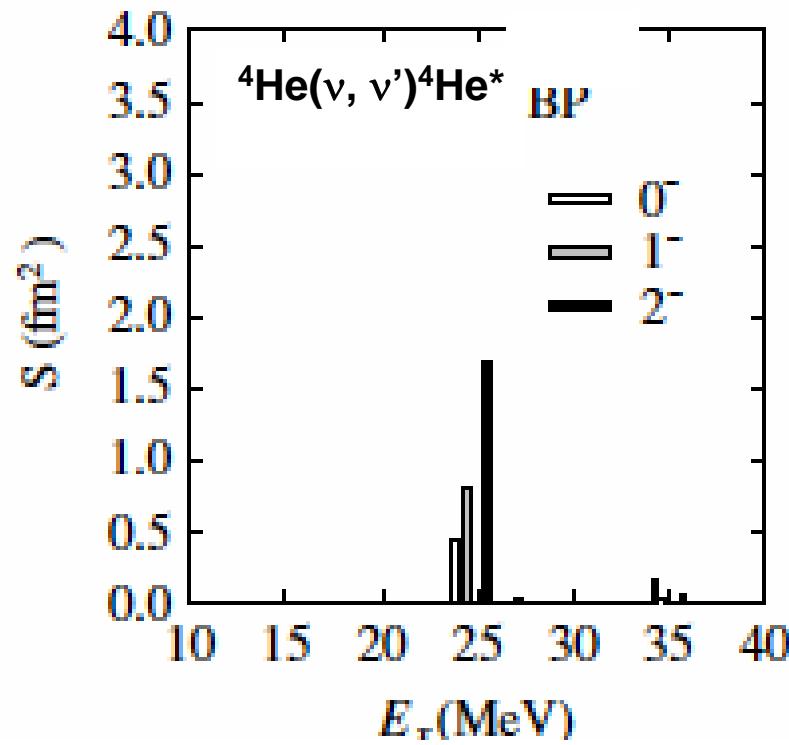


# Photo-induced Reaction

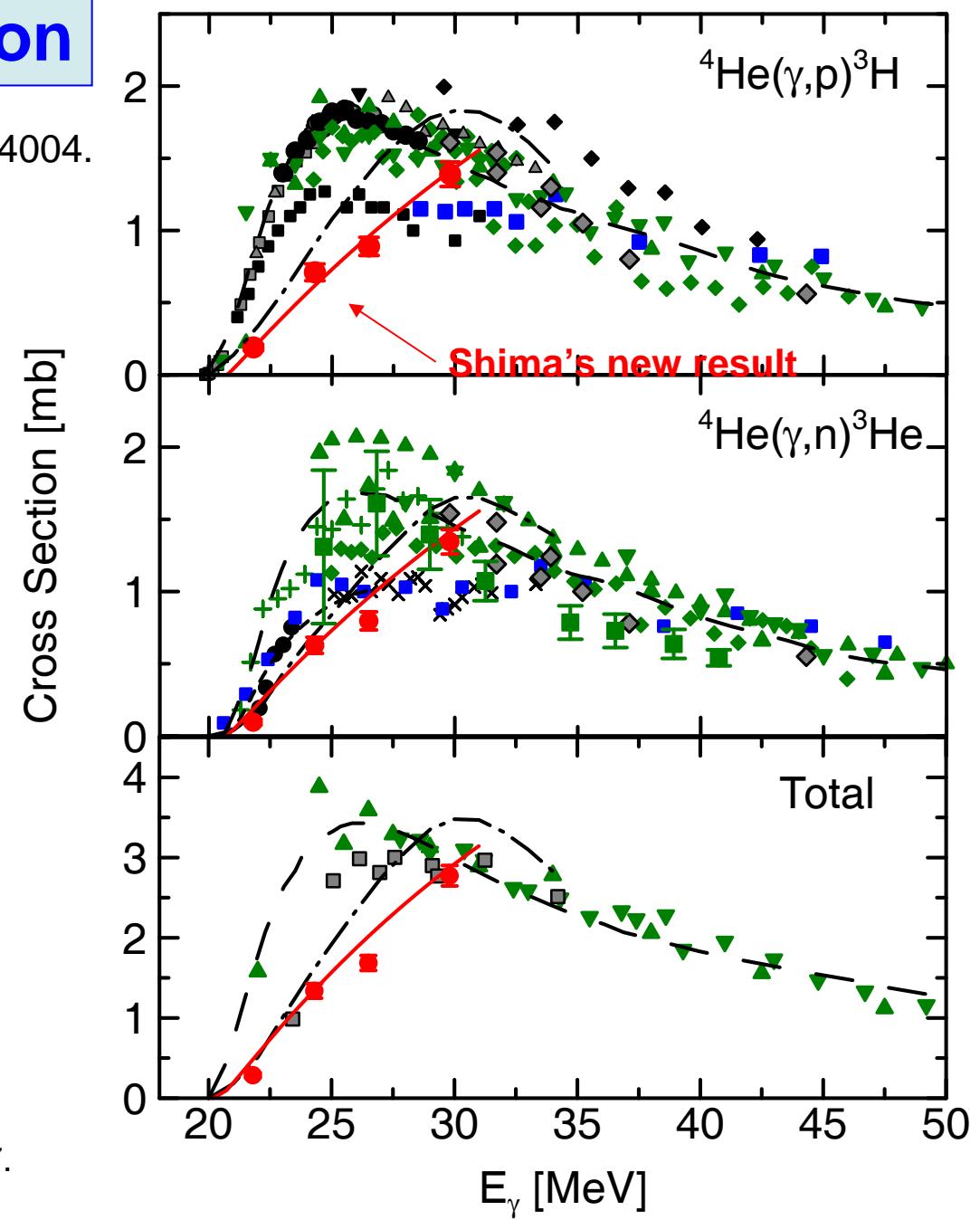
Shima et al. Phys. Rev. C72 (2005) 044004.

Experiment using real- $\gamma$  !

→ Absolute Yields !



Suzuki et al. Phys. Rev. C74 (2006) 034307.



# Core-Collapse, $\nu$ -Heating, Nucleosynthesis

Energy Hierarchy  
due to neutron-rich matter !

$$E_{\nu e} \leq E_{\bar{\nu} e} \leq E_{\nu \mu, \bar{\nu} \mu}$$

