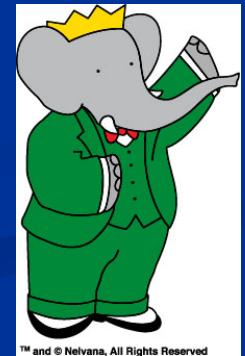


Recent results on Leptonic and Radiative B decays at BaBar

[$B \rightarrow \tau \nu$, $b \rightarrow (s,d)\gamma$]



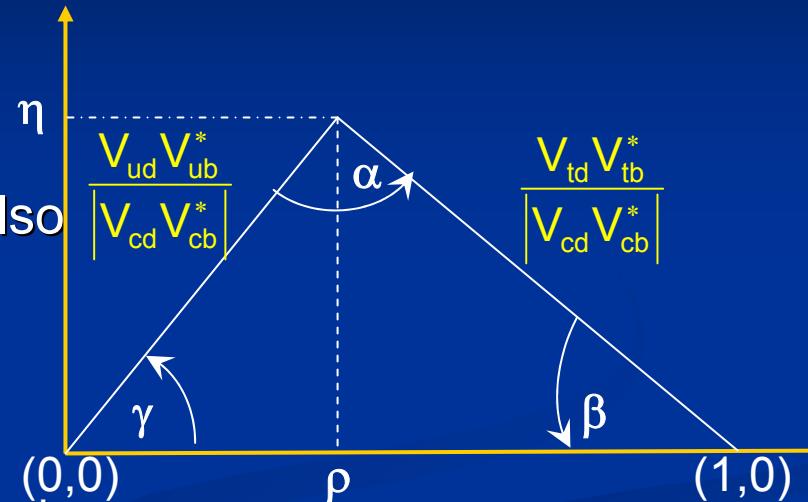
Tülay Çuhadar-Dönszelmann
University of British Columbia
On Behalf of the BaBar Collaboration



XIIIth Lomonosov Conference on Elementary Particle Physics
August 23-29, 2007
Moscow State University, Moscow, Russia

Rare Decays: Physics Motivation

- The constrain on Unitarity Triangle due to tree level or $\Delta F=2$ processes
- Processes other than tree level can also be used for constraining the UT
- Flavour-Changing neutral current (FCNC) [$b \rightarrow (s,d)\gamma$, $b \rightarrow s\bar{l}l$, etc]
 - Forbidden at tree level, proceed at one loop
 - Suppressed (rare decays) due to the CKM matrix elements
 - Good place to search for non-SM
 - New particles in the loop can enhance the observables (Branching Fraction, Asymmetries, etc) predicted by the SM
- Pure leptonic decays suppressed (CKM parameters - $|V_{ub}|$ and helicity - lepton mass squared)



Leptonic Decays: $B^+ \rightarrow \tau^+ \nu$

- Helicity suppressed pure leptonic B decay

■ Measure $|V_{ub}|, f_B$

- $\tau : \mu : e = 1 : 5 \times 10^{-3} : 1 \times 10^{-7}$

- SM prediction :

$$Br(B^+ \rightarrow \tau^+ \nu) = (1.6 \pm 0.4) \times 10^{-4}$$

$$f_B = 0.216 \pm 0.022 \text{ GeV}, |V_{ub}| = (4.31 \pm 0.30) \times 10^{-3}$$

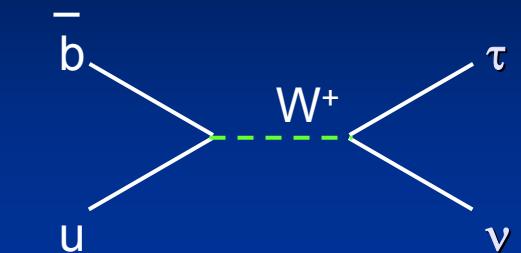
- First evidence by Belle (PRL 97, 251802 (2006))

$$Br(B^+ \rightarrow \tau^+ \nu) = (1.79^{+0.56}_{-0.49}(stat)^{+0.46}_{-0.51}(sys)) \times 10^{-4} \quad (3.5\sigma, 414 \text{ fb}^{-1})$$

- Possibility to constrain physics beyond SM

■ 2HDM model can enhance Branching fraction

$$Br(B \rightarrow \tau \nu) = Br(B \rightarrow \tau \nu)_{SM} \times \left(1 - \tan^2 \beta \frac{m_{B^\pm}^2}{m_{H^\pm}^2} \right)^2$$

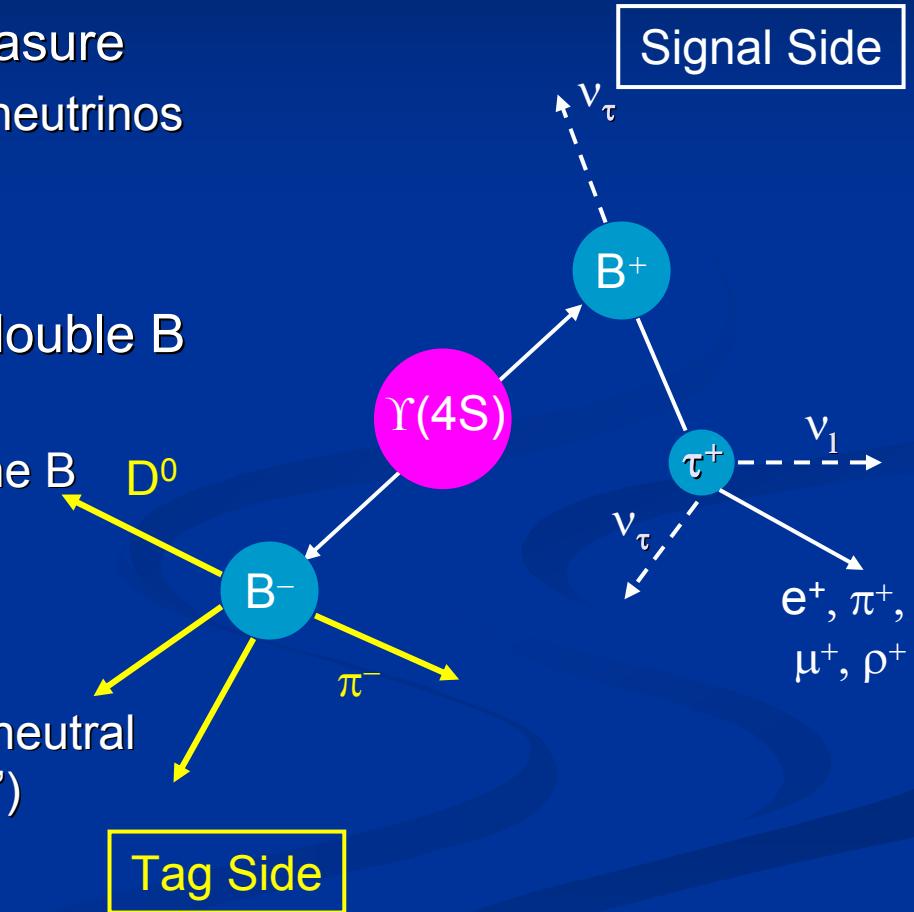


$$Br(B^+ \rightarrow l^+ \nu_l)_{SM} = \frac{G_F^2}{8\pi} m_B m_l^2 \tau_B \left(1 - \frac{m_l^2}{m_B^2} \right)^2 f_B^2 |V_{ub}|^2$$

Hou, PRD 48, 2342 (1993)

$B^+ \rightarrow \tau^+ \nu$: Analysis Overview

- Experimentally challenging to measure
 - Final state contains two or more neutrinos
 - Less kinematic constraints
- Method : Take the advantage of double B production in $\Upsilon(4S)$
 - Full or partial reconstruction of one B (“Tag B”)
 - $B^- \rightarrow D^0 l^- \bar{\nu} X^0$ (Semileptonic Tag)
 - $B^- \rightarrow D^{0(*)} X^-$ (**Hadronic Tag**)
 - Attribute remaining charged and neutral particles to the other B (“signal B”)



$B^+ \rightarrow \tau^+ \nu$: Tag Side

■ Hadronic: $B^- \rightarrow D^{(*)0} X^- (\sim 2700/\text{fb}^{-1})$

- $D^{*0} \rightarrow D^0 (\pi^0/\gamma)$
 $D^0 \rightarrow K^+\pi^-, K^+\pi^-\pi^0, K^+\pi^-\pi^-\pi^+, K_S\pi^+\pi^-$
- $X^+ = n_1 K^\pm + n_2 \pi^\pm + n_3 K_S + n_4 \pi^0$
 $(n_1+n_2 \leq 5, n_3 \leq 2, n_4 \leq 2)$

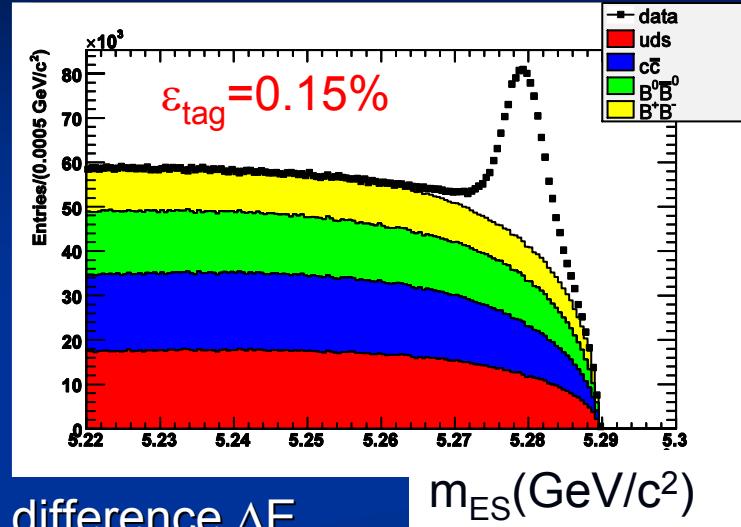
■ Full reconstruction of an event

- Beam energy-substituted mass m_{ES} ; Energy difference ΔE

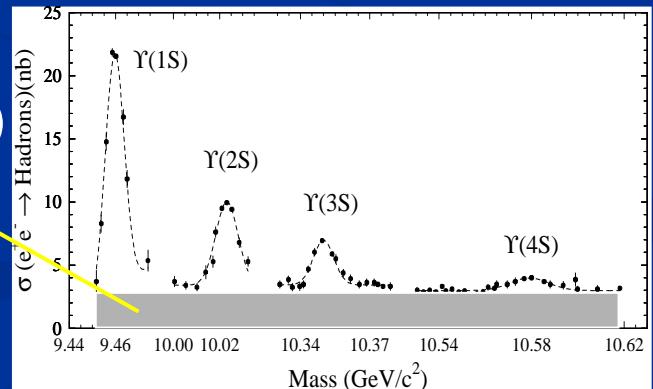
$$m_{ES} \equiv \sqrt{E_{beam}^{*2} - p_B^{*2}} \sim m_B \quad \Delta E \equiv E_B^* - E_{beam}^* \sim 0$$

■ Backgrounds

- Events not from $B\bar{B}$, $e^+e^- \rightarrow q\bar{q}$ ($q=u,d,s,c,\tau$)
“continuum”
- Mis-reconstructed B candidates
“combinatorial”

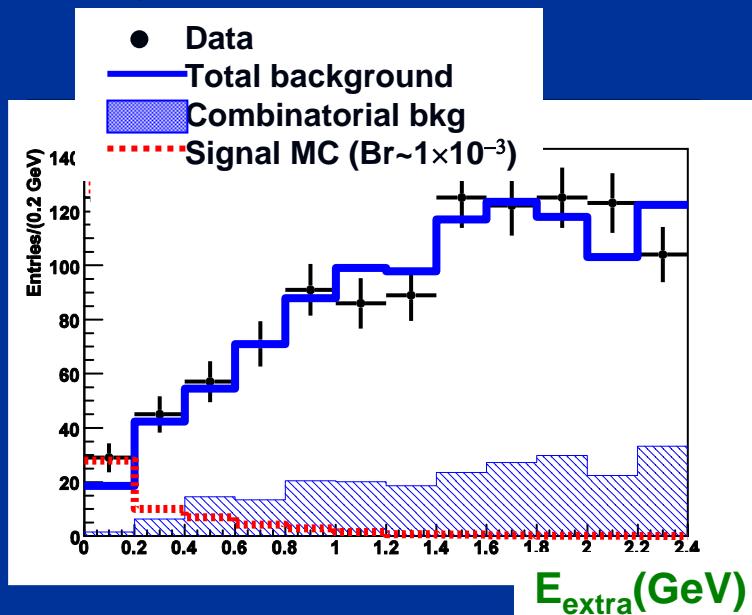


$m_{ES}(\text{GeV}/c^2)$



$B^+ \rightarrow \tau^+ \nu$: Signal Side

- Signal events $B^+ \rightarrow \tau^+ \nu$
 - $\tau^+ \rightarrow e^+ \nu \nu, \mu^+ \nu \nu, \pi^+ \nu, \pi^+ \pi^0 \nu$ (71%)
- Signal optimization for each mode separately
 - Particle ID, Charged track momentum, ρ quality ($\pi^+ \pi^0$ mode),..
 - E_{extra} sum of neutral energy not associated with Tag B or Signal B (π^0 in $\tau^+ \rightarrow \pi^+ \pi^0 \nu$)
 - $E_{\text{extra}} < 160, 100, 230$ and 290 MeV (use $s/(s+b)^{1/2}$ for optimization)
- Background is estimated from side band region ($0.4 < E_{\text{extra}} < 2.4$ GeV)



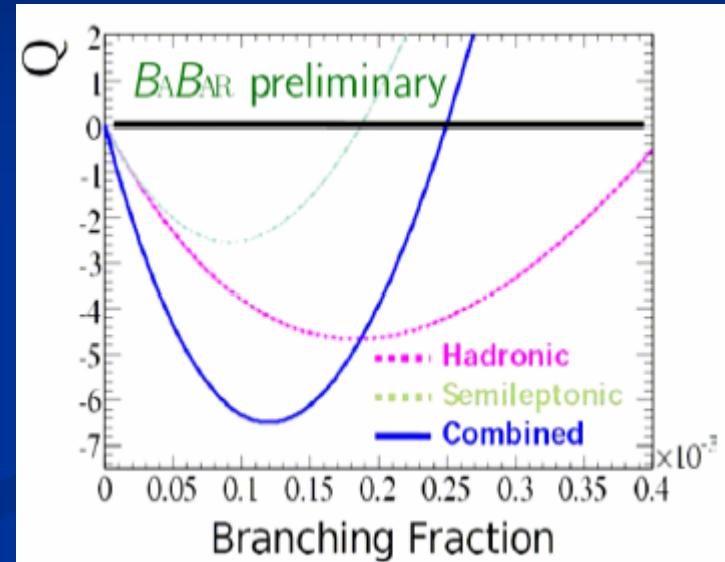
Mode	Expected background	Observed
$\tau \rightarrow e \nu \nu$	1.5 ± 1.4	4
$\tau \rightarrow \mu \nu \nu$	1.8 ± 1.0	5
$\tau \rightarrow \pi \nu \nu$	6.8 ± 2.1	10
$\tau \rightarrow \pi \pi^0 \nu$	4.2 ± 1.4	5
All	14.3 ± 3.0	24

$B^+ \rightarrow \tau^+ \nu$: Branching Fraction Results

Signal yield is extracted from minimizing the likelihood-based estimator

$$-2\ln Q = -2\ln(L(s+b)/L(b))$$

$$L(s+b) \equiv \prod_{i=1}^4 \frac{e^{-(s_i+b_i)}(s_i+b_i)^{n_i}}{n_i!}$$



arXiv:0705.1820
Submitted to PRD

$L = 346 \text{ fb}^{-1}$



	$Br(B^+ \rightarrow \tau^+ \nu_\tau) \times 10^4$	Significance $(f_B \cdot V_{ub}) \times 10^4$
Semileptonic	$0.9 \pm 0.6(\text{stat}) \pm 0.1(\text{sys})$	1.3σ $7.2_{-2.8}^{+2.0} \pm 0.2$
Hadronic	$1.8_{-0.9}^{+1.0} (\text{stat + bkg sys}) \pm 0.3(\text{other sys})$	2.2σ $10.1_{-2.5}^{+2.8} \pm 0.8$
Combined	$1.2 \pm 0.4(\text{stat}) \pm 0.3(\text{bkg sys}) \pm 0.2(\text{sys})$	2.6σ --

Constraints from $B^+ \rightarrow \tau^+ \nu$

CKMfitter, <http://ckmfitter.in2p3.fr>

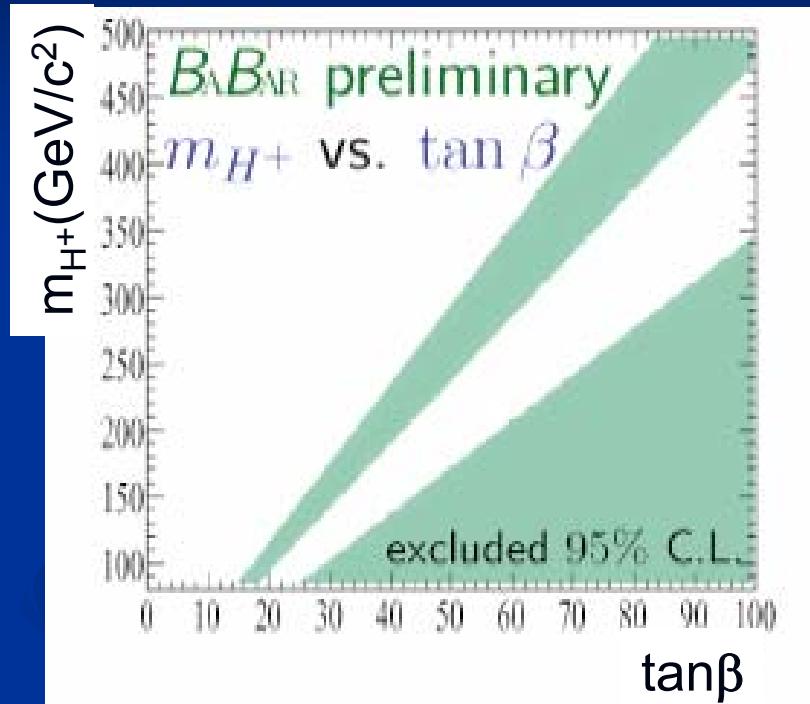
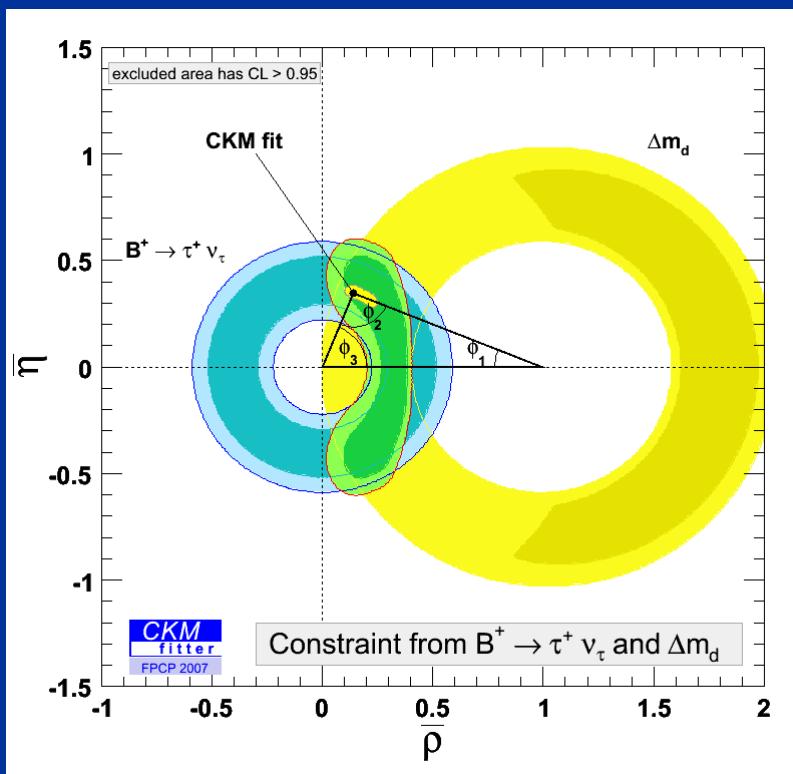
Exclusion plot in (ρ, η) plane

$f_B = (223 \pm 15 \pm 26) \text{ MeV}$

$B \rightarrow \tau \nu$ (Belle and BaBar)

$\Delta m_d = (0.507 \pm 0.005) \text{ ps}^{-1}$ (PDG'07)

Inputs

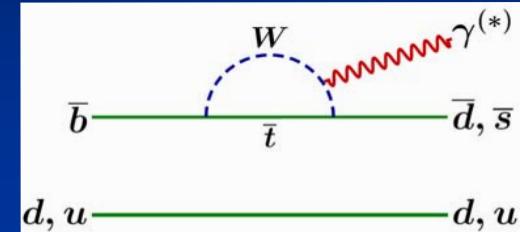


Inputs

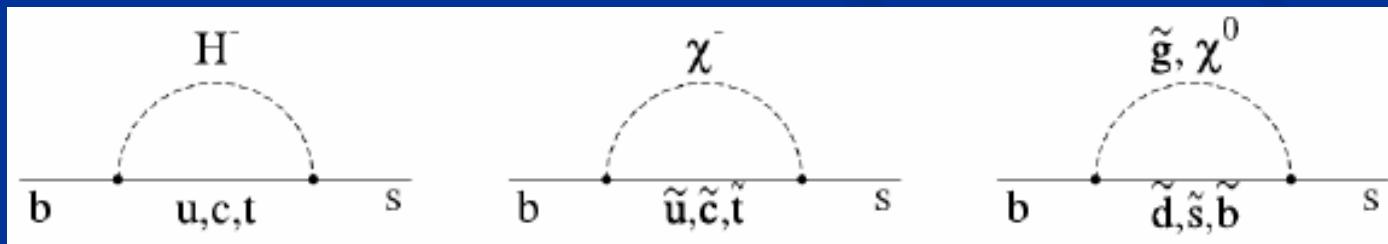
Exclusion plot in $(\tan \beta, m_{H^+})$ plane
Babar combined result
 $m_{H^+} > 79.3 \text{ GeV}/c^2$ (LEP limit)

Inclusive $b \rightarrow s\gamma$ decays

- FCNC decay dominated by W-loop
- Not so rare decay , SM $\text{Br}(b \rightarrow s\gamma) \sim \mathcal{O}(10^{-4})$
- Recent NNLO calculations ($E_\gamma > 1.6 \text{ GeV}$)
 $\text{Br}(b \rightarrow s\gamma) = (3.0\text{-}3.5) \times 10^{-4}$ (7-14)% uncertainties
 HFAG 2006 average $\text{Br}(b \rightarrow s\gamma) = (3.55 \pm 0.26) \times 10^{-4}$ (7%)



- Inclusive $b \rightarrow (s,d)\gamma$ is one of the cleanest decays for searching for NP
 - Look for any deviation in observables (branching fraction, CP asymmetry etc)



- γ spectrum is sensitive to mass and momentum of b quark inside B meson

$$\text{First Moment} = \langle E_\gamma^B \rangle \approx \frac{m_b}{2}$$

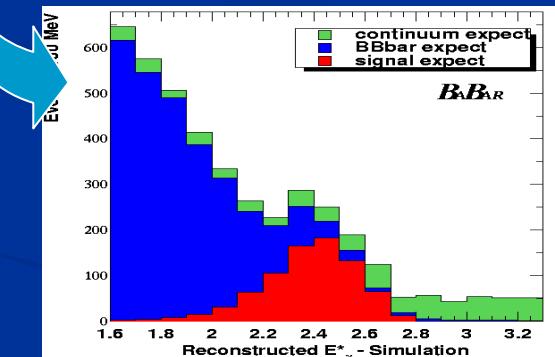
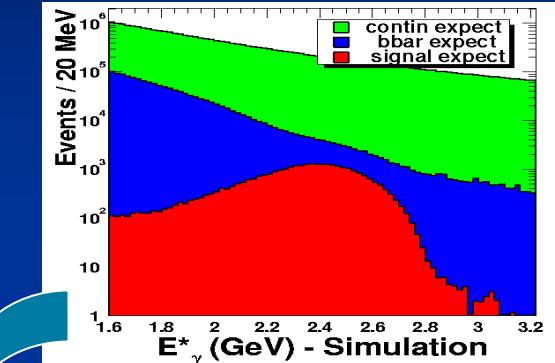
$$\text{Second Moment} = \langle (E_\gamma^B)^2 \rangle - \langle E_\gamma^B \rangle^2 \approx \mu_\pi^2$$

$b \rightarrow s\gamma$: Previous Measurements

- Inclusive methods
 - Request high energetic γ
 - No X_s sensitivity to fragmentation
 - Huge background from continuum events ($e^+e^- \rightarrow q\bar{q}$, $q = u,d,s,c$) with γ from ISR, π^0 or η
 - A lepton tag on the other B
 - Need to translate to B rest frame

- Semi-Inclusive methods
 - Sum of 38 exclusive decays ($K\pi\pi$, $K_S\pi$, etc)
 - Experimentally easier
 - B is fully reconstructed (m_{ES} and ΔE)
 - Photon in the B rest frame
 - Large error due to form factors

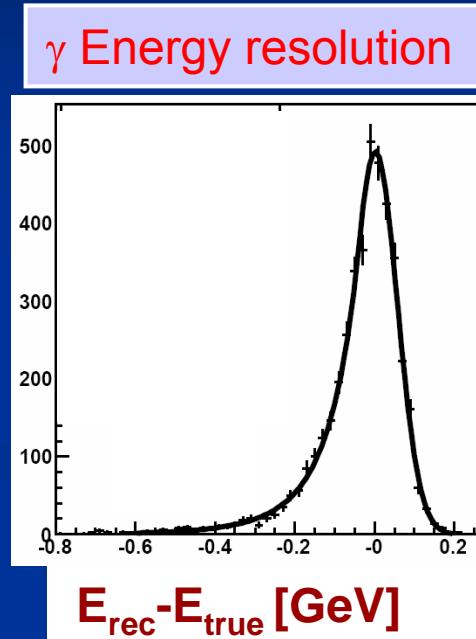
Lepton tag



$$E_\gamma = \frac{M_B^2 - M(X_S)^2}{2M_B}$$

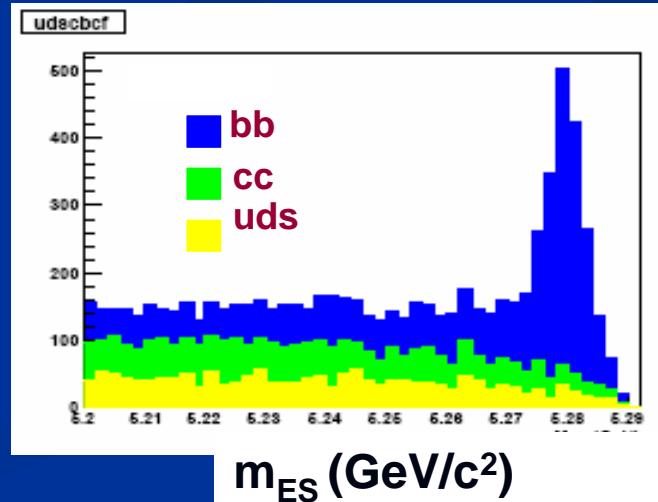
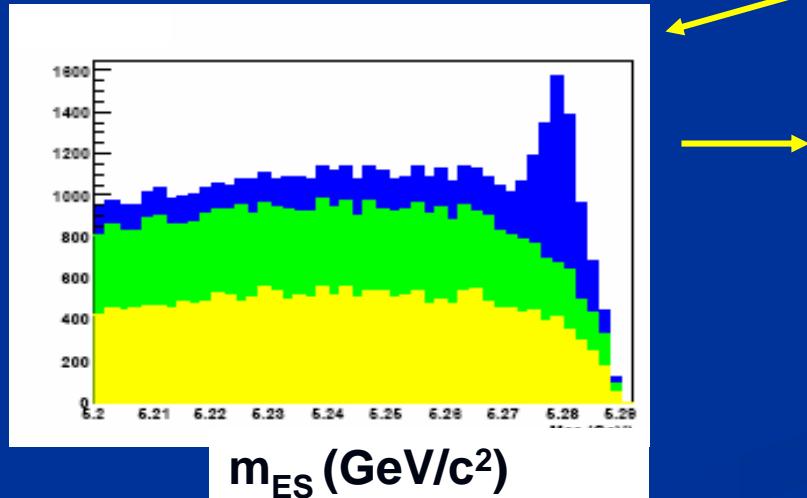
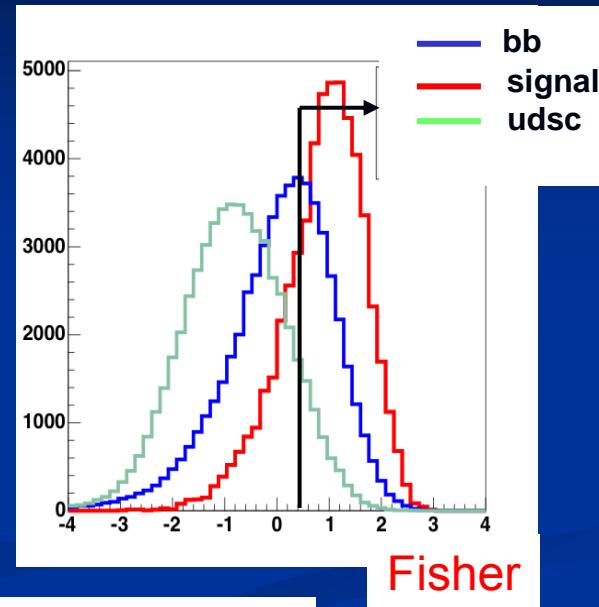
$b \rightarrow s\gamma$: New technique

- Hadronic Tag method
- Fully reconstruct one B with hadronic decays:
 $B \rightarrow D^{(*)} X$ (X : combination of π , and K with $|\Sigma q|=1$)
 - Flavour, charge and four momentum of signal B known
- Photon energy can be measured in B rest frame
 - Require a high energy photon ($E_\gamma > 1.3$ GeV in B frame) in other B (signal B)
- Small Tag efficiency ($\sim 0.3\%$)
- Photon energy spectrum and partial branching fractions in bins of photon energy
 - Number of events determined from fit to m_{ES} in E_γ bins



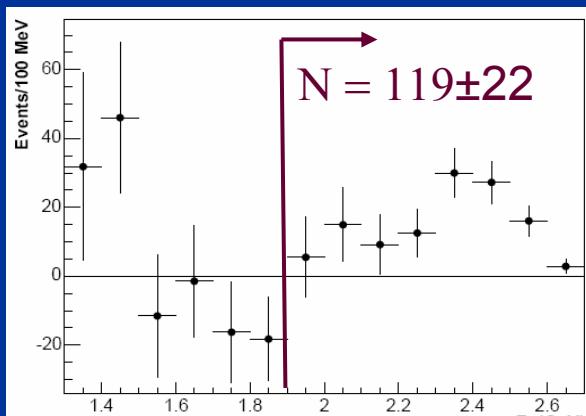
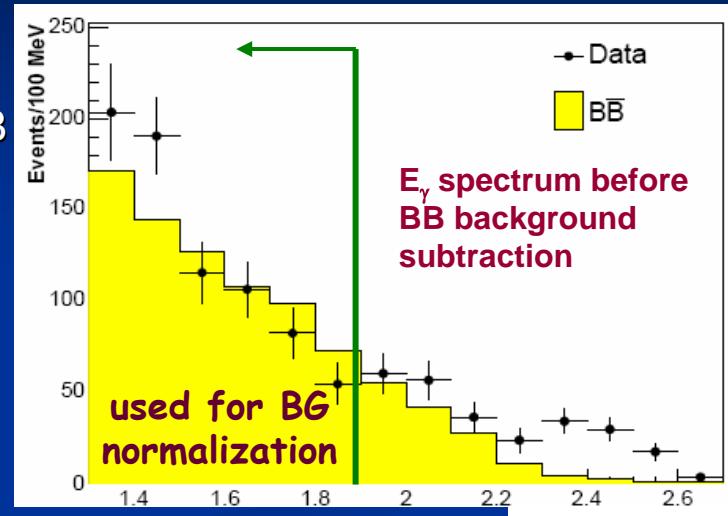
$b \rightarrow S\gamma$: Background Rejection

- Main backgrounds
 - Photons originating from π^0 , η , ρ
 - Continuum background: suppress using Fisher discriminants
 - 12 inputs based on event shapes variables
- Selection optimized by maximizing $s/(s+b)^{1/2}$

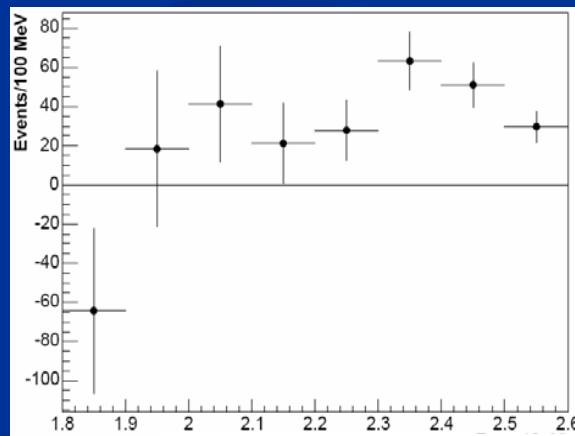


$b \rightarrow s\gamma$: Photon Energy Spectrum

- Photon energy spectrum
 - b quark mass (m_b) and momentum inside the B meson (μ_π^2)
 - Input for $|V_{u(c)b}|$ extraction from semileptonic B decays
- In two body decays, γ is monochromatic energy at b quark rest frame, due to “Fermi motion” the energy spectrum is smeared

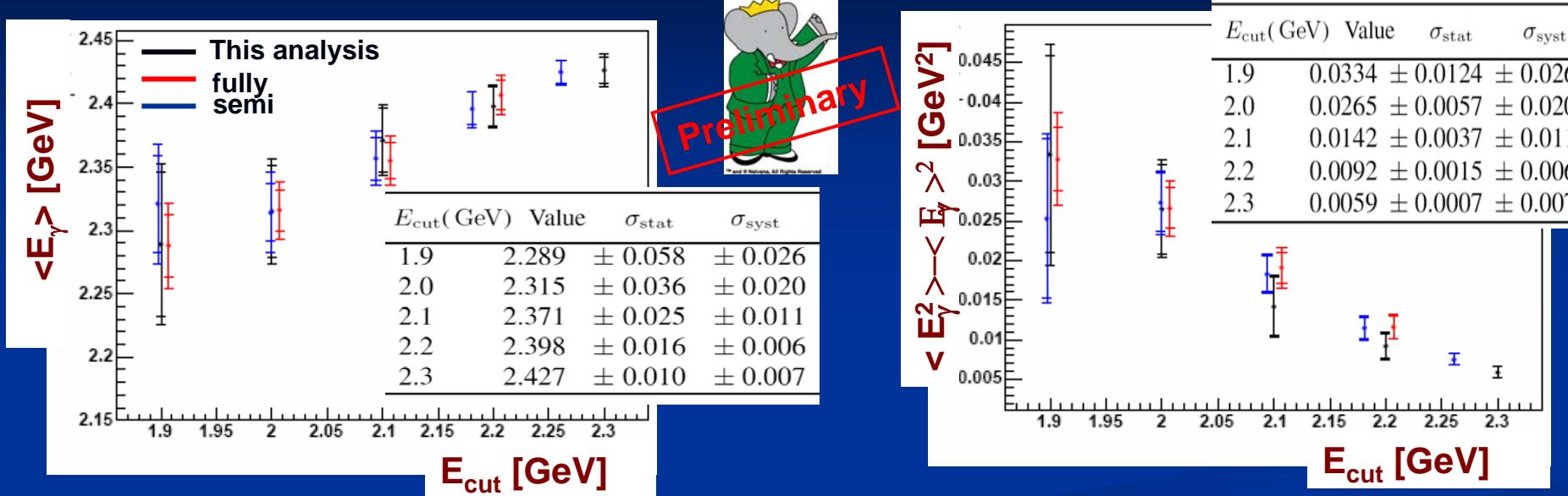


Background subtracted E_γ (GeV)



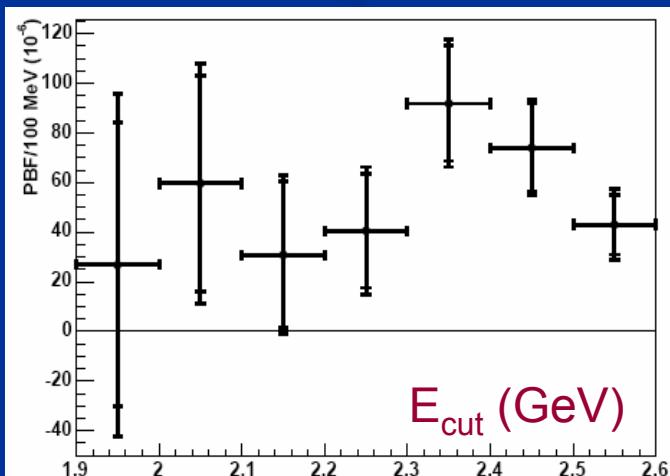
Resolution/Efficiency corrected E_γ (GeV)

$b \rightarrow s\gamma$: Moments & Partial Branching Fraction



- Photon energy moments from different methods agree well
- Next Step: Extract HQE parameters, combine the results and measure Asymmetries

$BF[E_\gamma > E_{cut}] / 10^{-6}$			
E_{cut} (GeV)	Value	σ_{stat}	σ_{syst}
1.9	366	± 85	± 59
2.0	339	± 64	± 47
2.1	278	± 48	± 34
2.2	248	± 38	± 26
2.3	207	± 30	± 19



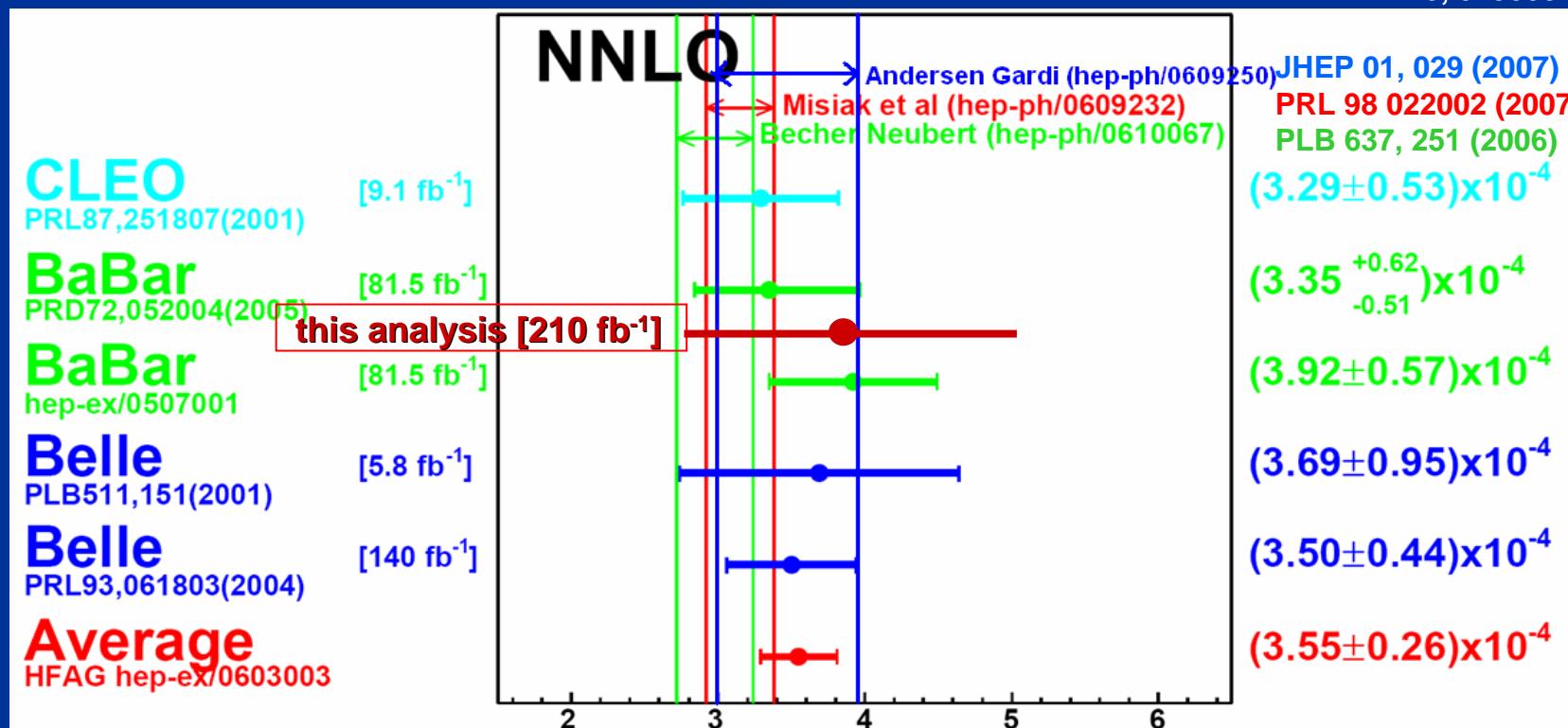
- Statistical error dominant
- Systematic error will be reduced with more data as well

$b \rightarrow s\gamma$: Branching Fraction

$$E_\gamma > 1.9 \text{ GeV} \quad \text{Br}(B \rightarrow X_s \gamma) = (3.66 \pm 0.85 \pm 0.59) \times 10^{-4}$$

$$E_\gamma > 1.6 \text{ GeV} \quad \text{Br}(B \rightarrow X_s \gamma) = (3.91 \pm 0.91 \pm 0.63) \times 10^{-4}$$

Extrapolation
down to 1.6 GeV
Buchmuller and Flacher
PRD 73, 073008 (2006)



$B^0 \rightarrow K^{*0}\gamma$: Time dependent CP Asymmetry

- Interference between $B^0 \rightarrow K^{*0}(K_s\pi^0)\gamma$ (decay) and $B^0 \rightarrow \bar{B}^0 \rightarrow K^{*0}(K_s\pi^0)\gamma$ (mixing) is suppressed due to photon polarization
 - Left-handed $\gamma(B^0)$ and right handed $\gamma(\bar{B}^0)$
- CP asymmetry measures the interference
 - SM : $A_{CP} \sim -0.02$
(Ball and Zwicky, PLB 642, 478 (2006))
- Time evolution of the $B^0 \rightarrow K^{*0}\gamma$

$$A_{CP}(t) = \frac{\Gamma(\bar{B}^0 \rightarrow K_s\pi^0\gamma) - \Gamma(B^0 \rightarrow K_s\pi^0\gamma)}{\Gamma(\bar{B}^0 \rightarrow K_s\pi^0\gamma) + \Gamma(B^0 \rightarrow K_s\pi^0\gamma)}$$
$$= S \sin(\Delta m t) - C \cos(\Delta m t)$$

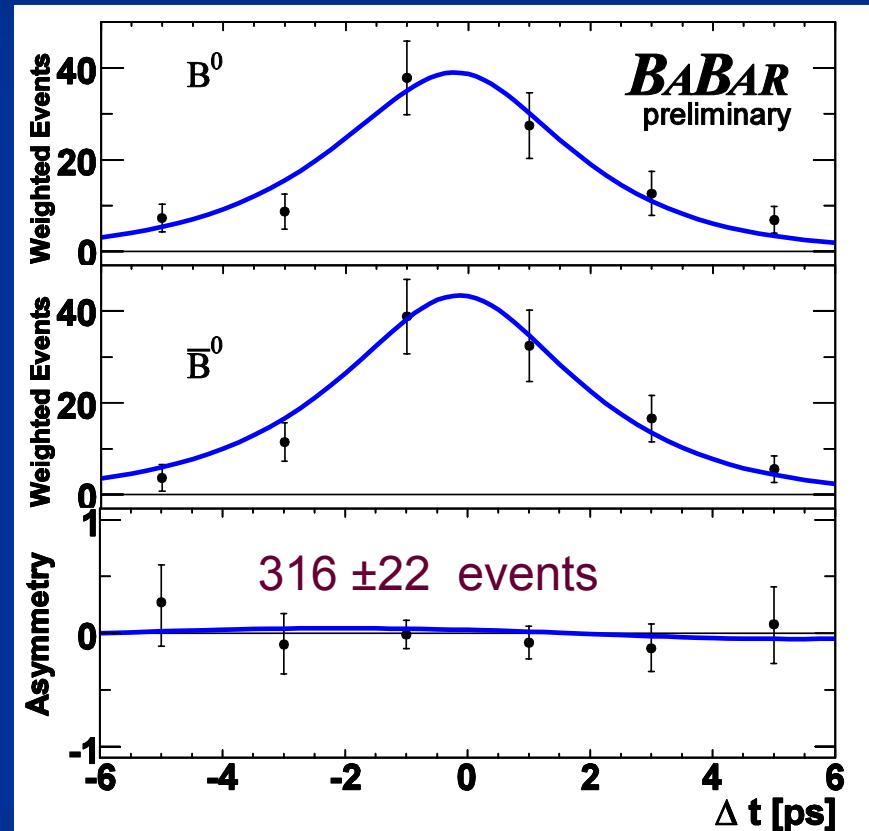
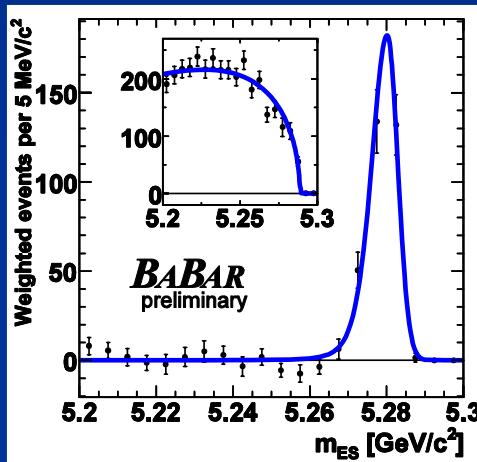
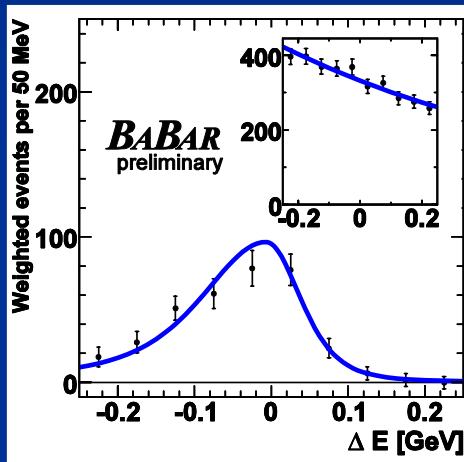
$$P_{\pm}(\Delta t) = \frac{e^{-|\Delta t|/\tau_B}}{4\tau_B} \times [1 \pm S \sin(\Delta m_d \Delta t) \mp C \cos(\Delta m_d \Delta t)]$$

S: CP violation in interference between decay and mixing
C: Direct CPV

(Details on the method: Talk presented this morning by Jacques Chauveau - Measurements of CP violation in B decays and CKM parameters)

$B^0 \rightarrow K^{*0}\gamma$: Time dependent CP Asymmetry

- $\Delta t = t_{\text{sig}} - t_{\text{tag}}$
- t_{sig} : decay time $B^0 \rightarrow K_S\pi^0\gamma$ ($K_S \rightarrow \pi^+\pi^-$)
 t_{tag} : B_{tag} (reconstructed from the rest of the tracks and clusters)



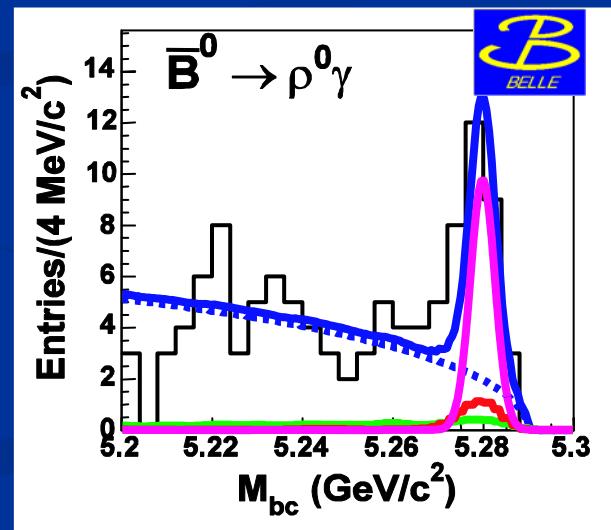
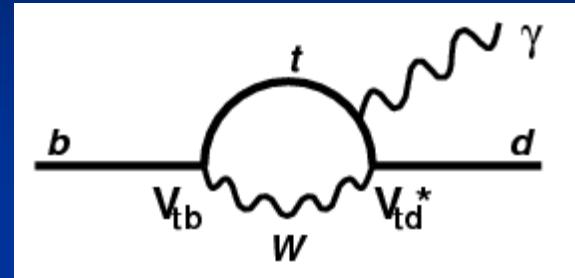
$L = 391 \text{ fb}^{-1}$

$$S_{K^*\gamma} = -0.08 \pm 0.31 \pm 0.05$$

$$C_{K^*\gamma} = -0.15 \pm 0.17 \pm 0.03$$

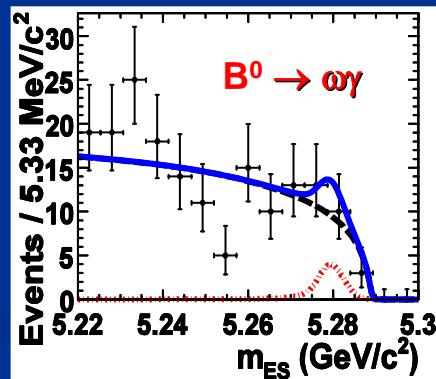
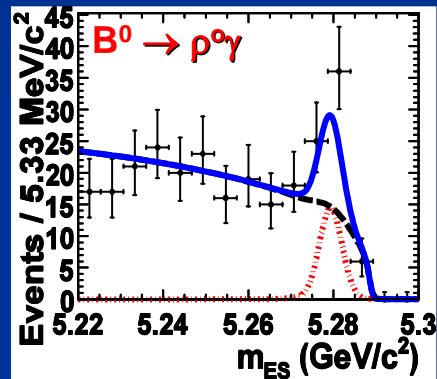
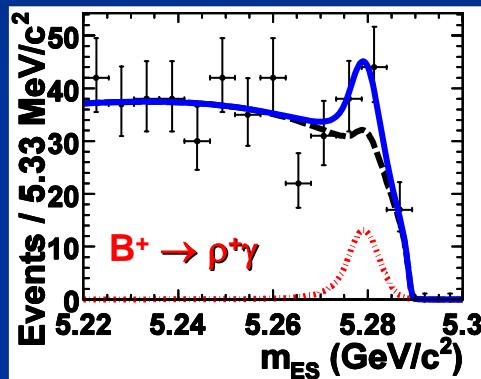
Exclusive $b \rightarrow d\gamma$ Decays

- $B^\pm \rightarrow \rho^\pm \gamma, B^0 \rightarrow (\rho^0, \omega) \gamma$
- Suppressed by $|V_{td}/V_{ts}|^2 \sim 0.04$ compared to $b \rightarrow s\gamma$
 - SM: $\text{Br}(B \rightarrow (\rho, \omega)\gamma) \sim (0.9-1.8) \times 10^{-6}$
- Difference between $|V_{td}/V_{ts}|$ from this decays and B_s mixing can indicate NP
- First observation by Belle on $B^0 \rightarrow \rho^0 \gamma$ decay with 5.2σ significance (**PRL 96, 221601 2006**)
- BaBar measurements
 - Results at 316 fb^{-1} presented here (**PRL 98 151802 (2007)**)



Exclusive $b \rightarrow d\gamma$: Analysis & Results

- Reconstruct $\rho^{+(0)} \rightarrow \pi^+ \pi^0(-)$ $\omega \rightarrow \pi^+ \pi^- \pi^0$
- Backgrounds (continuum, $B \rightarrow K^* \gamma$ and γ from π^0 , η) rejection
- Signal extraction from maximum 4D (5D) likelihood fit for ρ (ω)



Mode	N_{sig}	Significance	$Br(10^{-6})$
$B^+ \rightarrow \rho^+ \gamma$	$42.0^{+14.0}_{-12.7}$	3.8σ	$1.10^{+0.37}_{-0.33} \pm 0.09$
$B^0 \rightarrow \rho^0 \gamma$	$38.7^{+10.6}_{-9.8}$	4.9σ	$0.79^{+0.22}_{-0.20} \pm 0.06$
$B^0 \rightarrow \omega \gamma$	$11.0^{+6.7}_{-5.6}$	2.2σ	$0.40^{+0.24}_{-0.20} \pm 0.05$
$B \rightarrow (\rho, \omega)\gamma$		6.4σ	$1.25^{+0.25}_{-0.24} \pm 0.09$

Isospin-averaged
 $Br(B \rightarrow (\rho, \omega)\gamma)$

$$\begin{aligned}
 Br(B \rightarrow (\rho, \omega)\gamma) &= B(B^- \rightarrow \rho^- \gamma) \\
 &= 2 \frac{\tau_{B^+}}{\tau_{B^0}} B(B^0 \rightarrow \rho^0 \gamma) \\
 &= 2 \frac{\tau_{B^+}}{\tau_{B^0}} (B^0 \rightarrow \omega \gamma)
 \end{aligned}$$

First evidence for charged mode

First BaBar observation of $B \rightarrow (\rho, \omega)\gamma$

Exclusive $b \rightarrow d\gamma$: $|V_{td}/V_{ts}|$

Branching fraction results from BaBar and Belle agree well

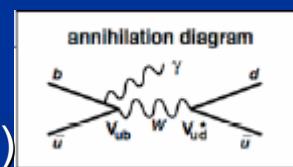
$\text{Br}(B \rightarrow (\rho, \omega)\gamma)(10^{-6})$	
BaBar	$1.25^{+0.25}_{-0.24} \pm 0.09$
Belle	$1.13 \pm 0.20 \pm 0.11$

(Belle preliminary result presented at LP07 by M. Nakao, KEK)

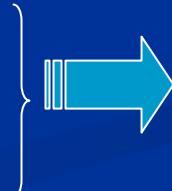
Ratio of branching fraction can be used for the extraction of $|V_{td}/V_{ts}|$

$$\frac{\text{Br}(B \rightarrow (\rho, \omega)\gamma)}{\text{Br}(B \rightarrow K^*\gamma)} = \left| \frac{V_{td}}{V_{ts}} \right|^2 \left(\frac{1 - m_{\rho, \omega}^2 / m_B^2}{1 - m_{K^*}^2 / m_B^2} \right)^3 \zeta^2 [1 + \Delta R]$$

$\zeta = f_{K^*} / f_\rho$ f = form factor
 ΔR accounts for the annihilation diagram (not exist K^*)



Inputs
 $\zeta = 1.17 \pm 0.09$ (Ball and Zwicky, JHEP 0604, 046 (2006))
 $\Delta R = 0.1 \pm 0.1$ (Ali et al, PLB 595, 323 (2004))
 BaBar isospin-averaged Br



$$\left| \frac{V_{td}}{V_{ts}} \right| = 0.200^{+0.021}_{-0.020} (\text{exp}) \pm 0.015 (\text{th})$$

Exclusive $b \rightarrow d\gamma$: Constraints on UT

BaBar result:

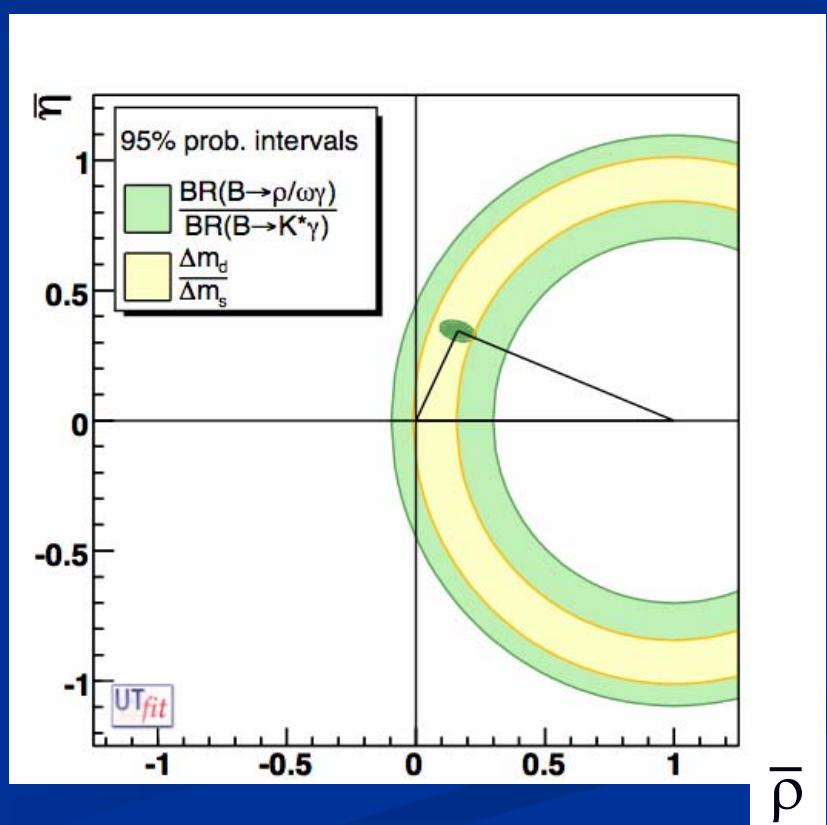
$$\left| \frac{V_{td}}{V_{ts}} \right| = 0.200^{+0.021}_{-0.020} (\text{exp}) \pm 0.015 (\text{th})$$

CDF (PRL 97, 242003 (2006))

$$\left| \frac{V_{td}}{V_{ts}} \right| = 0.2060 \pm 0.0007^{+0.0081}_{-0.0060}$$

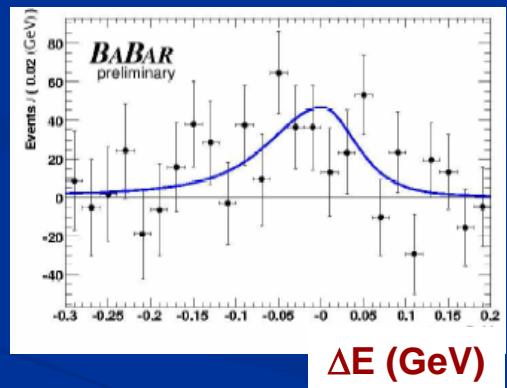
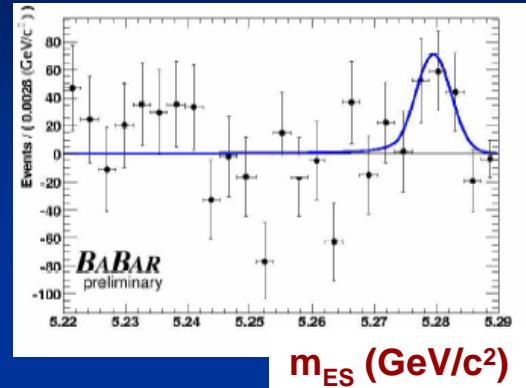
- Excellent agreement between two results
- The constraints on UT coming from two different physics is the same

<http://utfit.roma1.infn.it/>



Inclusive $b \rightarrow d\gamma$

- First inclusive search on $b \rightarrow d\gamma$
 - Sum of 7 exclusive decay modes
 - $B^0 \rightarrow \pi^+ \pi^- \gamma$, $B^+ \rightarrow \pi^+ \pi^0 \gamma$, $B^+ \rightarrow \pi^+ \pi^- \pi^+ \gamma$, $B^0 \rightarrow \pi^+ \pi^- \pi^0 \gamma$,
 $B^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^- \gamma$, $B^+ \rightarrow \pi^+ \pi^- \pi^+ \pi^0 \gamma$, $B^+ \rightarrow \pi^+ \eta \gamma$
- Hadronic mass system
 - $1.0 < M(X_d) < 1.8 \text{ GeV}/c^2$
 - Seven final states corresponds to $\sim 50\%$ of the total X_d fragmentation in this mass range
- $0.6 < M(X_{s(d)}) < 1.8 \text{ GeV}/c^2$ region used as control sample for Br of $B \rightarrow K^* \gamma$ ($B \rightarrow \pi^+ \pi^- \gamma$, $B^+ \rightarrow \pi^+ \pi^0 \gamma$, $B^0 \rightarrow \pi^+ \pi^- \pi^0 \gamma$)
- 2D (m_{ES} , ΔE) Unbinned-likelihood fit used for signal and background yields extraction
 - 348 fb^{-1} , 178 ± 53 signal events found



$$\sum_{X_d=1}^7 Br(B \rightarrow X_d \gamma) \Big|_{1.0 < X_d < 1.8 \text{ GeV}/c^2} = (3.1 \pm 0.9(\text{stat})^{+0.6}_{-0.5}(\text{sys}) \pm 0.5(\text{th})) \times 10^{-6}$$

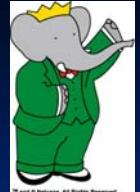
3.1 σ significance
First evidence for $b \rightarrow d\gamma$ outside $B \rightarrow (\rho, \omega)\gamma$ resonance

Next step: Extrapolate hadronic mass region, $|V_{td}/V_{ts}|$ extraction using $b \rightarrow s\gamma$

Summary

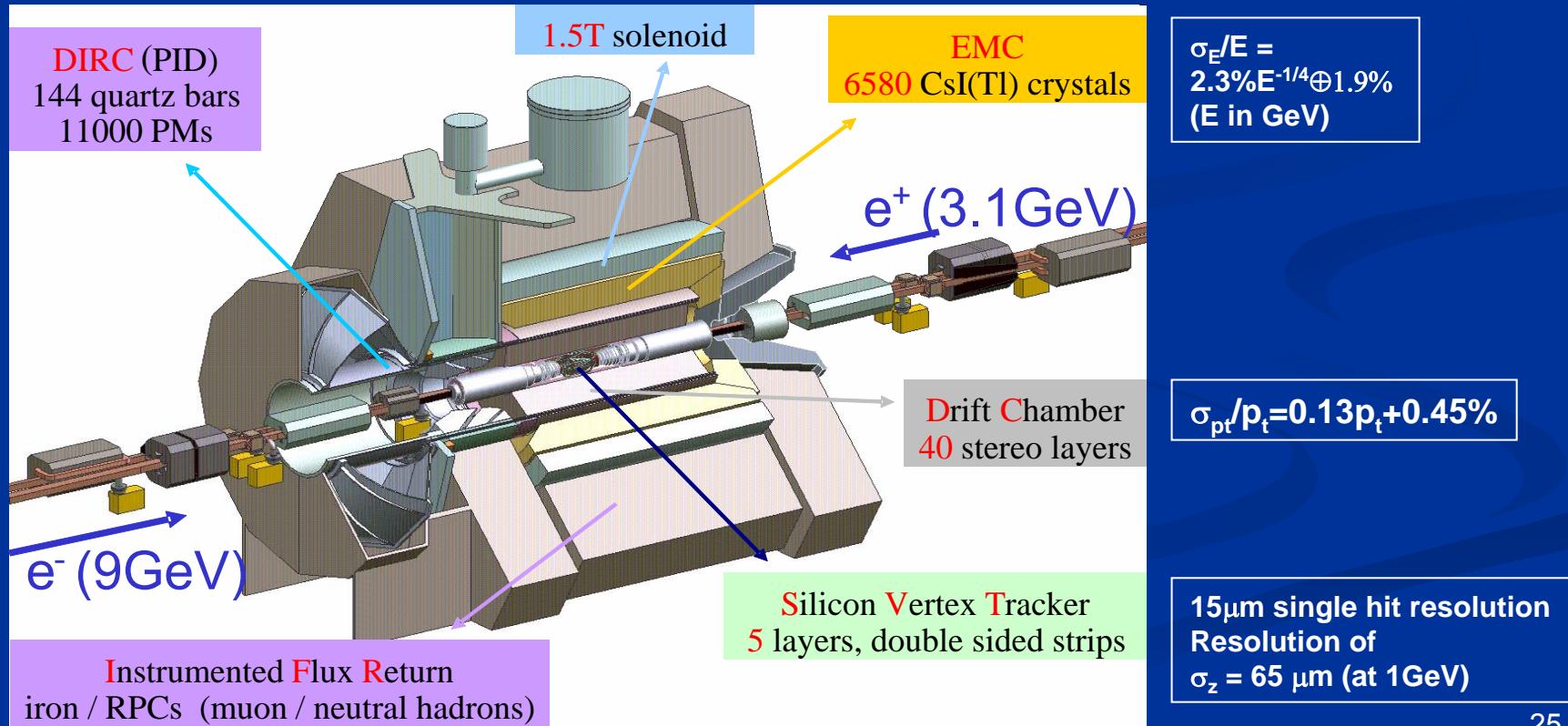
- Rare decays are very interesting place to study new physics and test the constraints on Unitarity Triangle
- $B^+ \rightarrow \tau^+ \nu$ signal seen and the sensitivity is approaching to SM rates
- Recent progress in $b \rightarrow s \gamma$ decays both
 - Theory: NNLO
 - and
 - Experimental (new approach)
 - Complementary to previous measurements (advantages direct information on photon B rest frame and better systematic control)
 - Different methods agree well
- No TDCP asymmetry is observed in $B \rightarrow K^{*0} \gamma$
- Exclusive $b \rightarrow d \gamma$ decays through $B \rightarrow (\rho, \omega) \gamma$
 - First evidence of $B^+ \rightarrow \rho^+ \gamma$ and first BaBar observation of isospin-averaged branching fraction
 - Excellent agreement on $|V_{td}/V_{ts}|$ from decay and B_s mixing (Tevatron)
- First evidence on inclusive $b \rightarrow d \gamma$ transition in a $M(X_d)$ outside ρ/ω resonances

Backup Slides

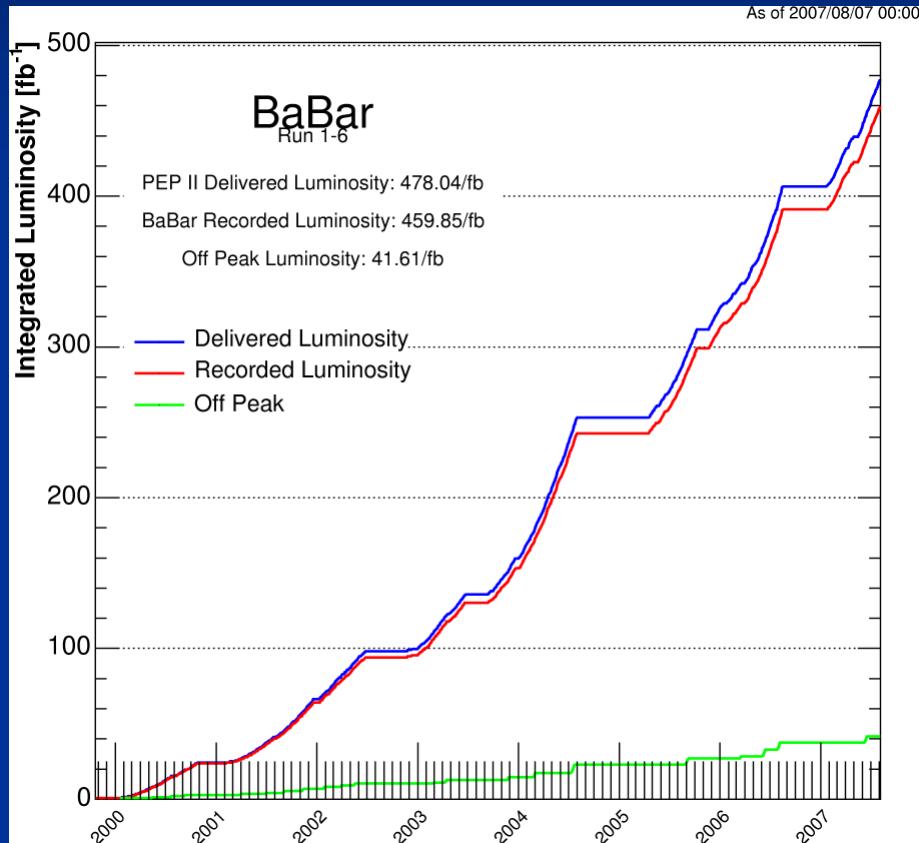


The BaBar Detector

- B factory experiment operated at SLAC since 1999
- Two asymmetric (electron & positron) beams at the center-of-mass energy of 10.58 GeV
- B mesons are produced in pairs: $e^+e^- \rightarrow \Upsilon(4S) \rightarrow BB$



The B Factory

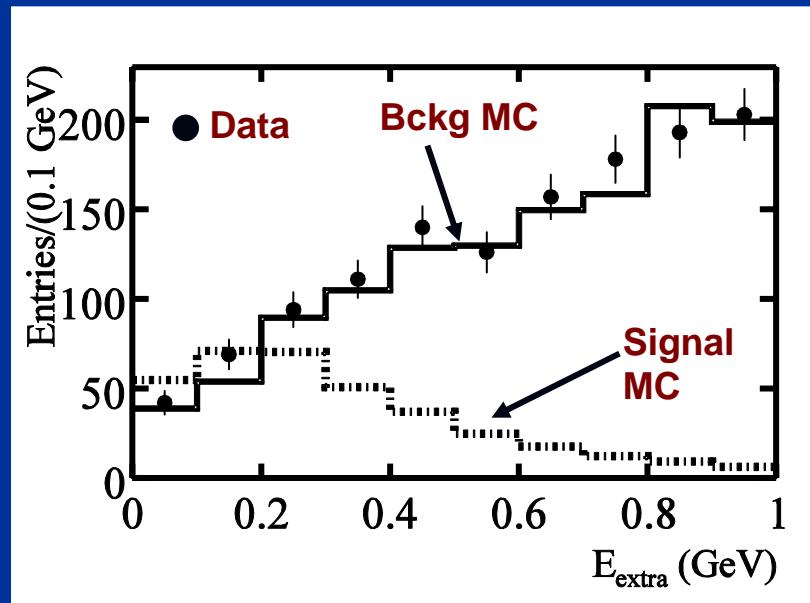


- Total ~500 fb⁻¹ data recorded until now at the $\Upsilon(4S)$ cm energy
- In addition, ~10% of total data with an energy that is 40 MeV less than the nominal c.m. energy
 - Background from continuum event
- BaBar/PEPII programme to run until end of summer 2008

$B^+ \rightarrow \tau^+ \nu$: Signal Side

Semileptonic
Tag

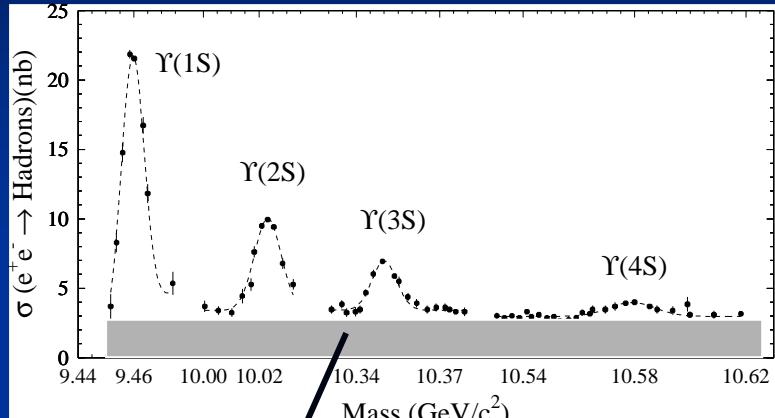
- Same τ decay modes as in hadronic tag analysis
- E_{extra} sum of charged tracks and neutral clusters which are not associated signal B or Tag B
 - $E_{\text{extra}} < 310$ (e), 260 (μ), 480 (π), 250 ($\pi\pi^0$) MeV
- Background estimated E_{extra} sideband ($E_{\text{extra}} > 500$ MeV) and verified with D^0 mass sideband (4σ and 9σ) above and below D^0 mass



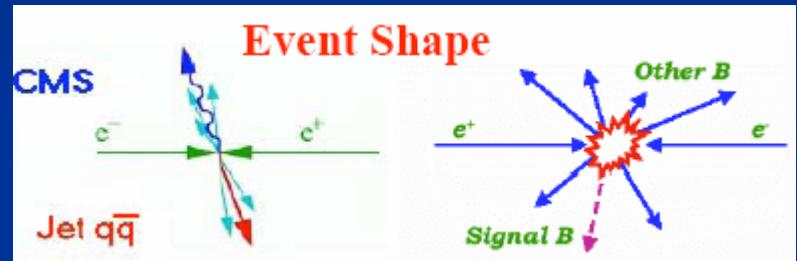
Mode	Expected background	Observed
$\tau \rightarrow e \nu \nu$	44.3 ± 5.2	59
$\tau \rightarrow \mu \nu \nu$	39.8 ± 4.4	43
$\tau \rightarrow \pi \nu \nu$	120.3 ± 10.2	125
$\tau \rightarrow \pi\pi^0\nu$	17.3 ± 3.3	18
All	221.7 ± 12.7	245

Continuum Background

$$\sigma(e^+e^- \rightarrow \gamma(4S) \rightarrow B\bar{B}) = 1.05 \text{ nb}$$



Events from continuum are jet-like while signal events are spherical



Non-resonant background “continuum”
 $e^+e^- \rightarrow q\bar{q}$ ($q=u,d,s,c,\tau$)

Event shape variables

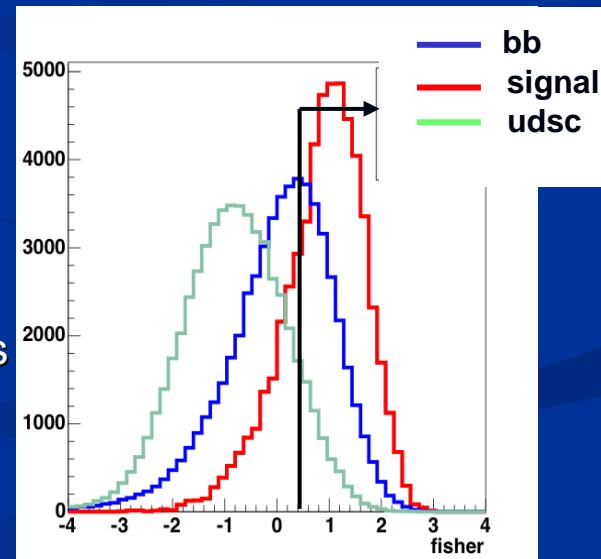
- $R_2 = H_2 / H_0$; $H_l = \sum_{i,j} |p_i||p_j| P_l(\cos(p_i, p_j))$

H_l = Fox-Wolfram moments, P_l = Legendre Polynomials

$R_2 \sim 1$ (continuum), $R_2 \sim 0$ (BB events)

Thrust, Sphericity, etc

- Combine the variables in Fisher discriminants, Neural network



Example for Fisher Discriminants

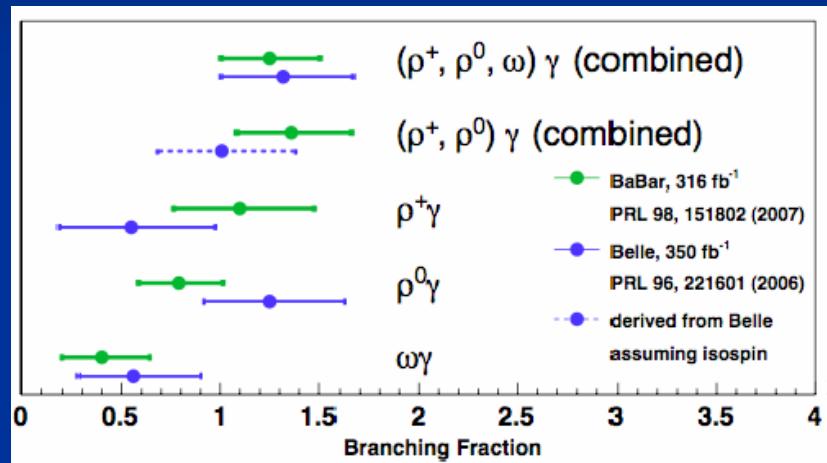
Inclusive $b \rightarrow s\gamma$ Decays

Systematic Uncertainties:

$E_{\text{cut}} (\text{GeV})$	Value	σ_{stat}	σ_{syst}	$\mathcal{B}(B \rightarrow X_s\gamma) (10^{-6})$				$B \rightarrow X_s\gamma$ Model	$b \rightarrow d\gamma$ Subtraction
				Background Modelling	M_{ES} fit Parameterisation	Detector Response			
1.9	366	± 85	± 59	35	44	16	8	2	
2.0	339	± 64	± 47	31	34	4	6	1	
2.1	278	± 48	± 34	22	24	6	5	1	
2.2	248	± 38	± 26	14	18	8	5	1	
2.3	207	± 30	± 19	10	14	1	5	1	

Exclusive $b \rightarrow d\gamma$ Decays

Comparison between BaBar and Belle results



	$\text{Br}(B \rightarrow (\rho, \omega)\gamma)(10^{-6})$
BaBar	$1.25^{+0.25}_{-0.24} \pm 0.09$
Belle	$1.32^{+0.34+0.10}_{-0.31-0.09}$
Average	$1.28^{+0.20}_{-0.19} \pm 0.06$

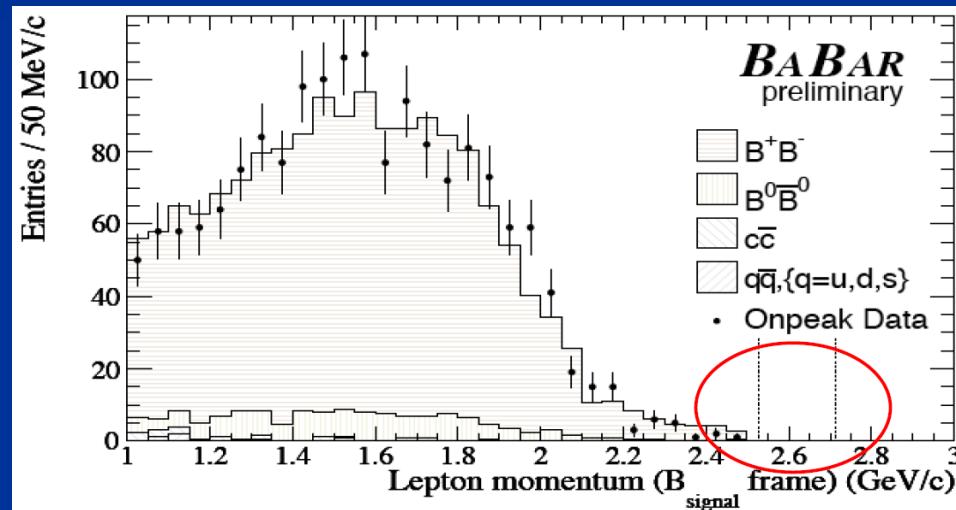
$B^+ \rightarrow (e^+, \mu^+) \nu$

- SM prediction
 - $B(B^+ \rightarrow e^+ \nu) \sim 10^{-12}$
 - $B(B^+ \rightarrow \mu^+ \nu) \sim 4 \times 10^{-7}$
- Search done using 209 fb^{-1}
- No events observed in either mode
- Expected background events
 $e: 0.23 \quad \mu: 0.12$
- @90% CL

$$B(B^+ \rightarrow e^+ \nu) < 7.9 \times 10^{-6}$$

$$B(B^+ \rightarrow \mu^+ \nu) < 6.2 \times 10^{-6}$$

[arXiv:hep-ex/0607110v1](https://arxiv.org/abs/hep-ex/0607110v1)



$B^+ \rightarrow l^+ \nu \gamma$

- Due to photon in the final state, no helicity suppression
 - Branching fraction is enhanced
 - SM prediction: $(1\text{-}5) \times 10^{-6}$ (Korchemsky, Pirjol, and Yan, PRD 61, 114510 2000)

$$\Gamma(B^+ \rightarrow l^+ \nu \gamma) = \alpha \frac{G_F^2 |V_{ub}|^2 m_B^5}{288\pi^2} f_B^2 \left(\frac{Q_u}{\lambda_B} - \frac{Q_b}{m_b} \right)$$

$\Lambda \sim B$ light cone
distribution amplitude

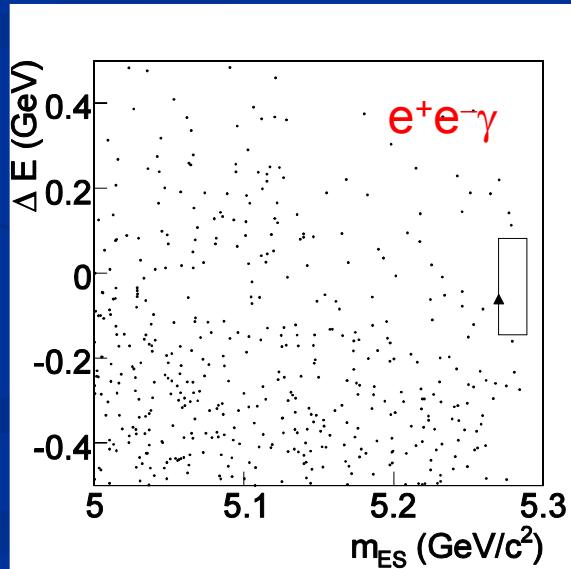
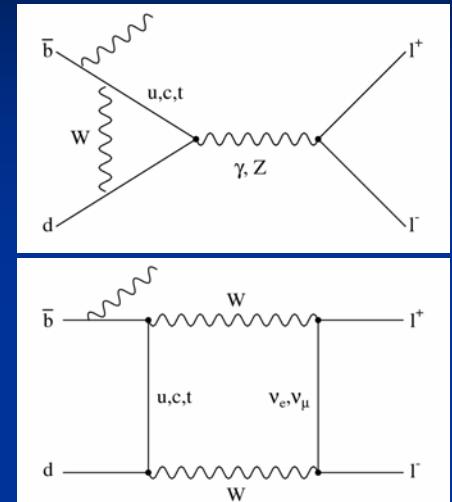
- 90% CL (210.5 fb^{-1} [0704.1478 \[hep-ex\]](#))
 - $B(B \rightarrow \mu \nu \gamma) < 2.1 \times 10^{-6}$
 - $B(B \rightarrow e \nu \gamma) < 2.8 \times 10^{-6}$
 - $B(B \rightarrow l \nu \gamma) < 2.3 \times 10^{-6}$
- Experimental sensitivity reaching to theoretical prediction

$B^0 \rightarrow l^+ l^- \gamma$

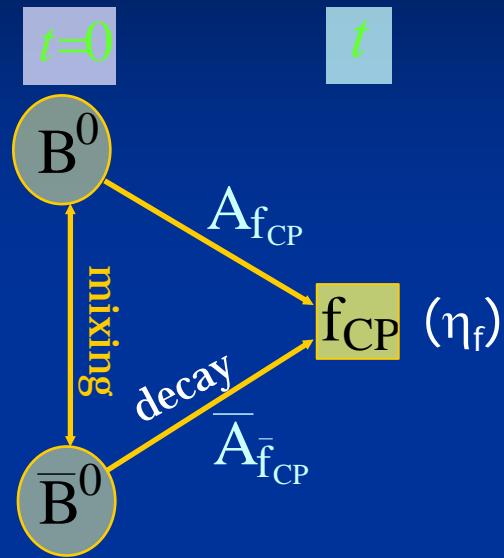
- First search on $B^0 \rightarrow l^+ l^- \gamma$ ($l=e, \mu$) FCNC process
 - Main contributions: photon emission from one of the initial quark
 - Not helicity suppressed, still Br is small
 - SM prediction: $\text{Br} \sim \mathcal{O}(10^{-10})$
- m_{ES} and ΔE for two leptons and a photon
- Backgrounds: QED process, J/Ψ , $\Psi(2S)$, π^0 , continuum.
- 292 fb^{-1} , limits are set at 90% CL

[arXiv:0706.2870 \[hep-ex\]](https://arxiv.org/abs/0706.2870), submitted to PRL

	N_{obs}	N_{bkg}	$\varepsilon(\%)$	$\text{Br}(B^0 \rightarrow l^+ l^- \gamma)$
e	1	$1.75 \pm 1.38 \pm 0.36$	7.4 ± 0.3	1.2×10^{-7}
μ	1	$2.66 \pm 1.40 \pm 1.58$	5.2 ± 0.2	1.5×10^{-7}



Time Dependent Asymmetry



$$A_{CP}(t) = \frac{N(\bar{B}^0(t) \rightarrow f_{CP}) - N(B^0(t) \rightarrow f_{CP})}{N(\bar{B}^0(t) \rightarrow f_{CP}) + N(B^0(t) \rightarrow f_{CP})}$$

$$= S_f \sin(\Delta m t) - C_f \cos(\Delta m t)$$

$$C_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \quad S_f = \frac{2 \operatorname{Im} \lambda_f}{1 + |\lambda_f|^2} \quad \lambda_f = \frac{q}{p} \cdot \frac{\bar{A}_f}{A_f}$$

